

Dark Energy after DESI DR2

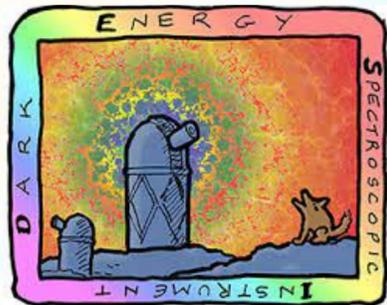
Rodrigo Calderón

Institute of Physics (FZU), Czech Academy of Sciences

In collaboration with K. Lodha, A. Shafieloo, E. Linder, W. Matthewson
& DESI collaboration

CosmoGrav - Spring 2025

07/04

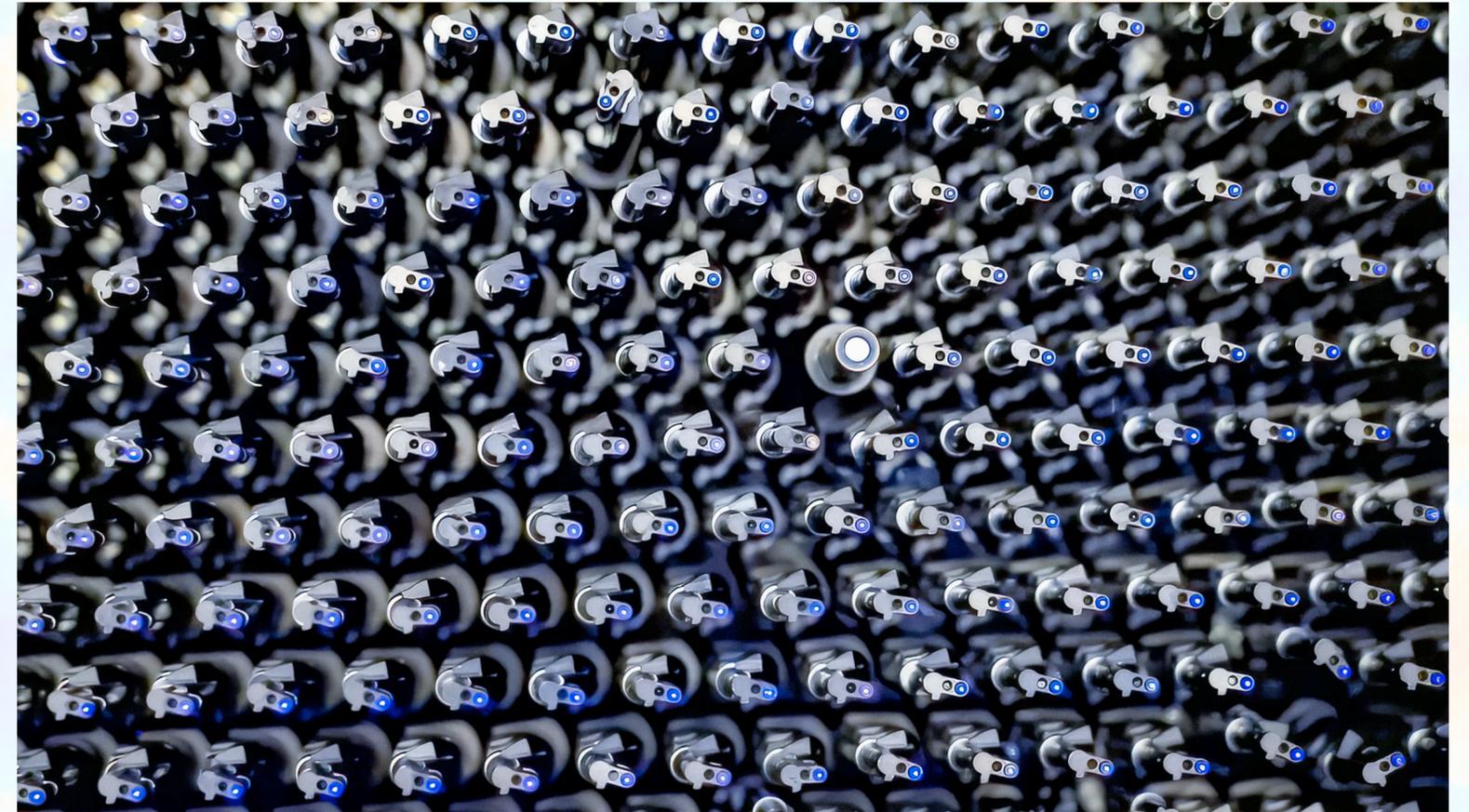


Co-funded by
the European Union



Dark Energy Spectroscopic Instrument

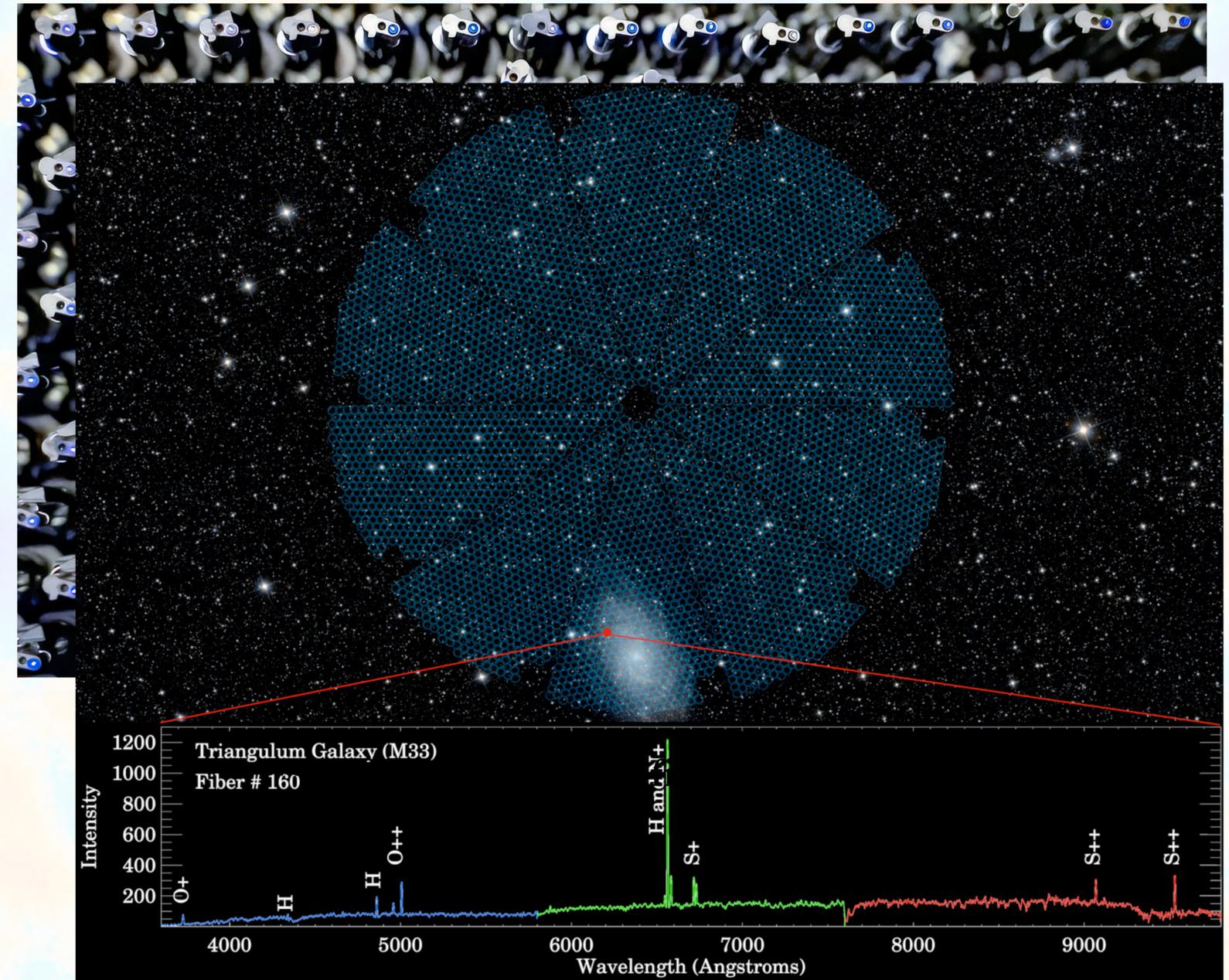
The era of Stage-IV surveys: DESI, Euclid, Rubin



~5,000 (robot) optic fiber positioners

Dark Energy Spectroscopic Instrument

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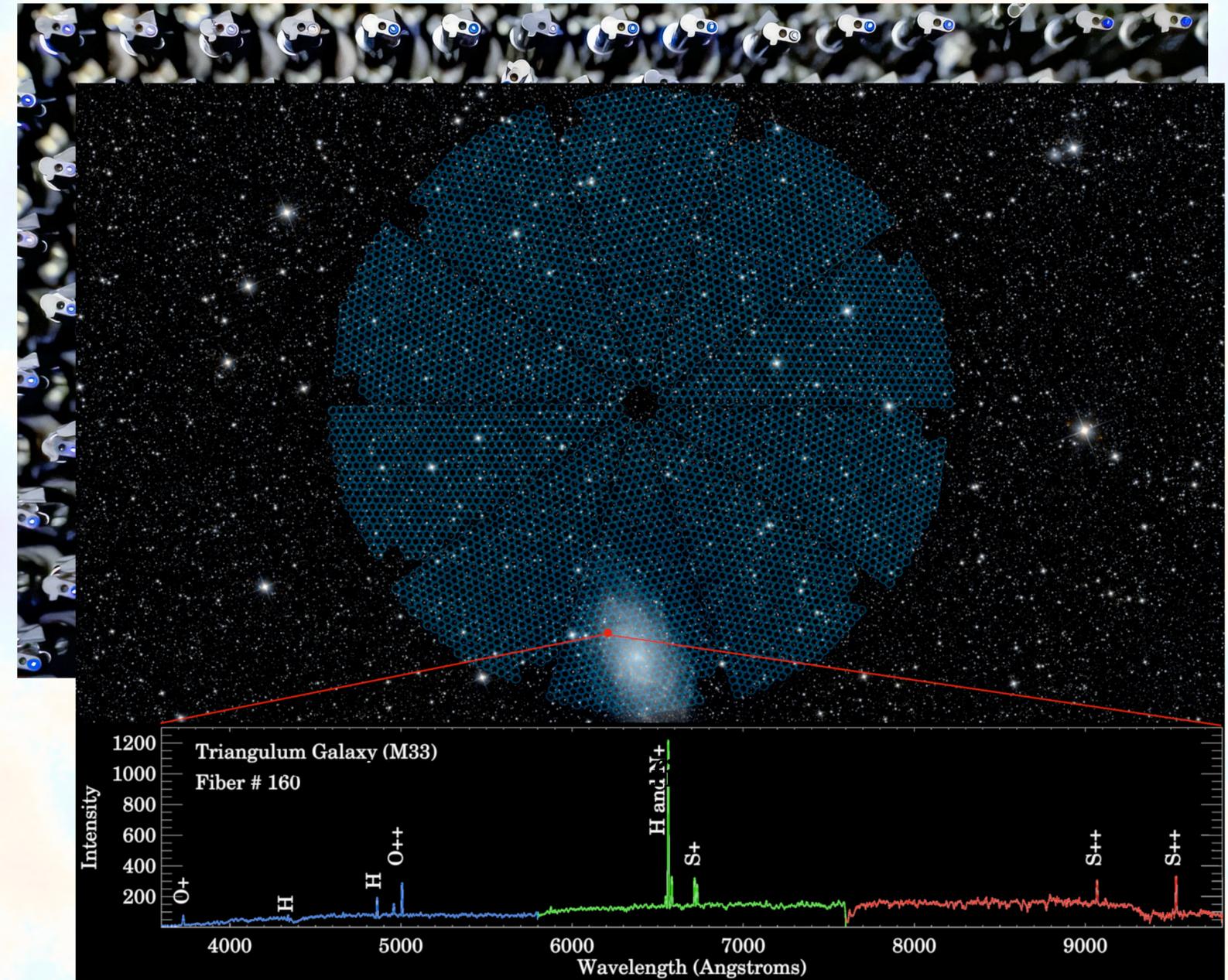


Dark Energy Spectroscopic Instrument

The era of Stage-IV surveys: DESI, Euclid, Rubin

Schematically, LSS probes

$$P_g(z, k, \mu) \sim \underbrace{P_\zeta(k)}_{\text{Inflation}} \underbrace{T^2(k)}_{\text{Cosmology}} \underbrace{\delta^2(z)}_{\text{Gravity/Expansion}} \underbrace{b^2(z, k)}_{\text{PNG}} \underbrace{(1 + \beta(z)\mu^2)^2}_{\text{Redshift-space}}$$



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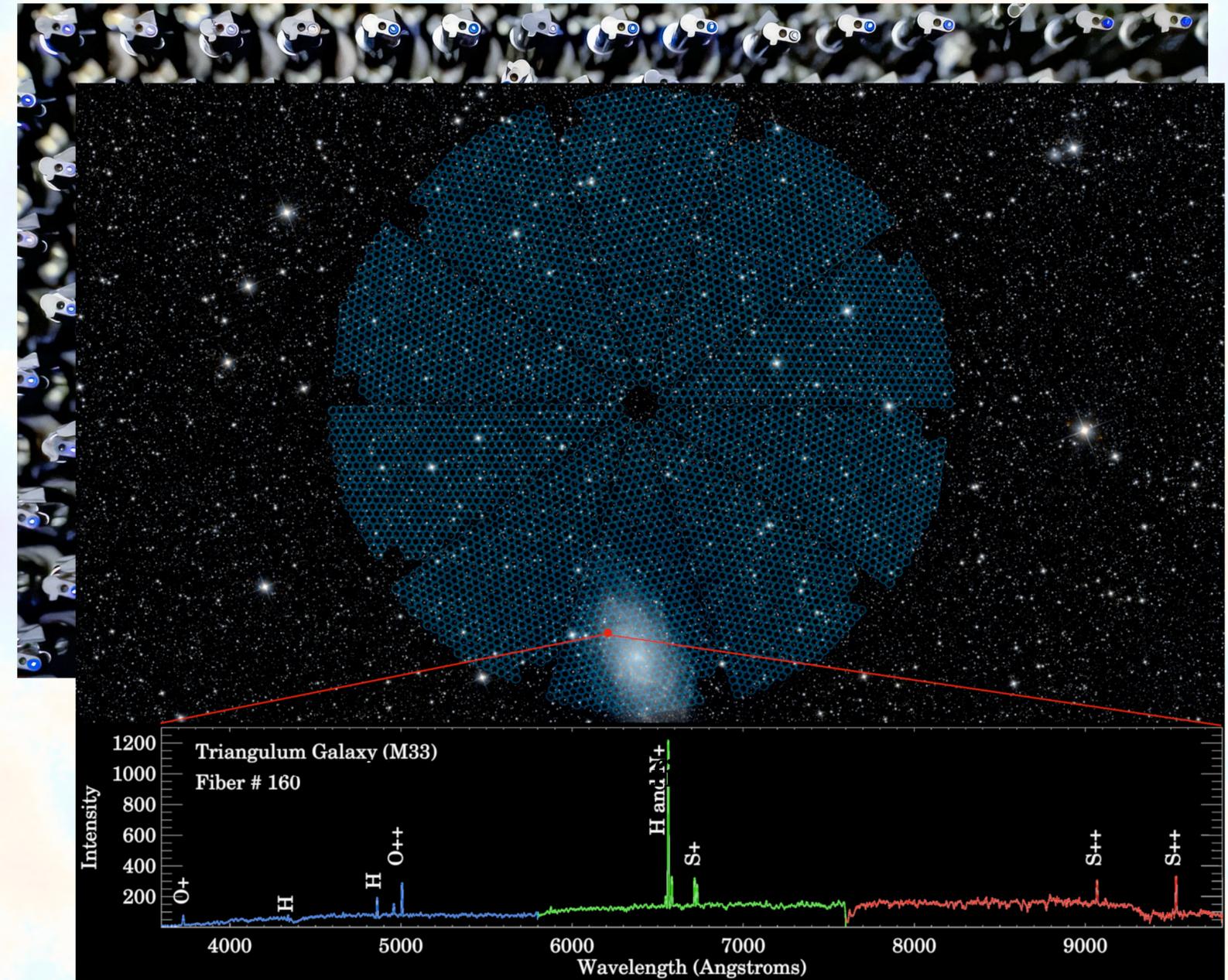
Exquisite measurements of Growth & Expansion Histories!

Modified Expansion

$$\frac{H^2(z)}{H_0^2} = \Omega_m a^{-3} + (1 - \Omega_m)$$

Modified Growth

$$f' + \left(f + 2 + \frac{h'}{h} \right) f = \frac{3}{2} \Omega_m(z)$$



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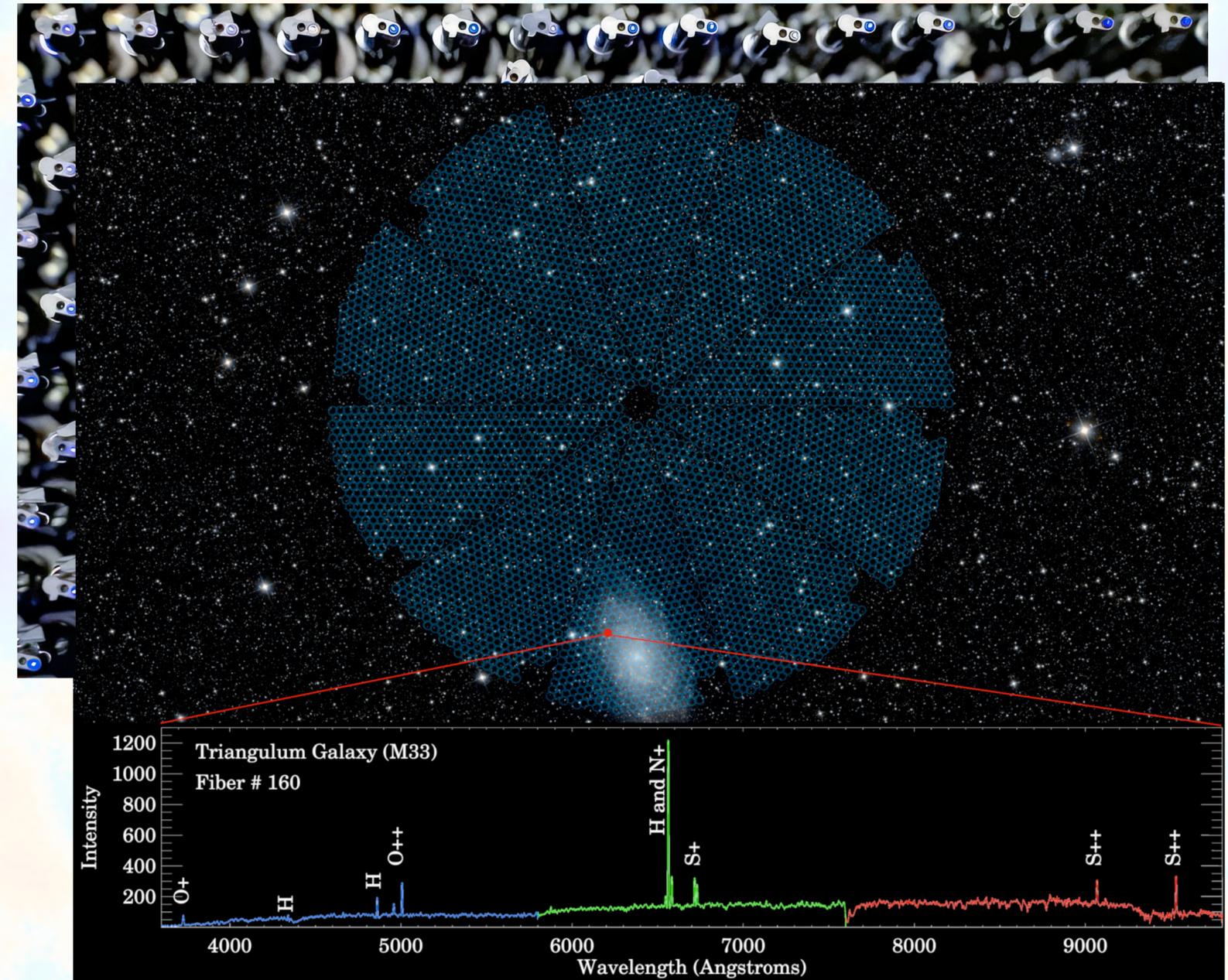
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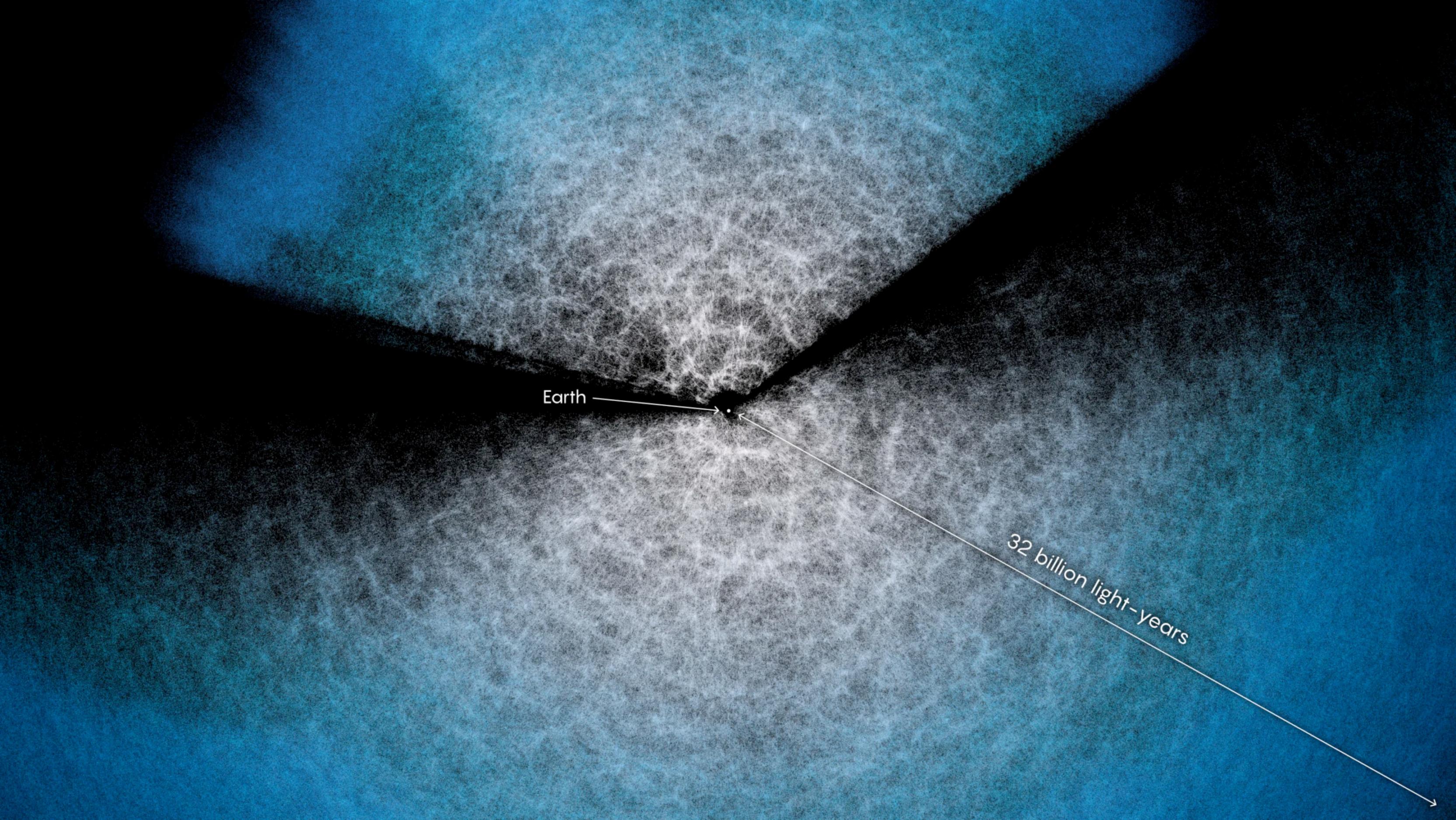
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Earth

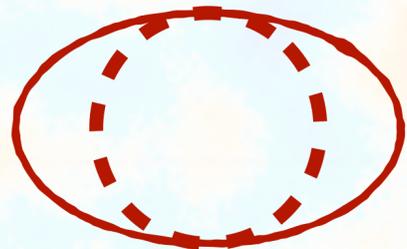
32 billion light-years

Clustering : 2pt statistics

Raw data in the form :
 (z, ϕ, θ)

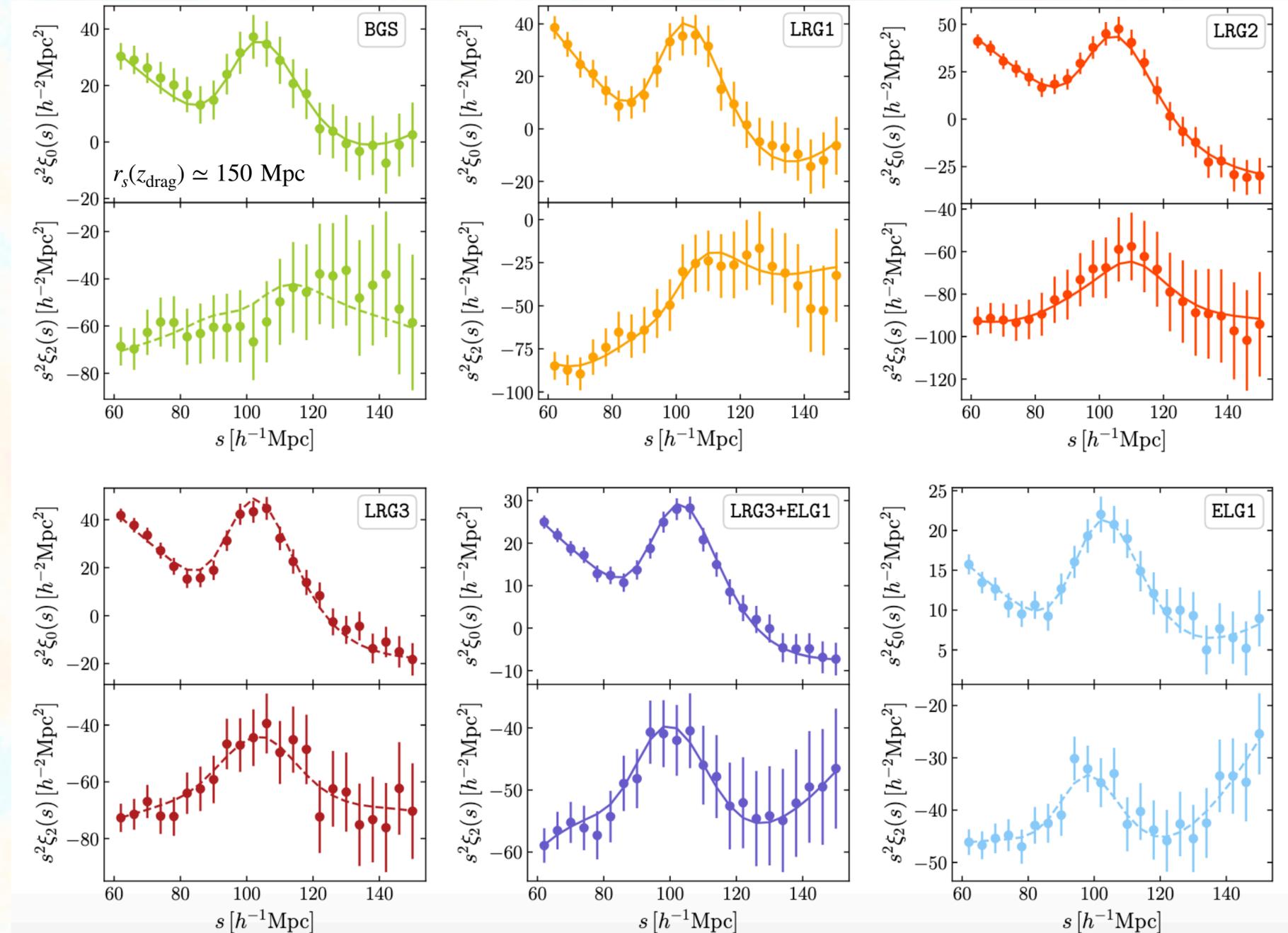
$$z \xrightarrow{\Theta_{\text{fid}} = \Theta_{\Lambda\text{CDM}}^{\text{Planck}}} r(z)$$

Geometrical ‘Alcock-Paczyński’ (AP) effect



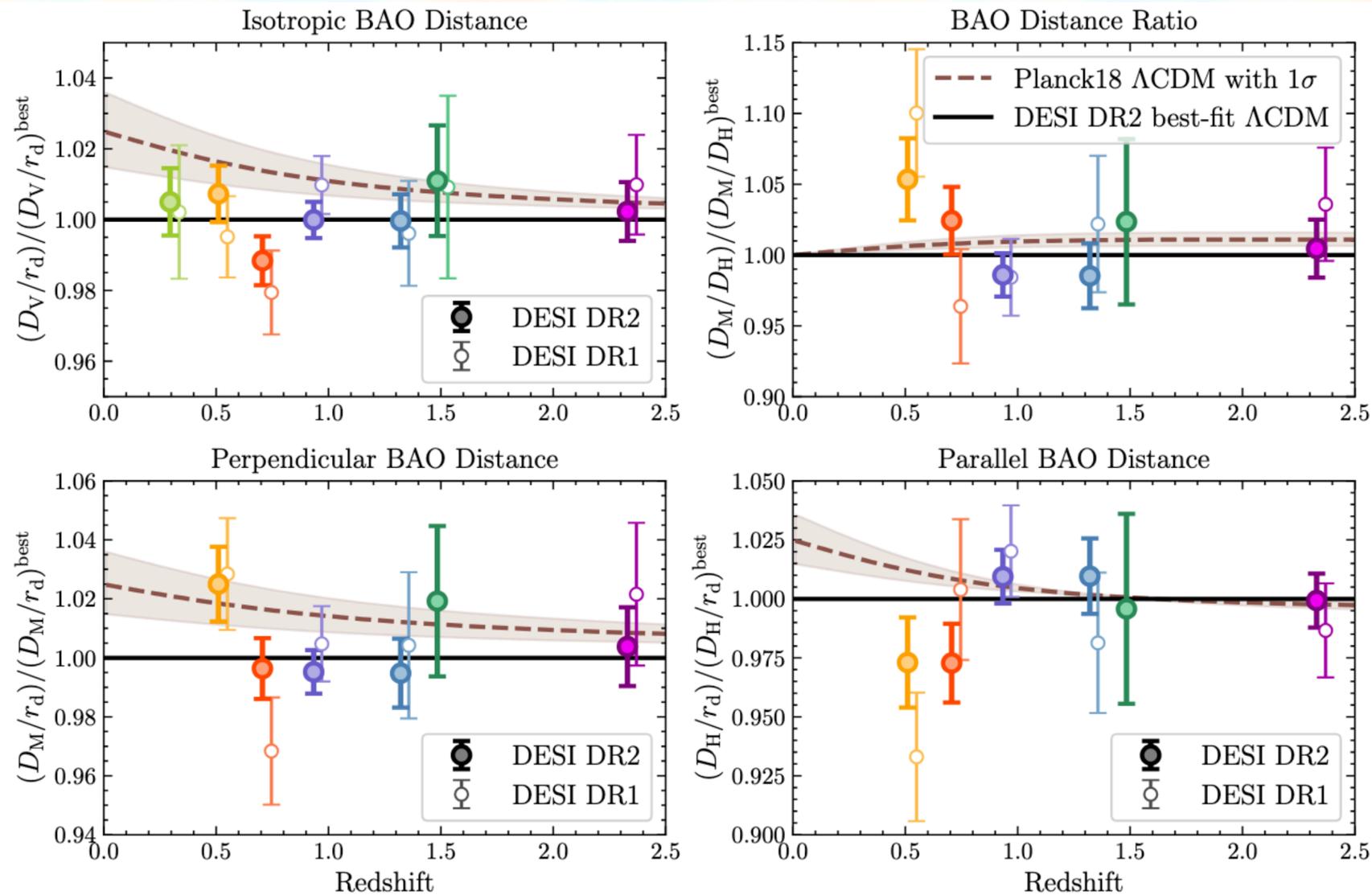
$$\frac{D_M}{r_d} = \alpha_{\perp} \frac{D_M^{\text{fid}}}{r_d^{\text{fid}}}$$

$$\frac{D_H}{r_d} = \alpha_{\parallel} \frac{D_H^{\text{fid}}}{r_d^{\text{fid}}}$$



DESI Collaboration, Abdul-Karim et al - arXiv: 2503.14738

Distance measurements



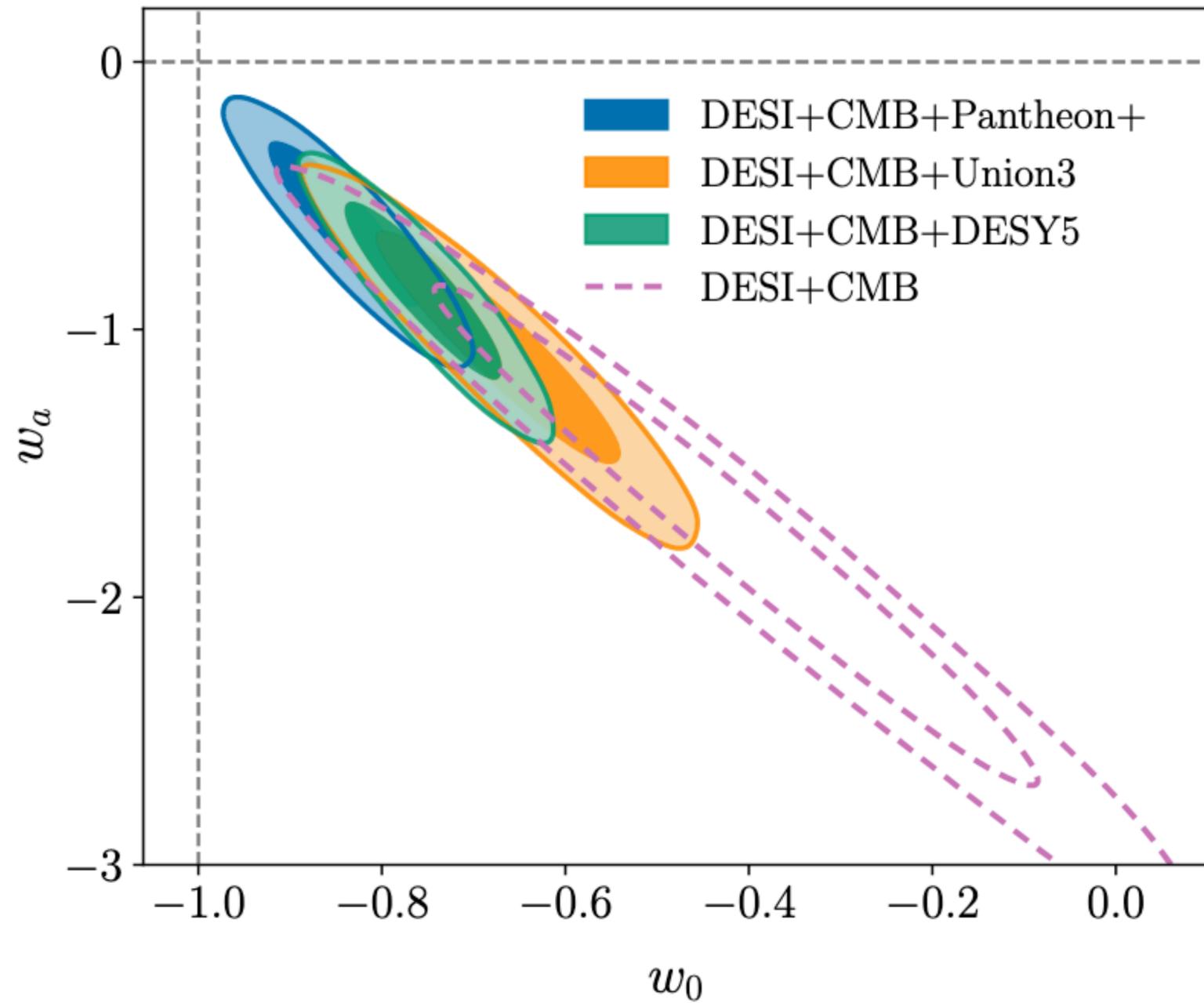
$$D_H(z) = H^{-1}(z; \Theta_{\text{cosmo}})$$

$$D_M(z) = \int_0^z \frac{dz'}{H(z'; \Theta_{\text{cosmo}})}$$

DESI Collaboration, Abdul-Karim et al - arXiv: [2503.14738](https://arxiv.org/abs/2503.14738)

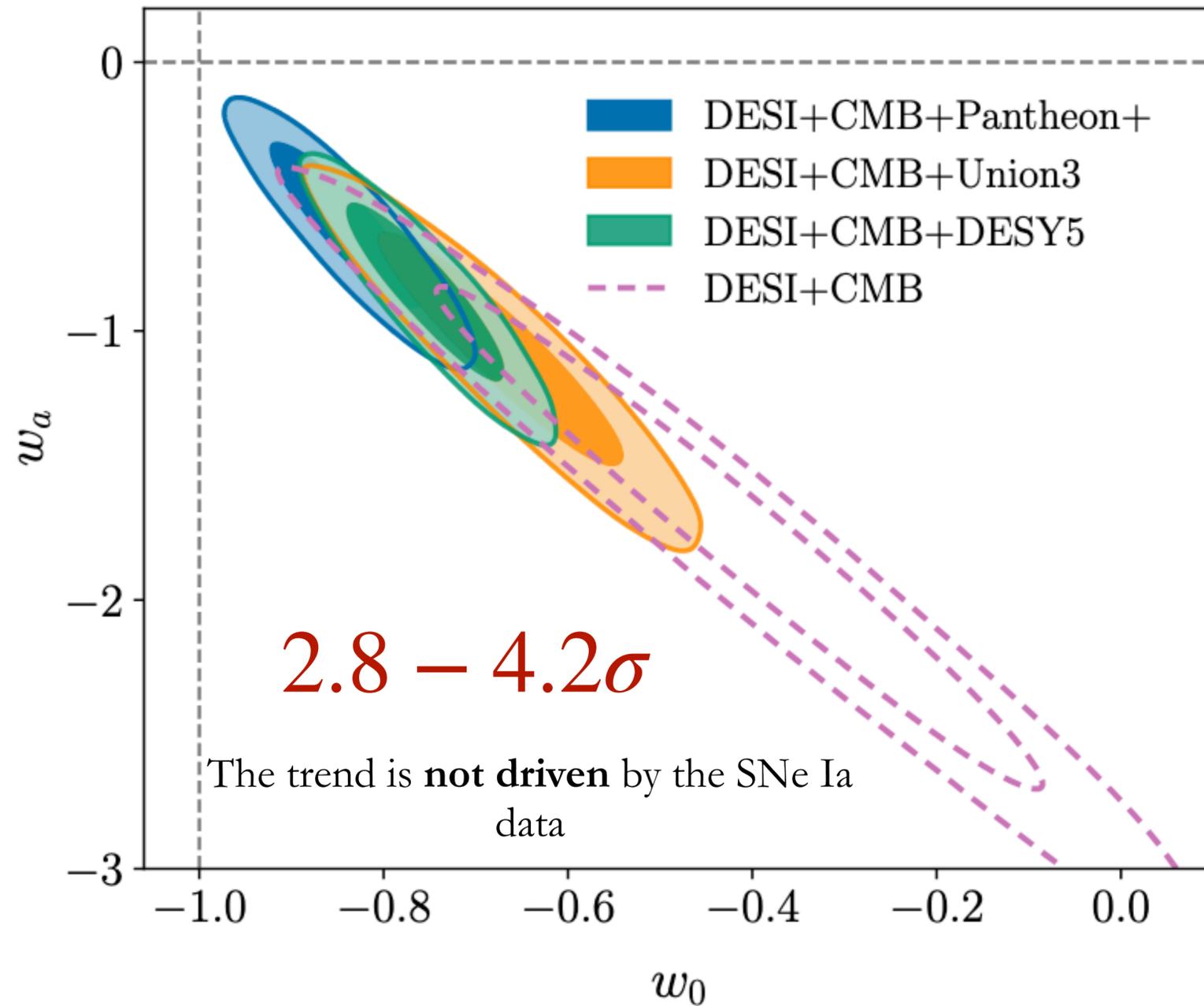
The w_0 - w_a plane

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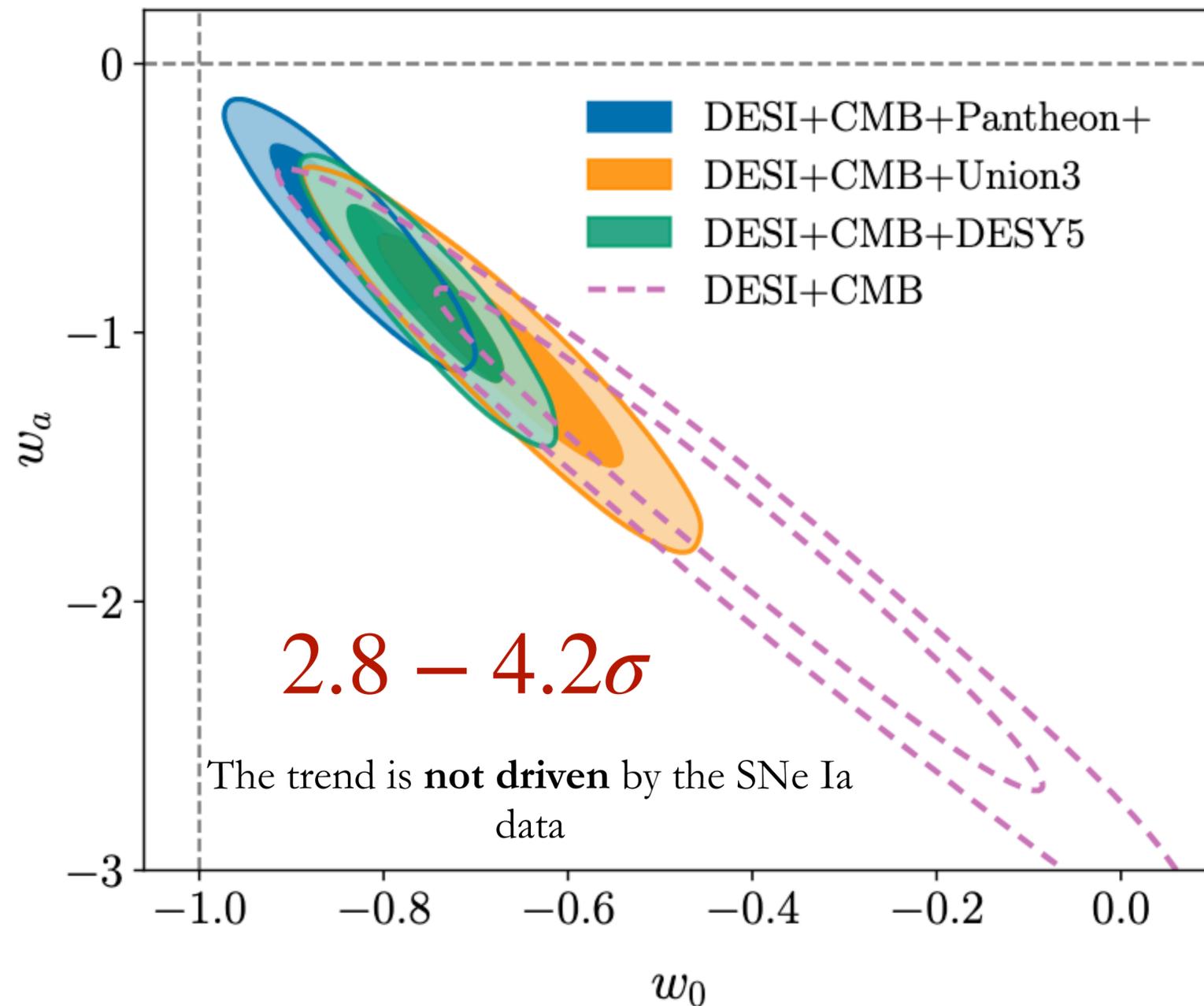
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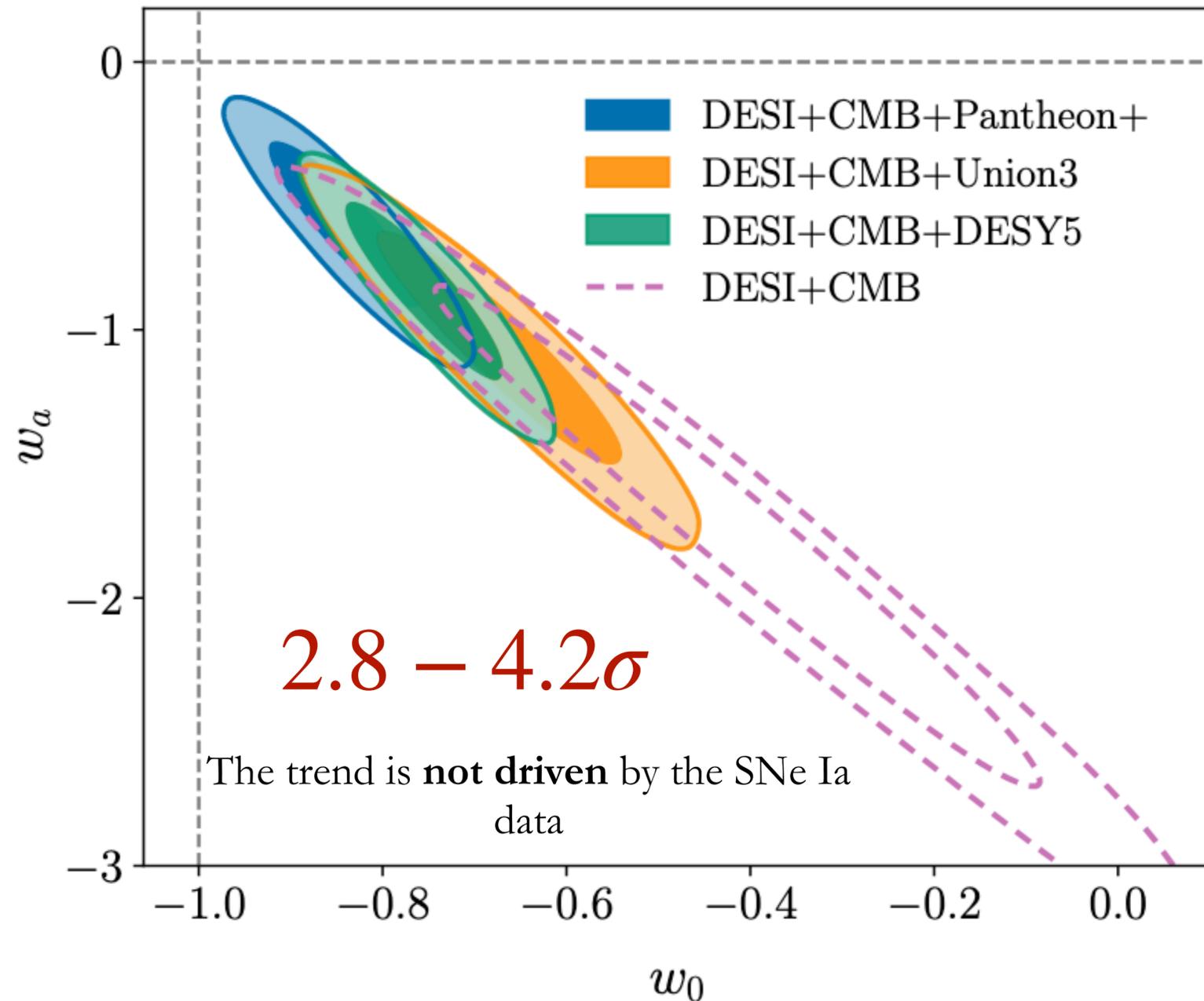
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- $w(a) = w_0 + w_a(1 - a)$
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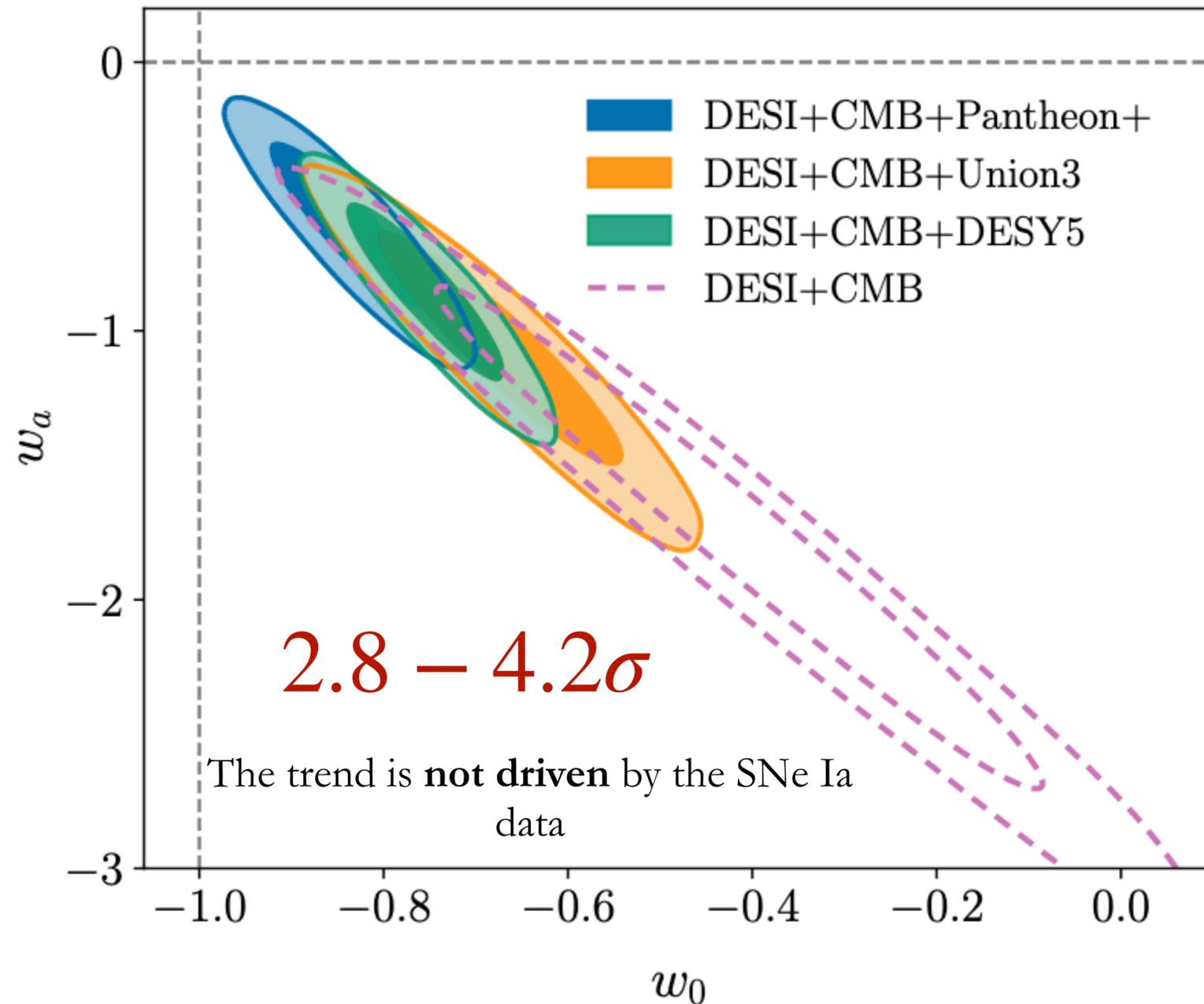
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- Extremely efficient in approximating the observables, i.e. $D_A(z)$ & $H(z)$
NOT $w(z)$ itself!

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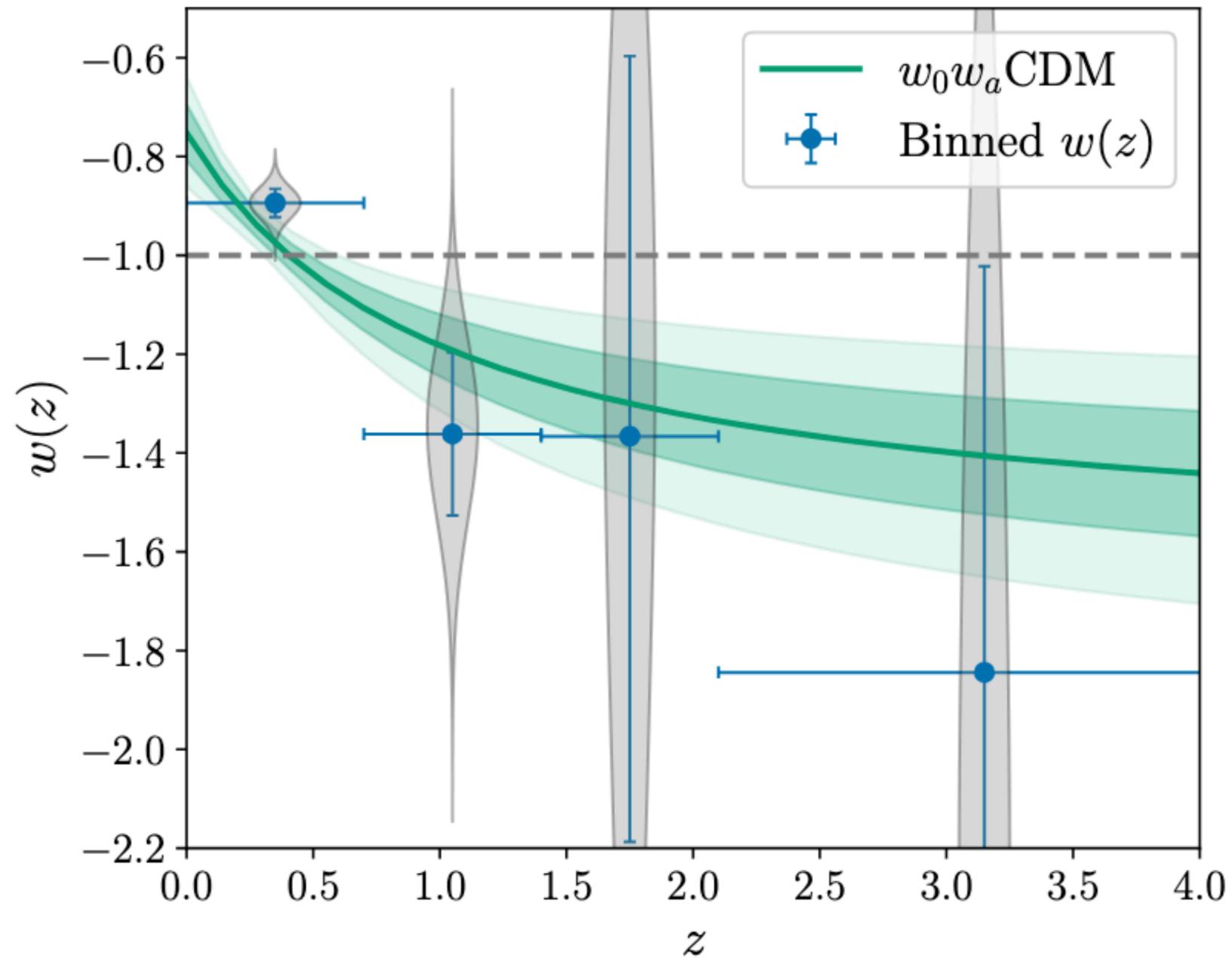


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→ spurious “phantom-crossing”
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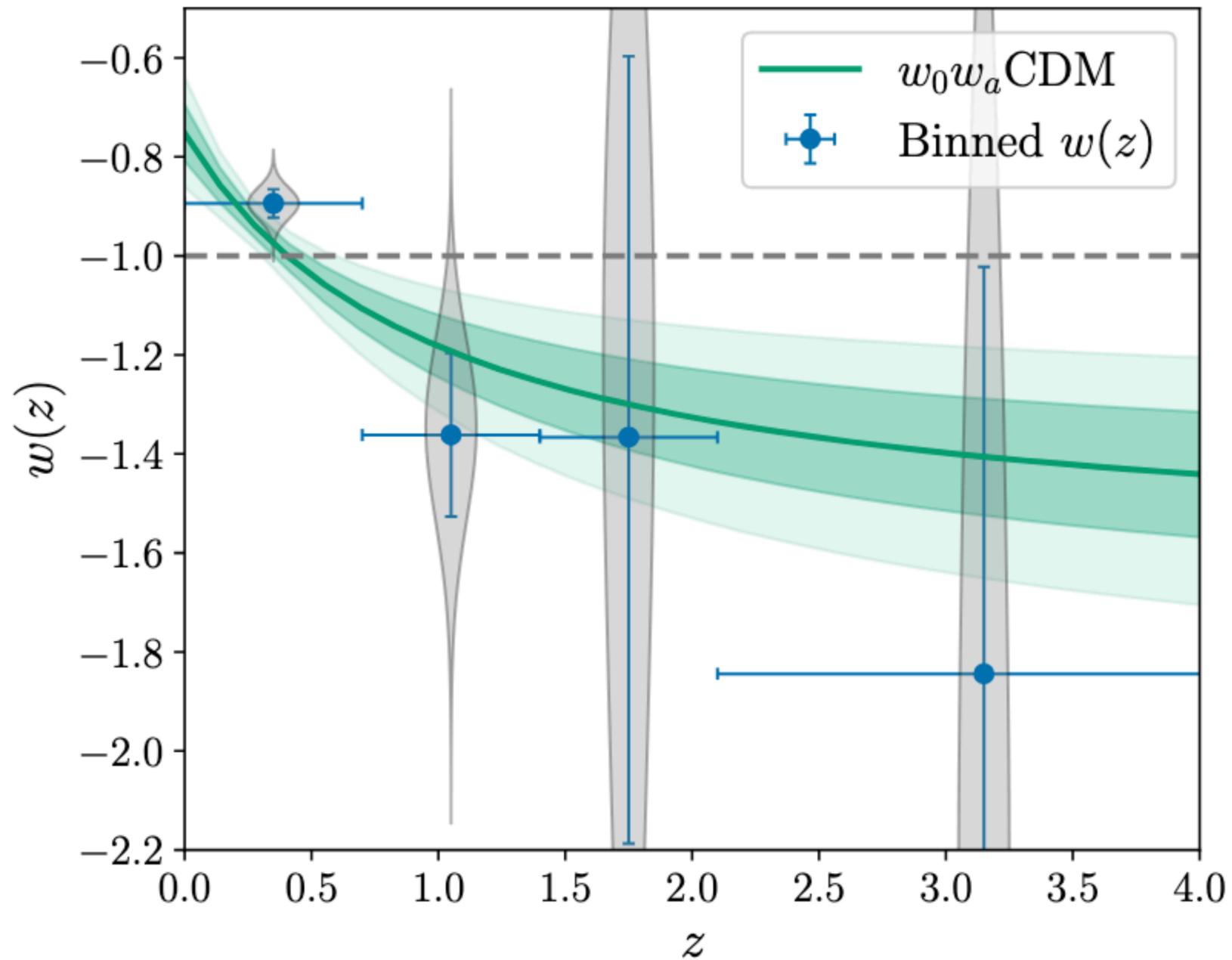


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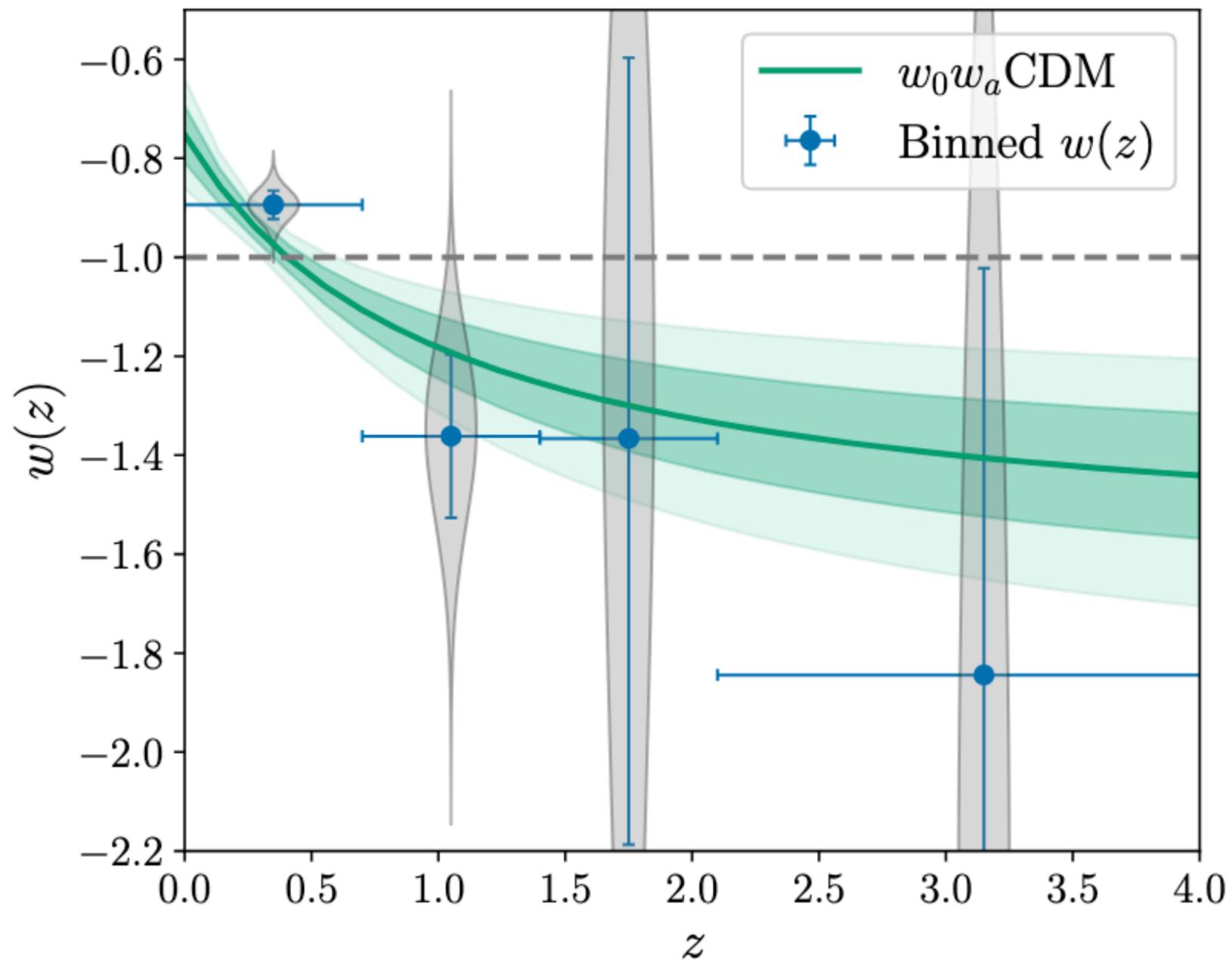
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Minimally-coupled scalar field ϕ

$$w_\phi(z) = \frac{P_\phi}{\rho_\phi} = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)} \rightarrow \boxed{-1 \leq w_\phi(z) \leq 1}$$

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How robust are these results?

Beyond a linearly evolving $w(a)$

$$3M_{\text{Pl}}^2 H^2(z) = \rho_m(z) + \rho_{\text{DE}}(z) + \dots$$

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Chebyshev Polynomial
Expansion

$$w(z) \equiv P/\rho = \sum_{i=0}^N C_i T_i(x)$$

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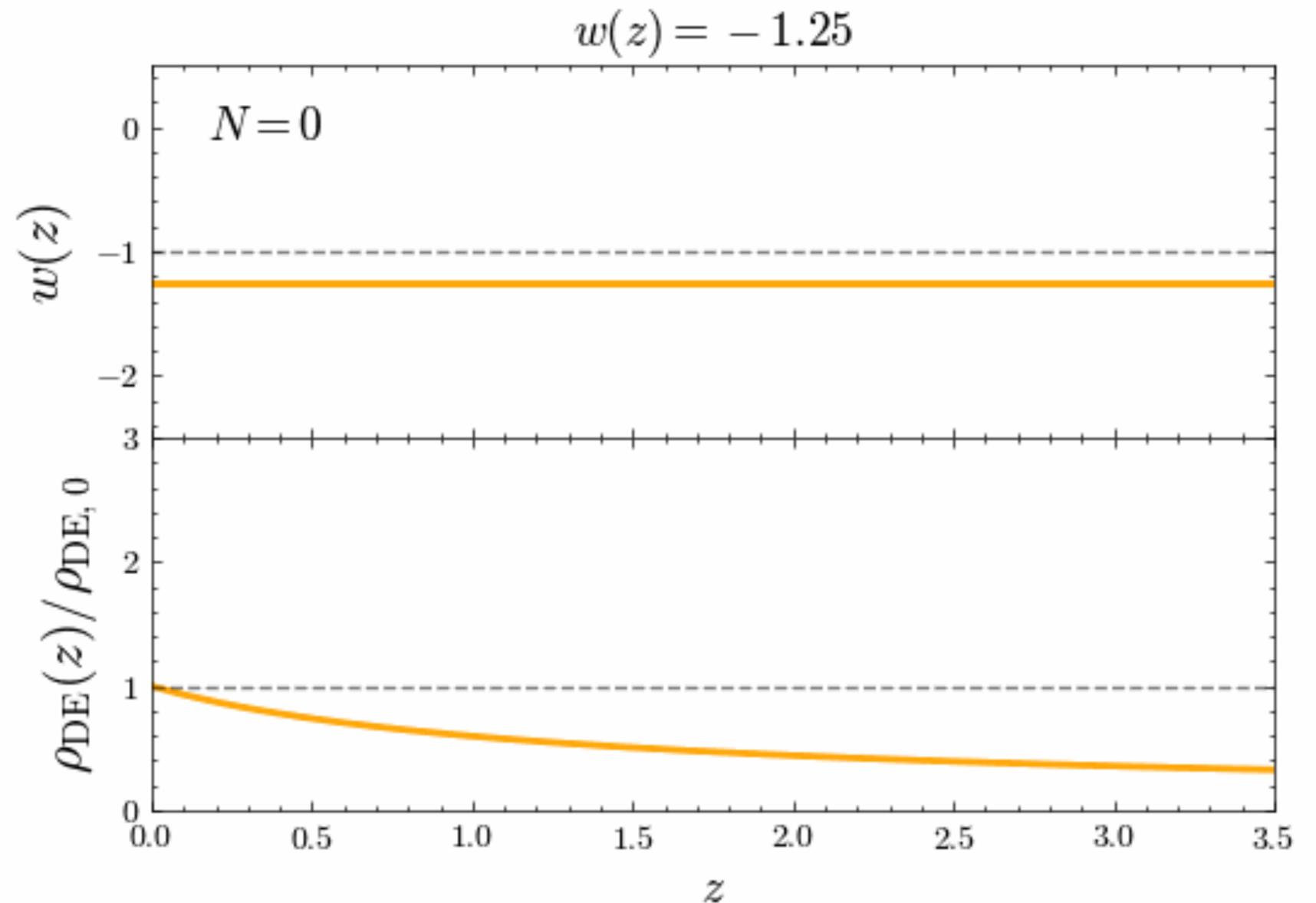
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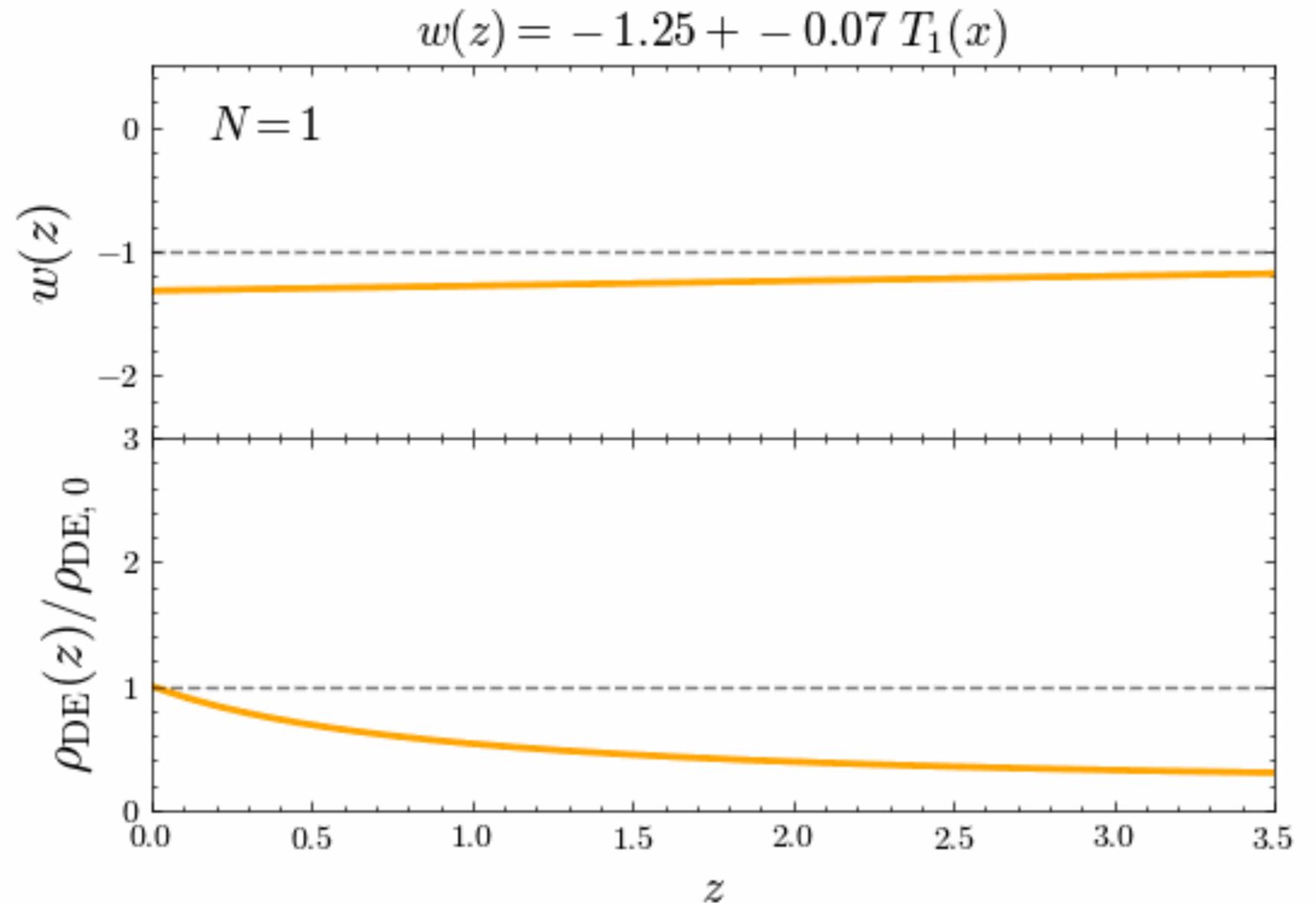
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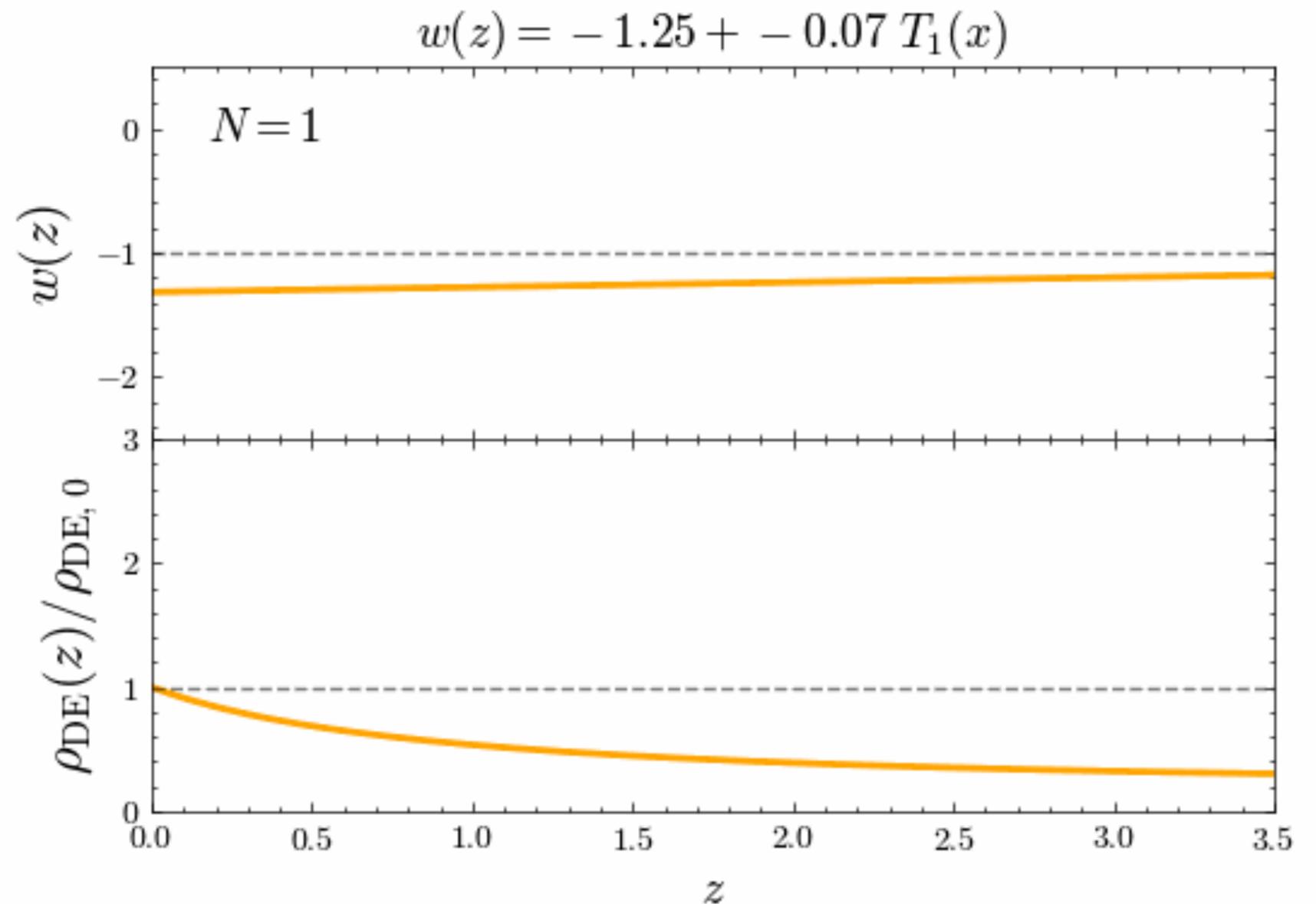
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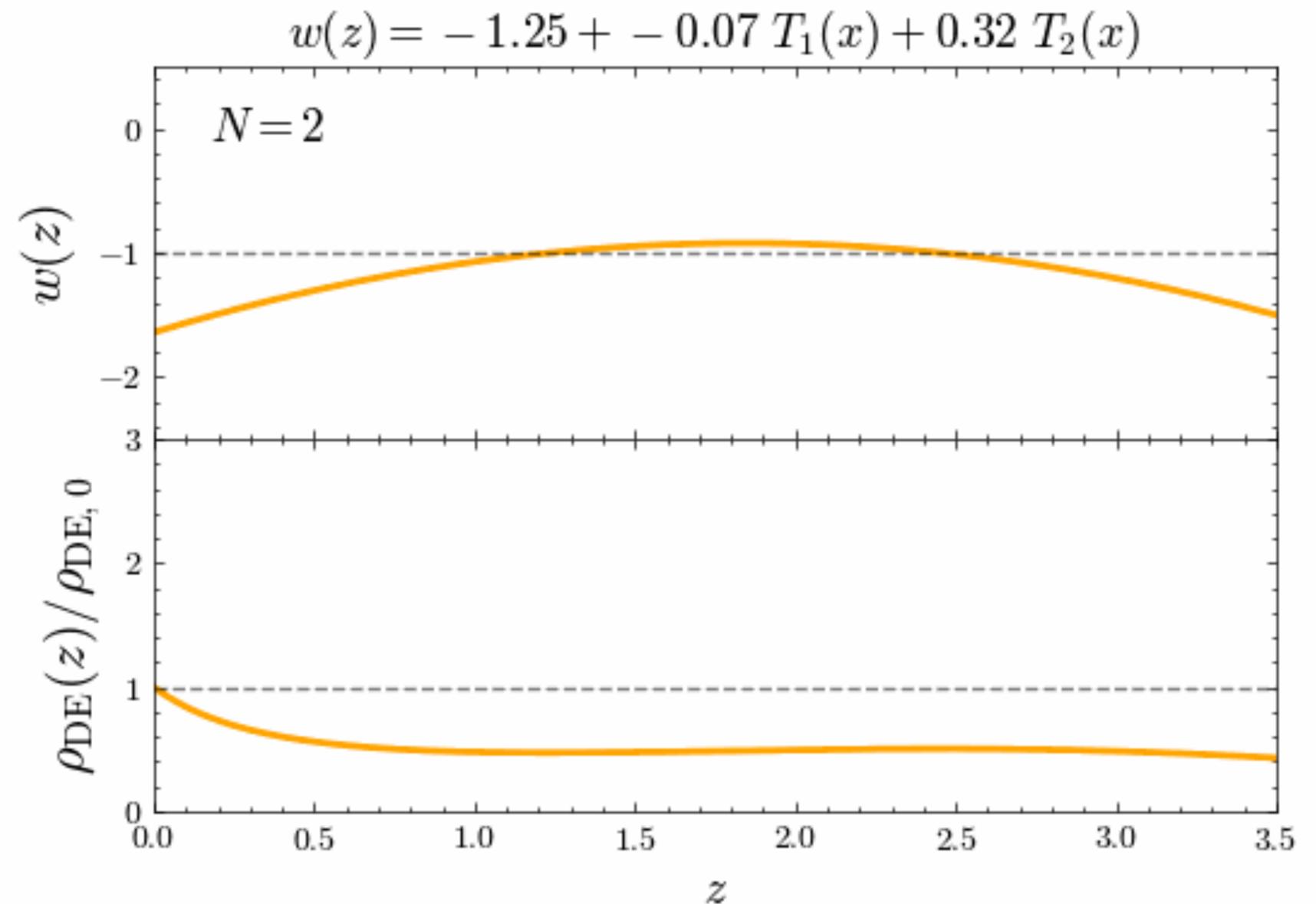
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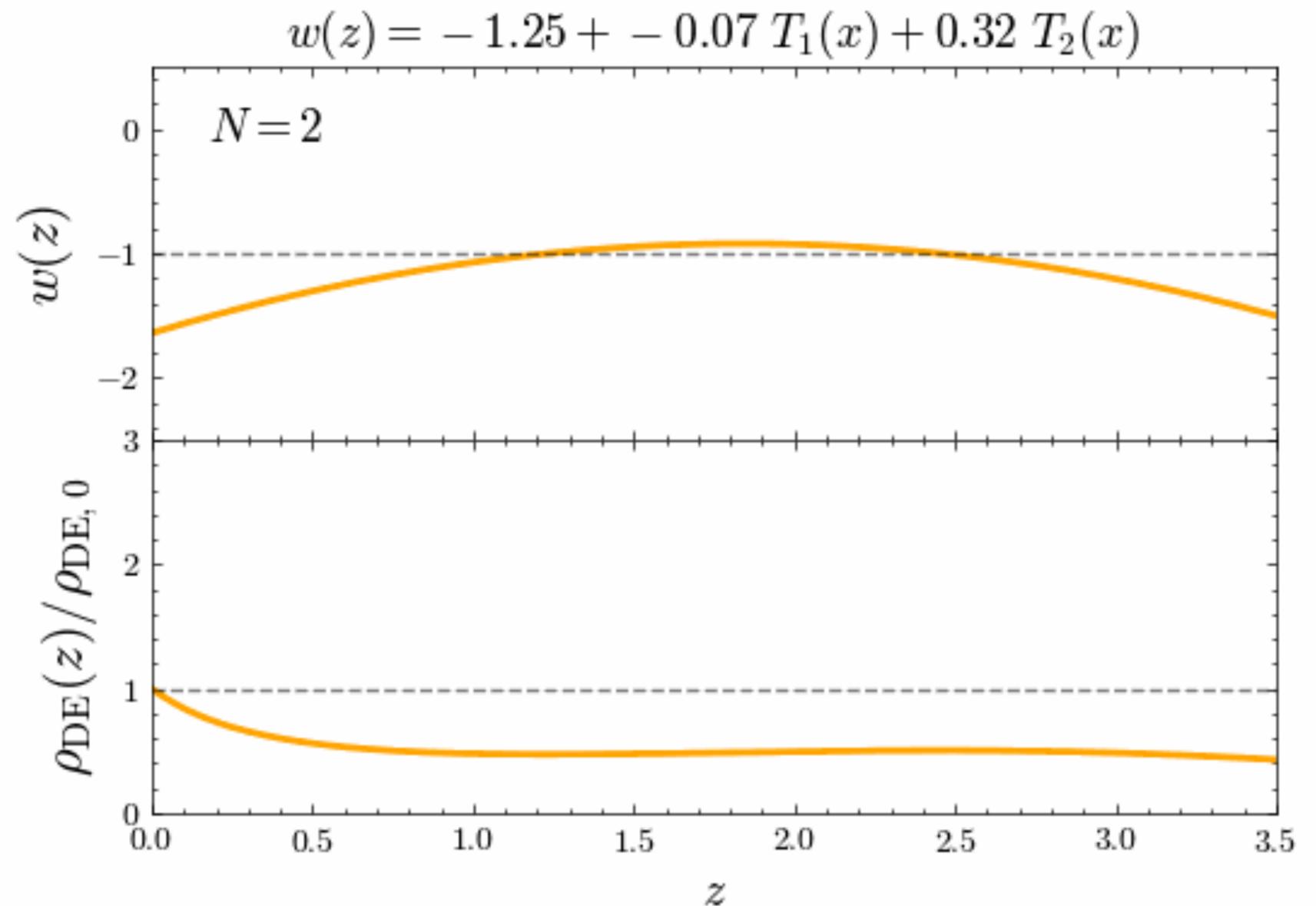
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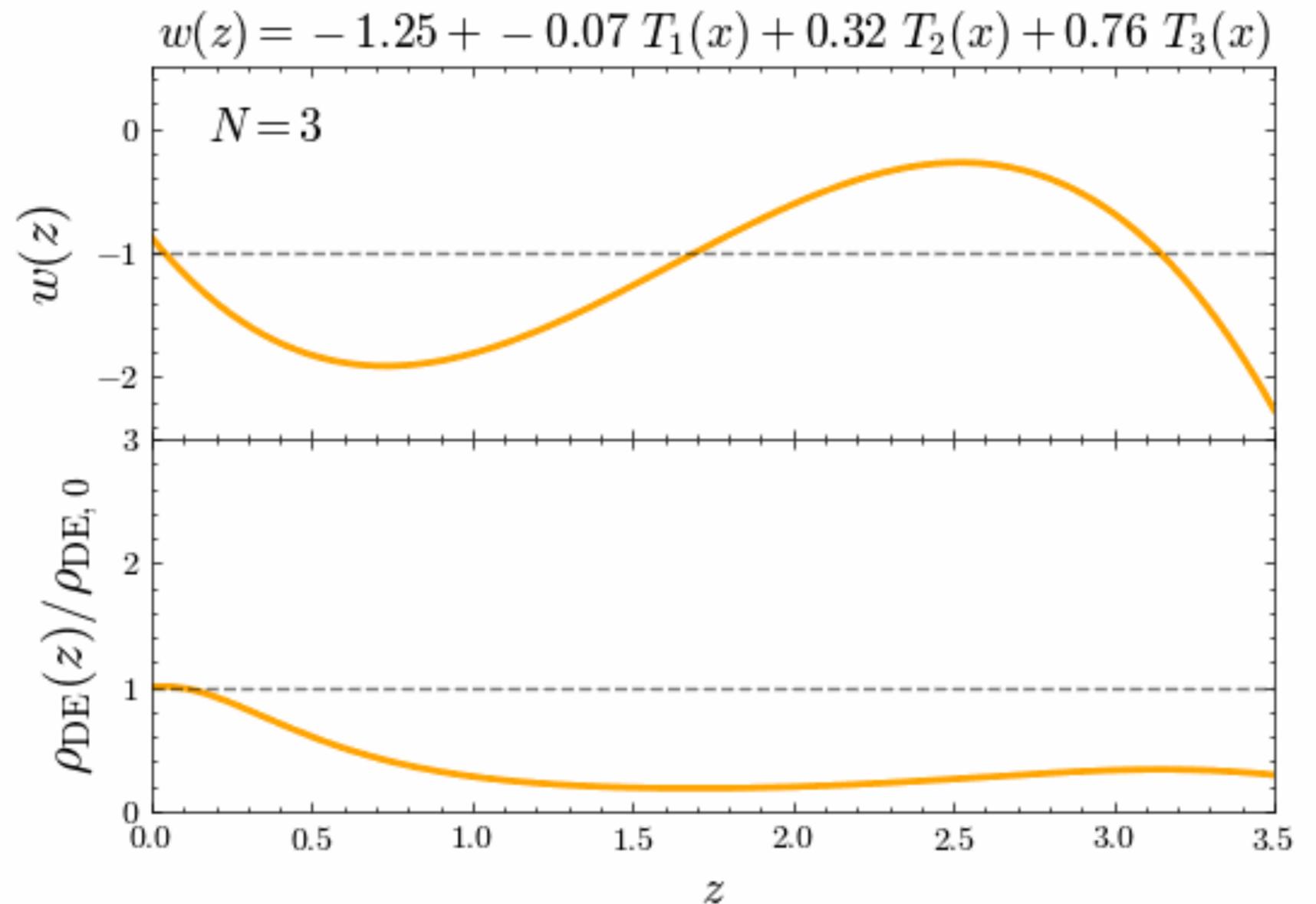
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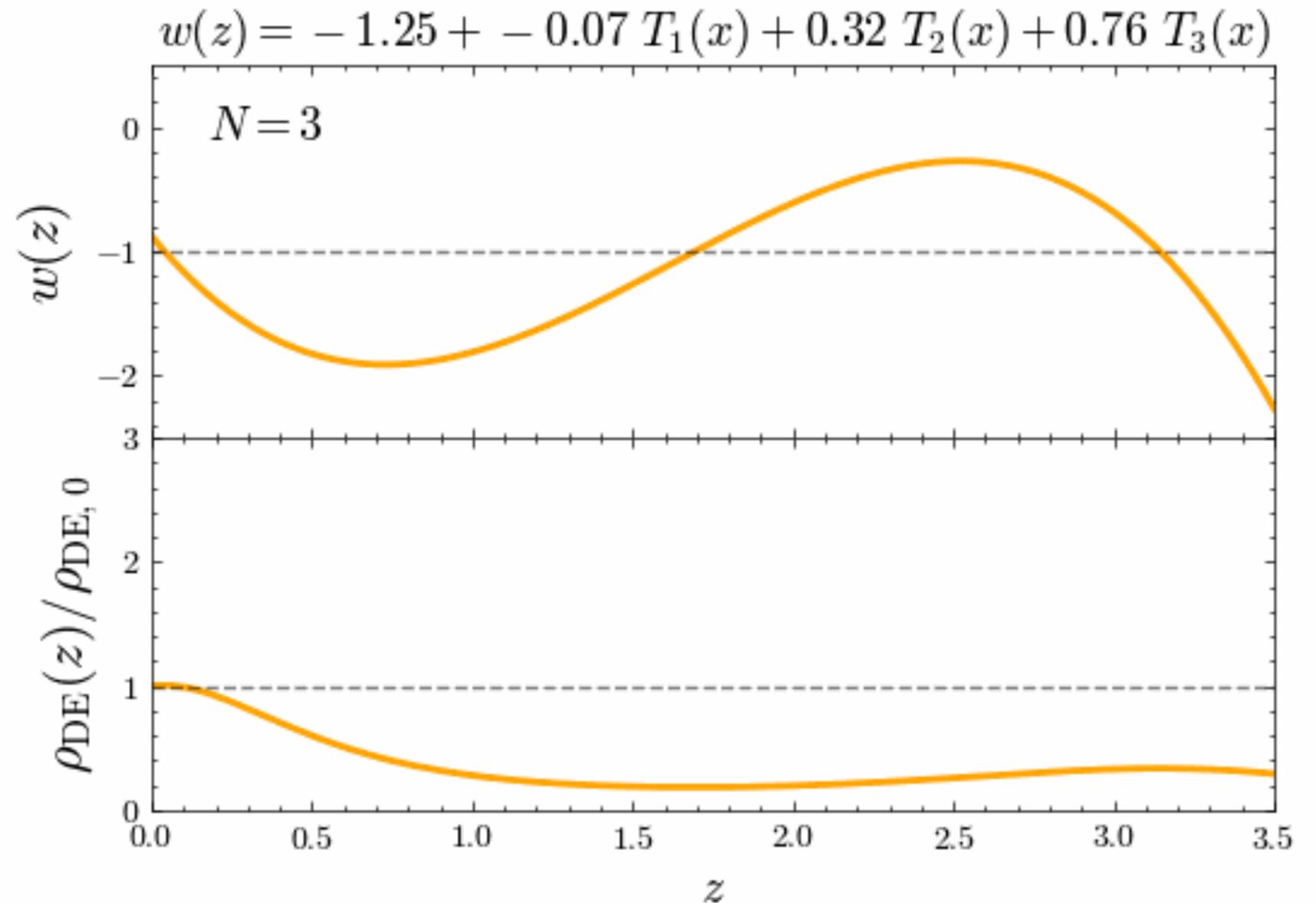
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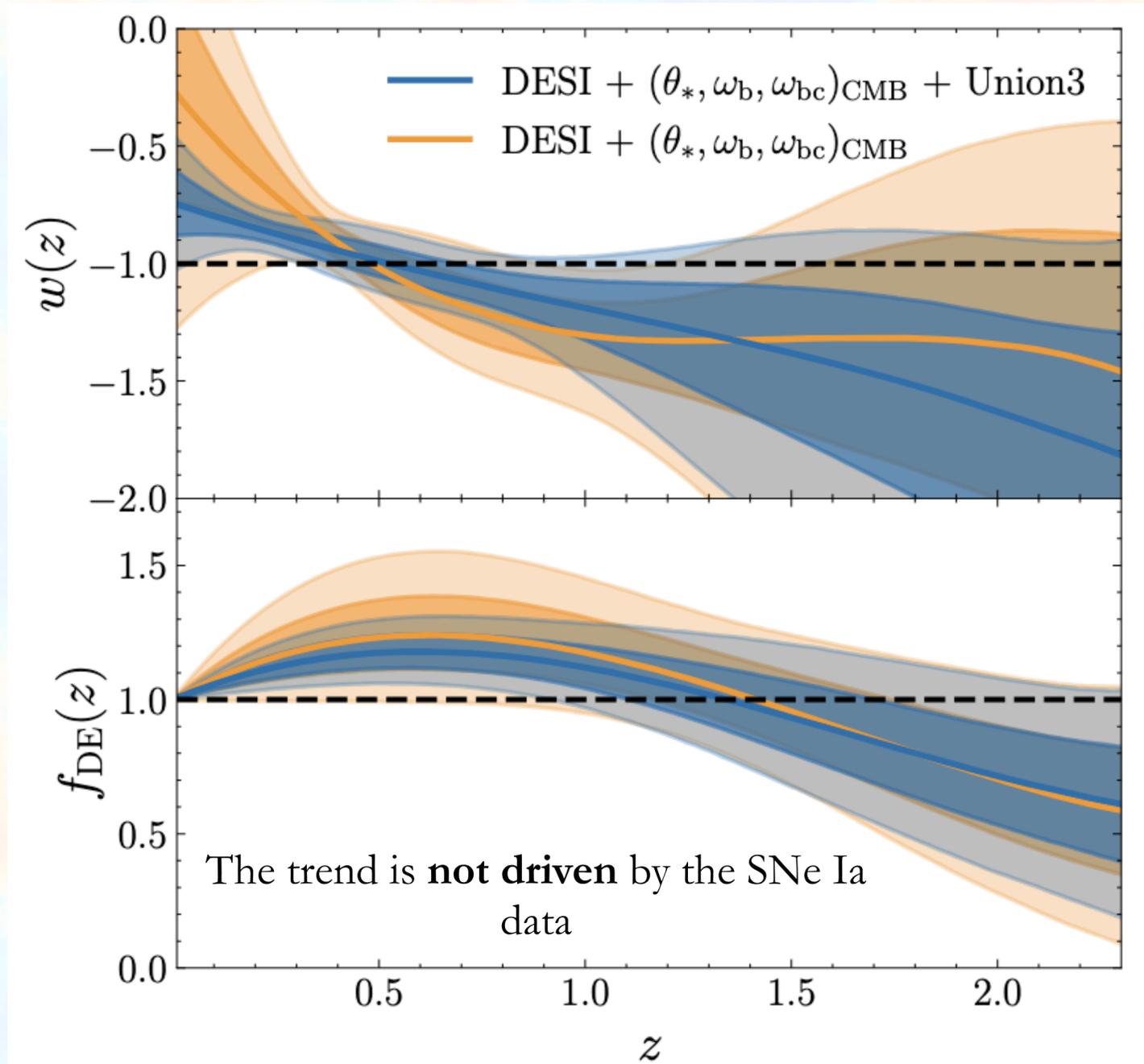
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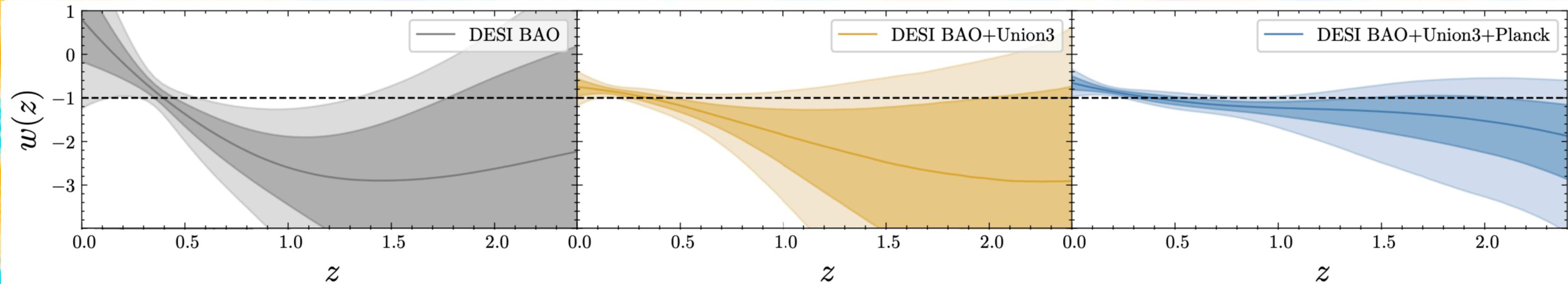
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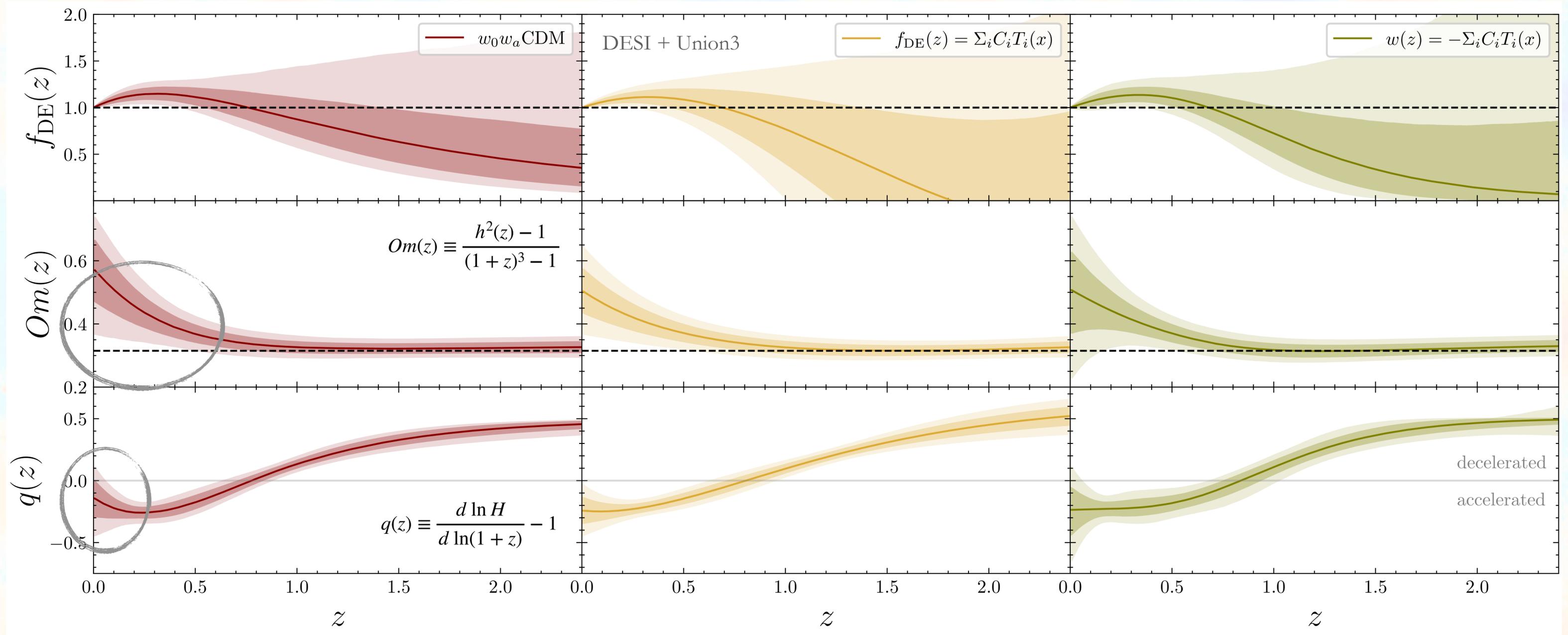
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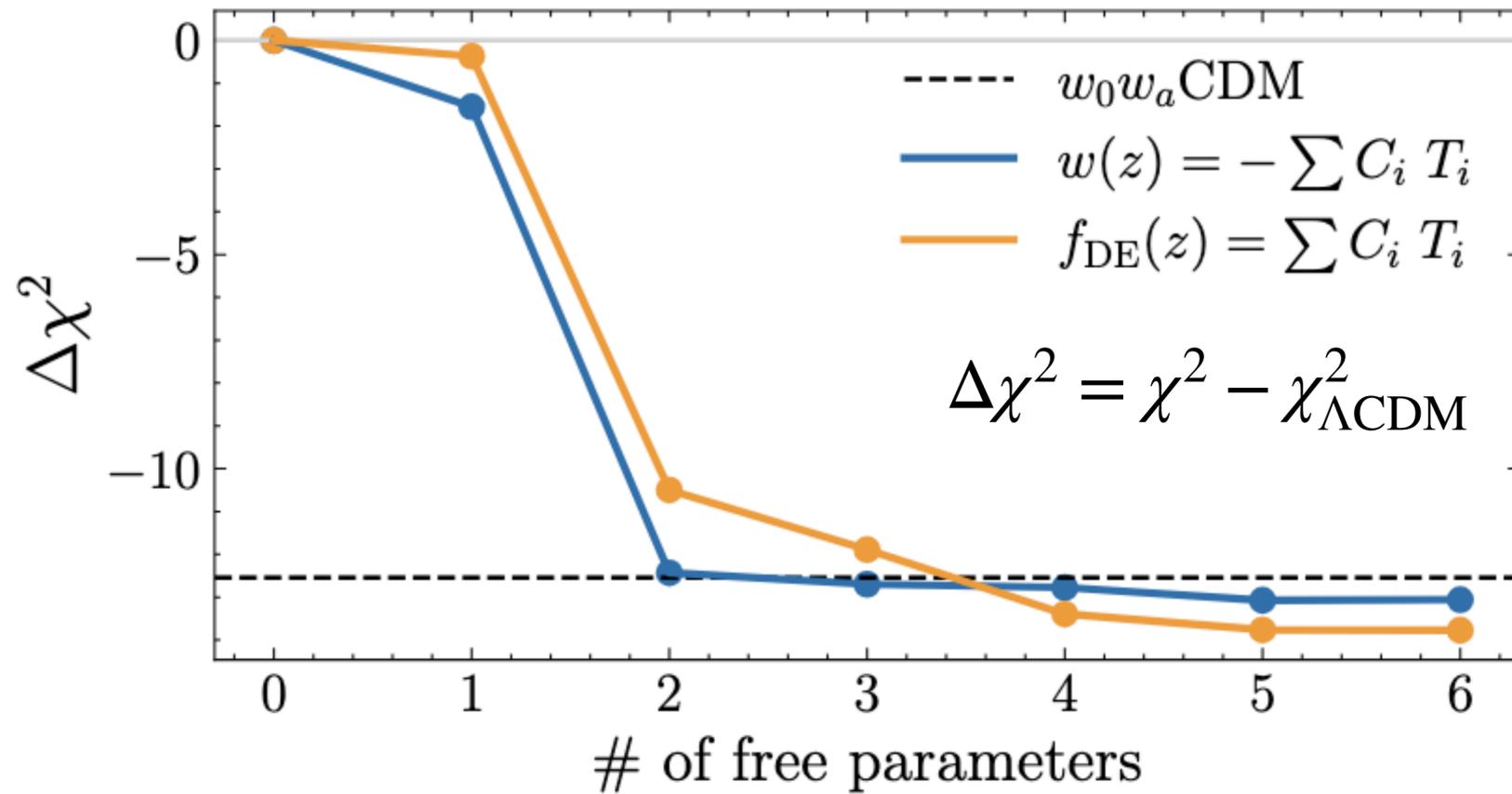
Robustness of the results



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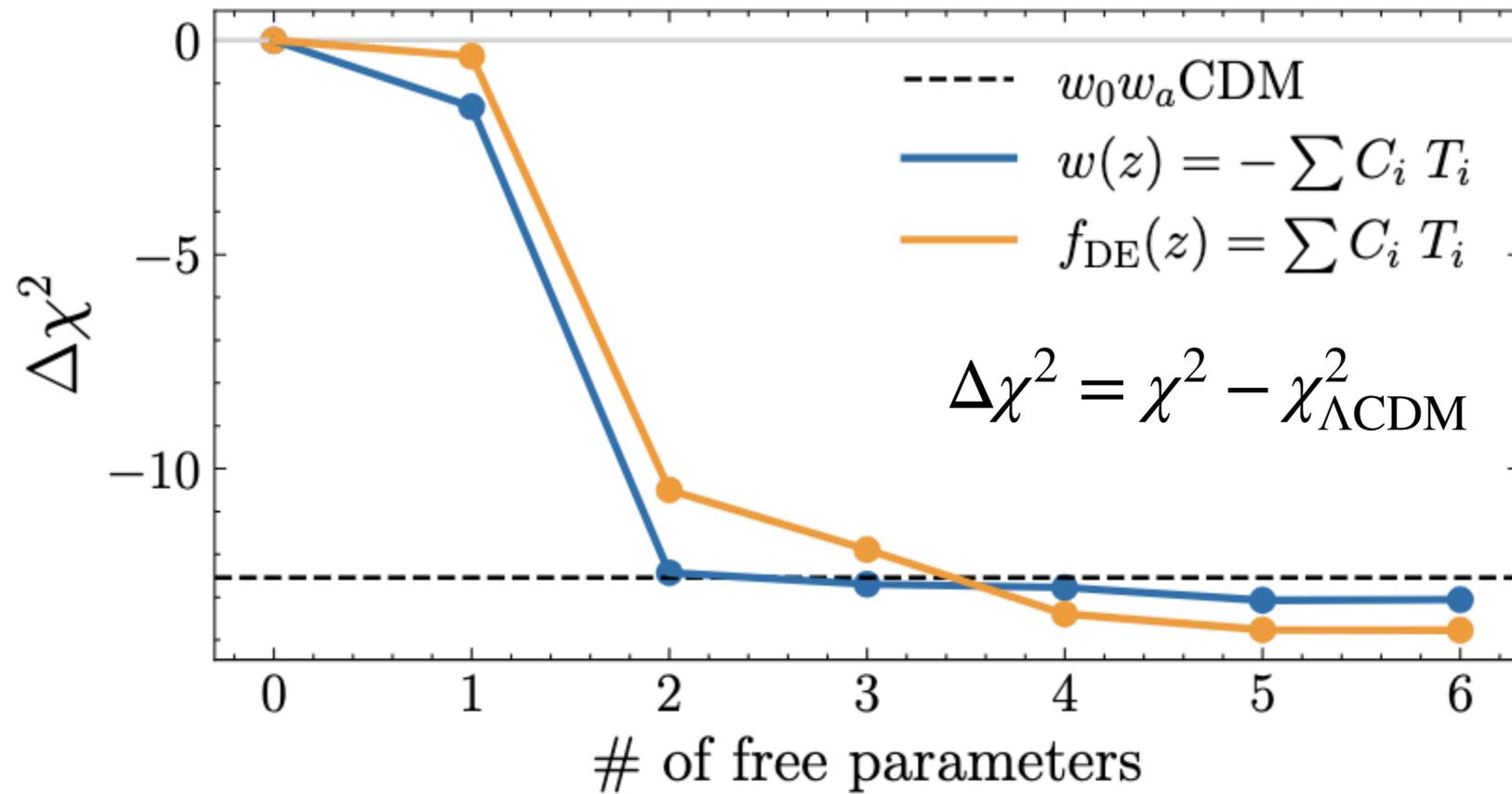


χ^2 'saturates' at ~ 2 free parameters

Additional degrees of freedom are **NOT**
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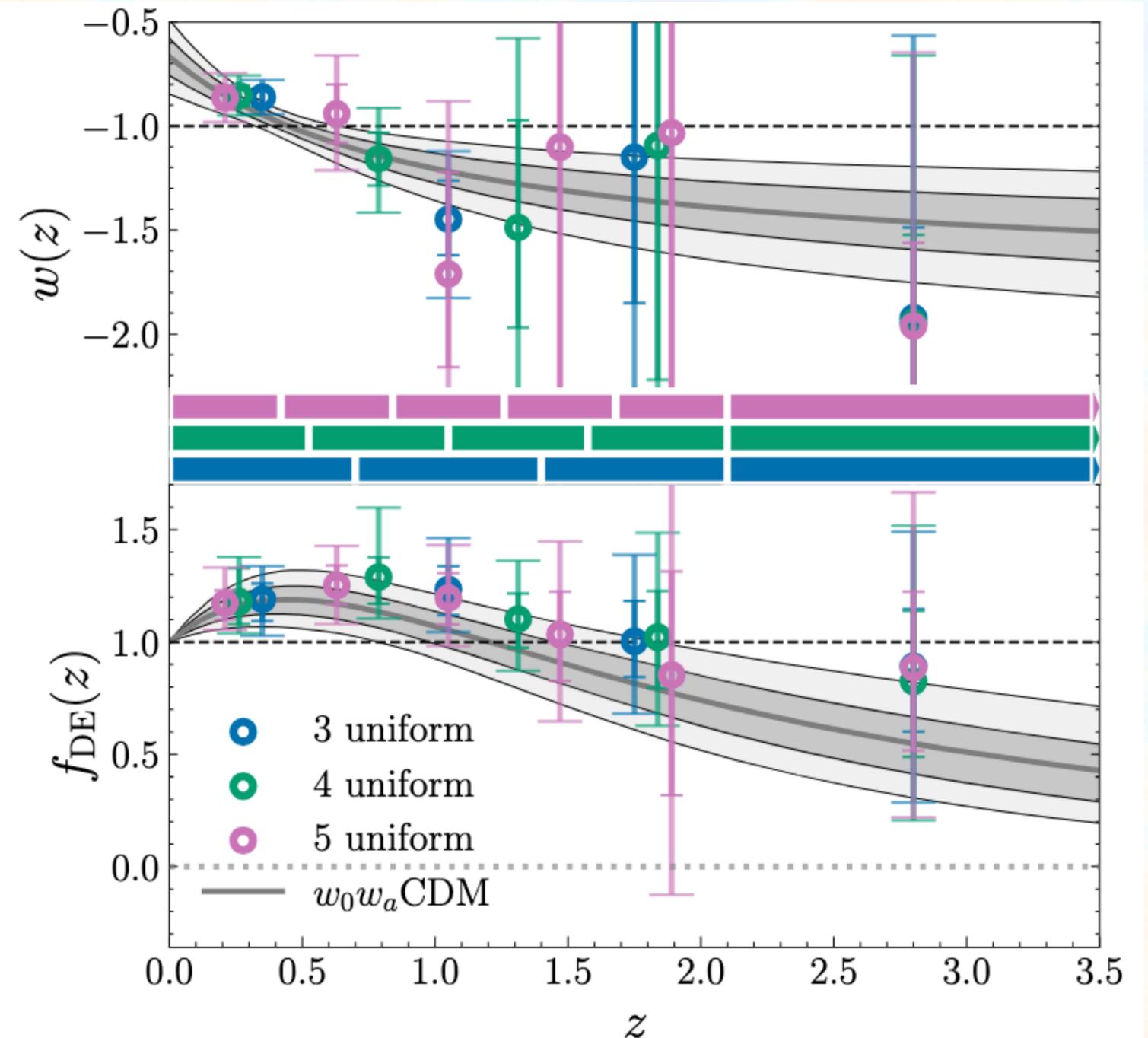
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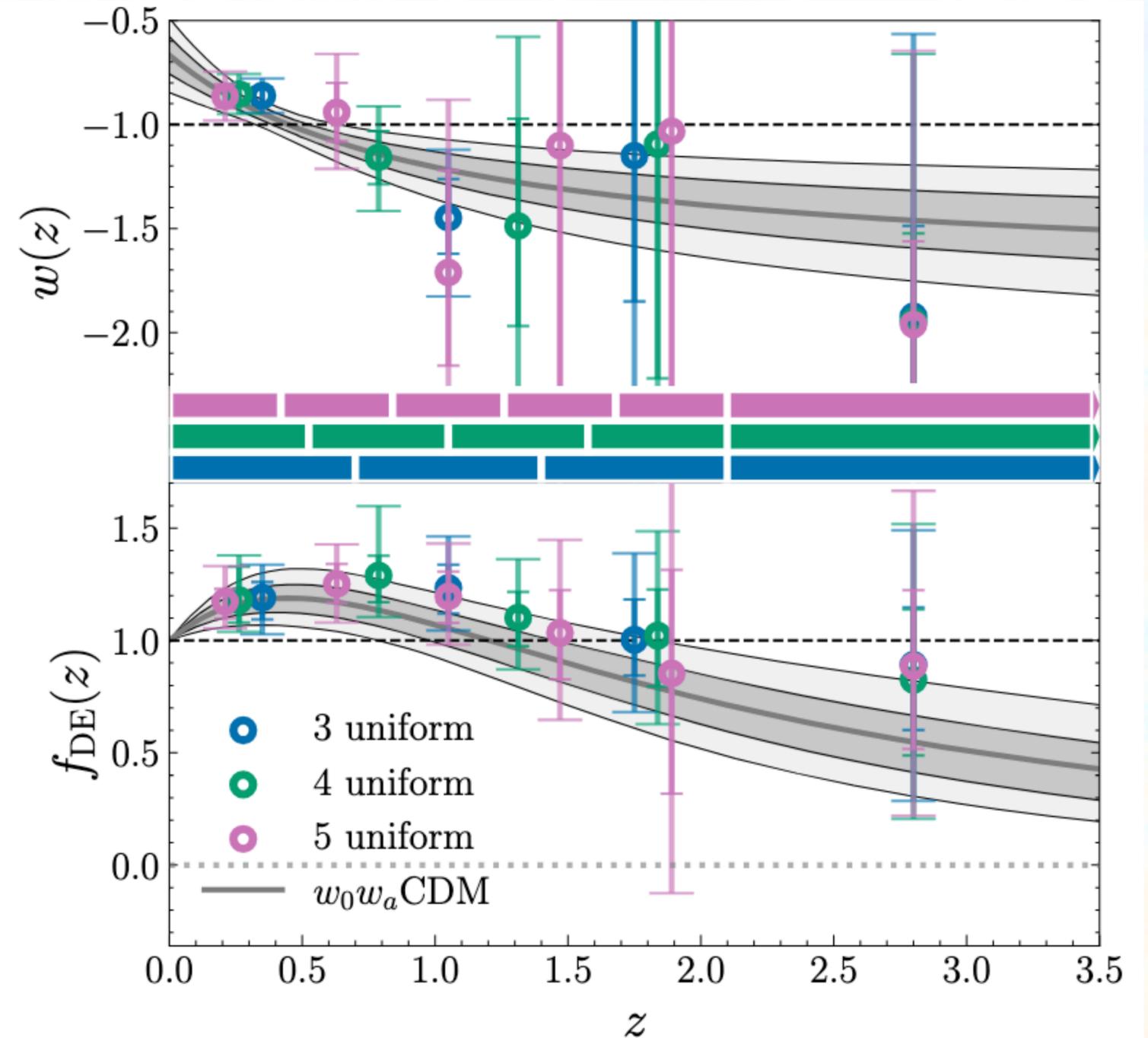
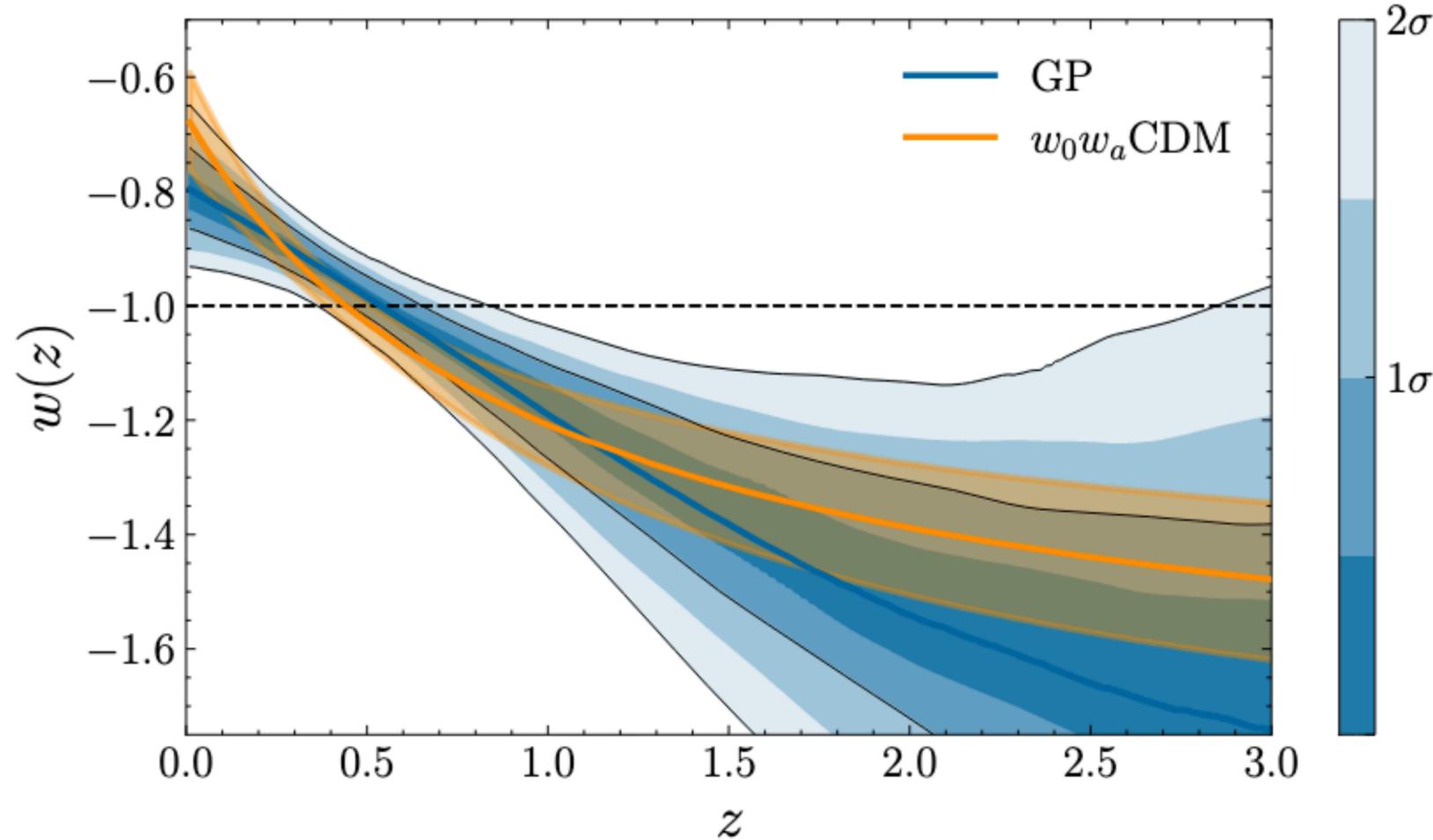


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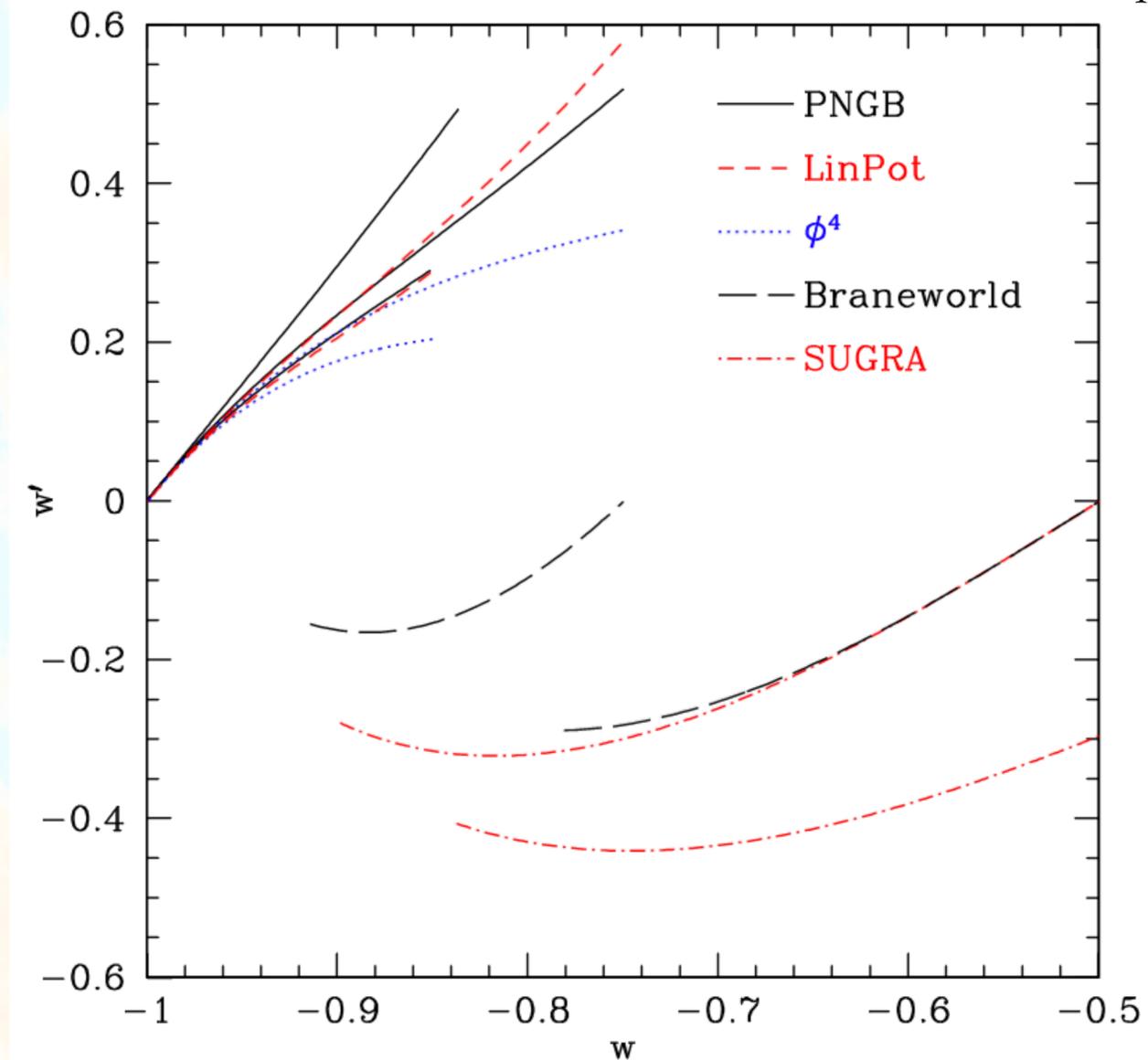
All parametric and non-parametric methods suggest
the same DE behaviour,
in agreement with w_0w_a CDM.

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Dynamics of various DE models

$$(\phi, \dot{\phi}) \longrightarrow (w, w')$$

2 “distinct” regions
in phase-space

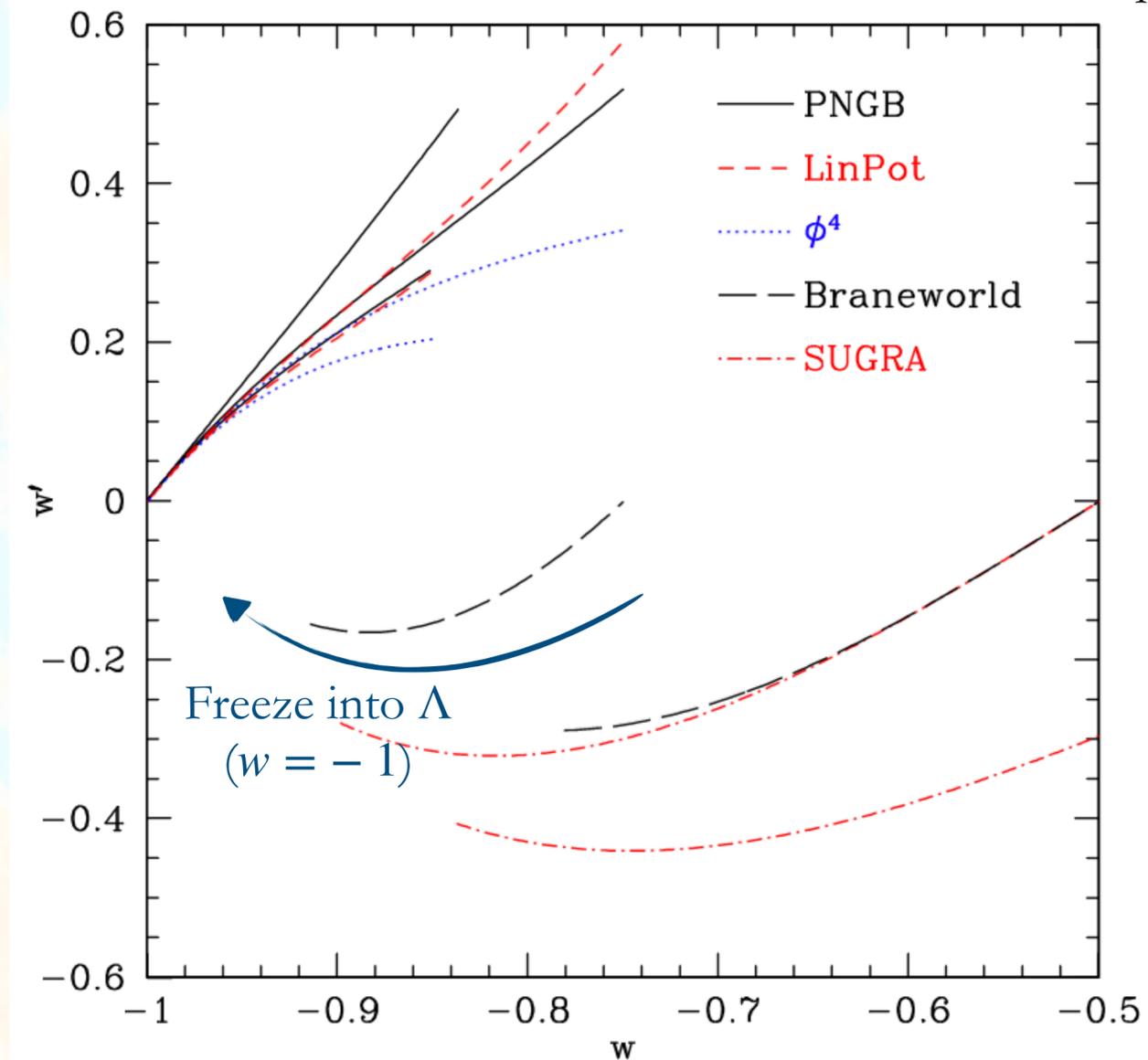


R. de Putter & E. Linder - JCAP 10 (2008) 042

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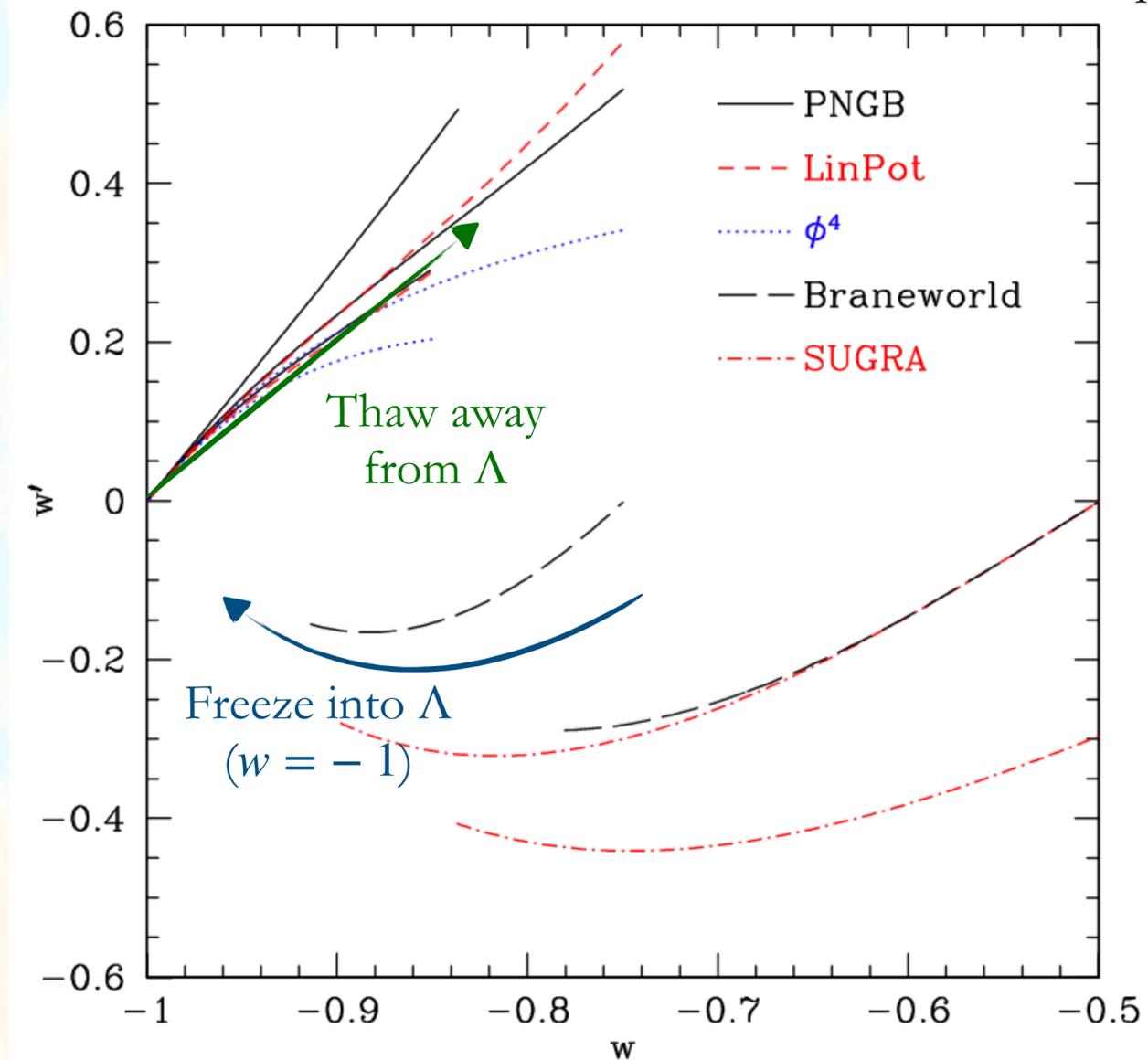


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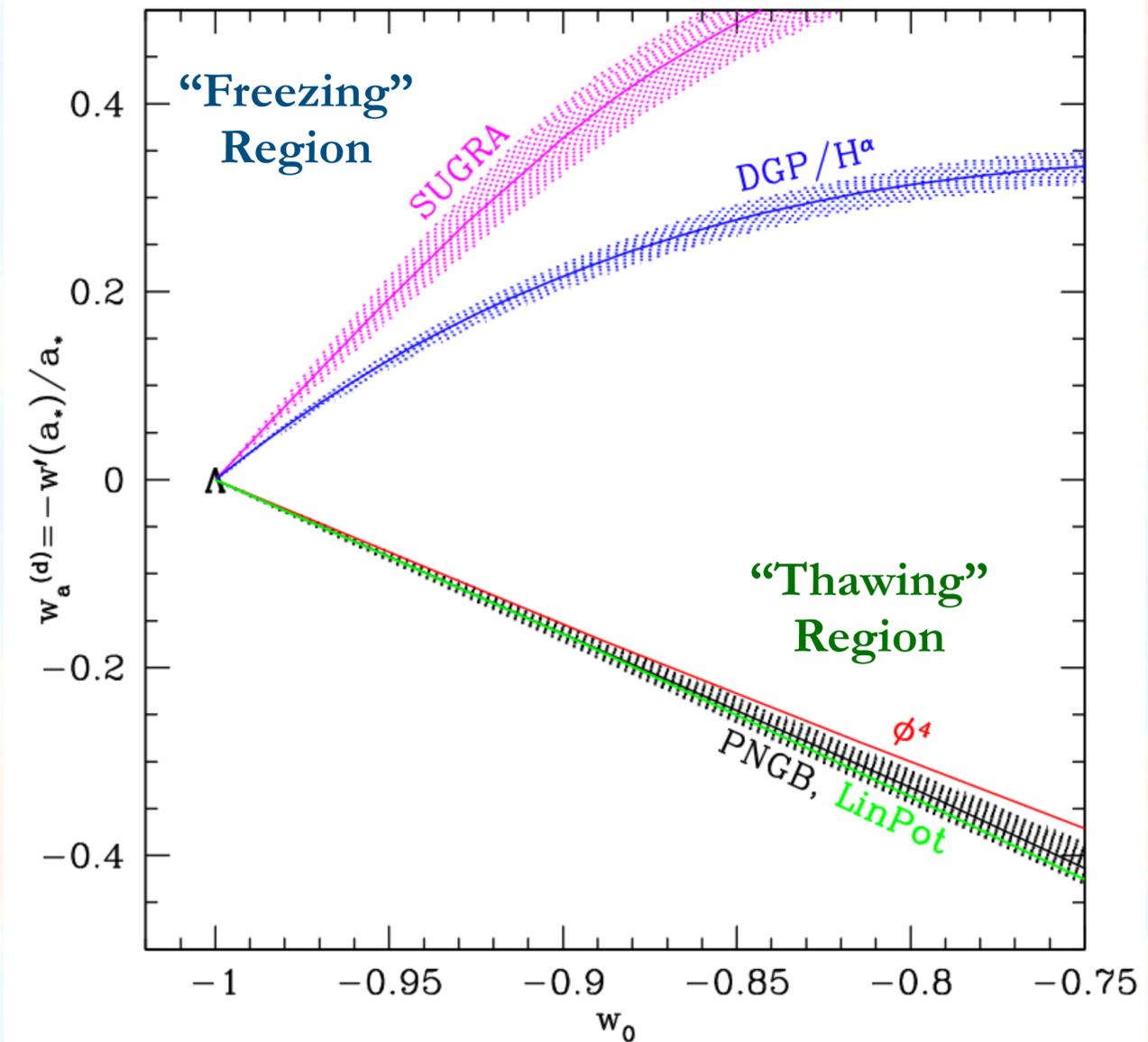
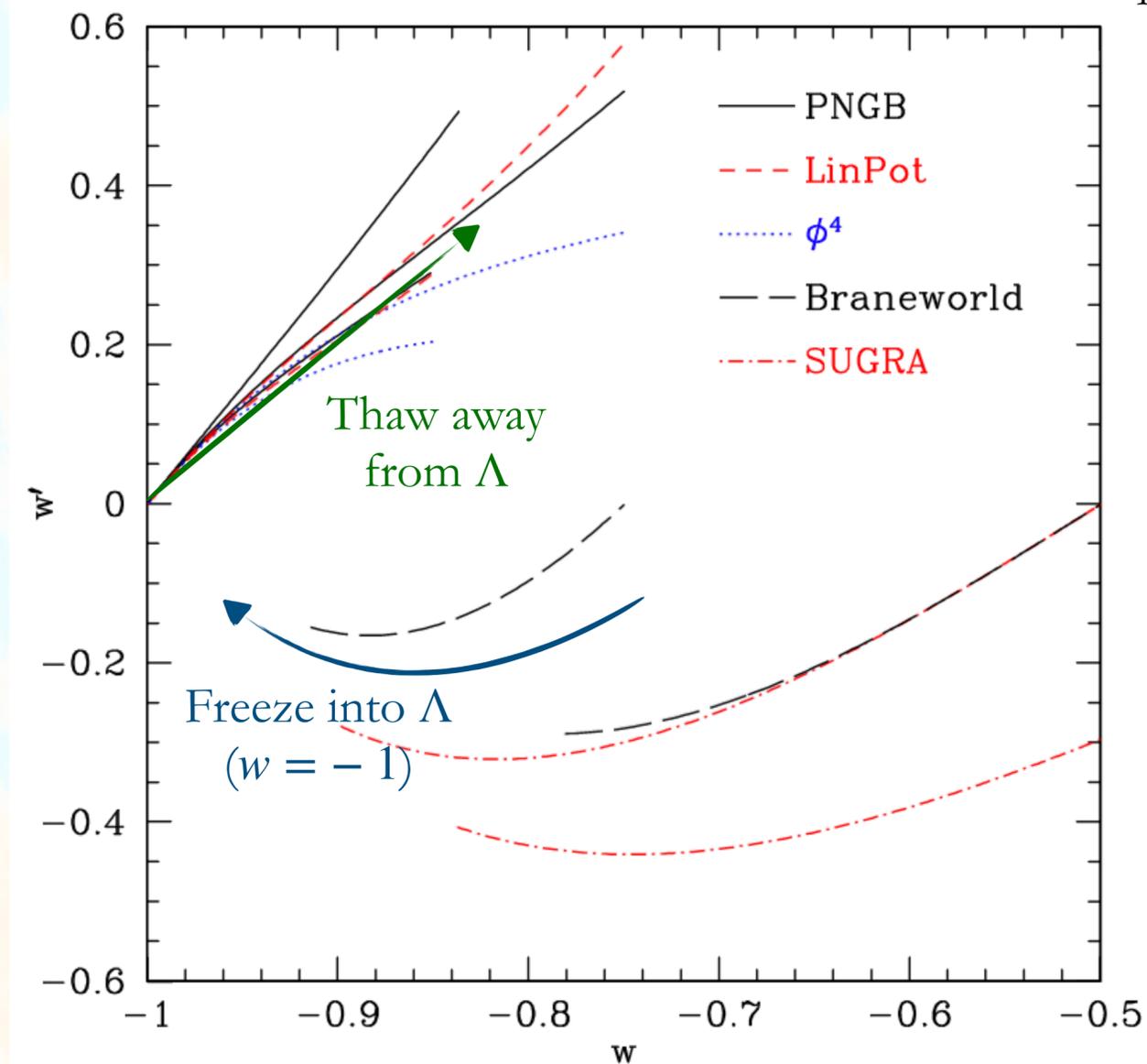
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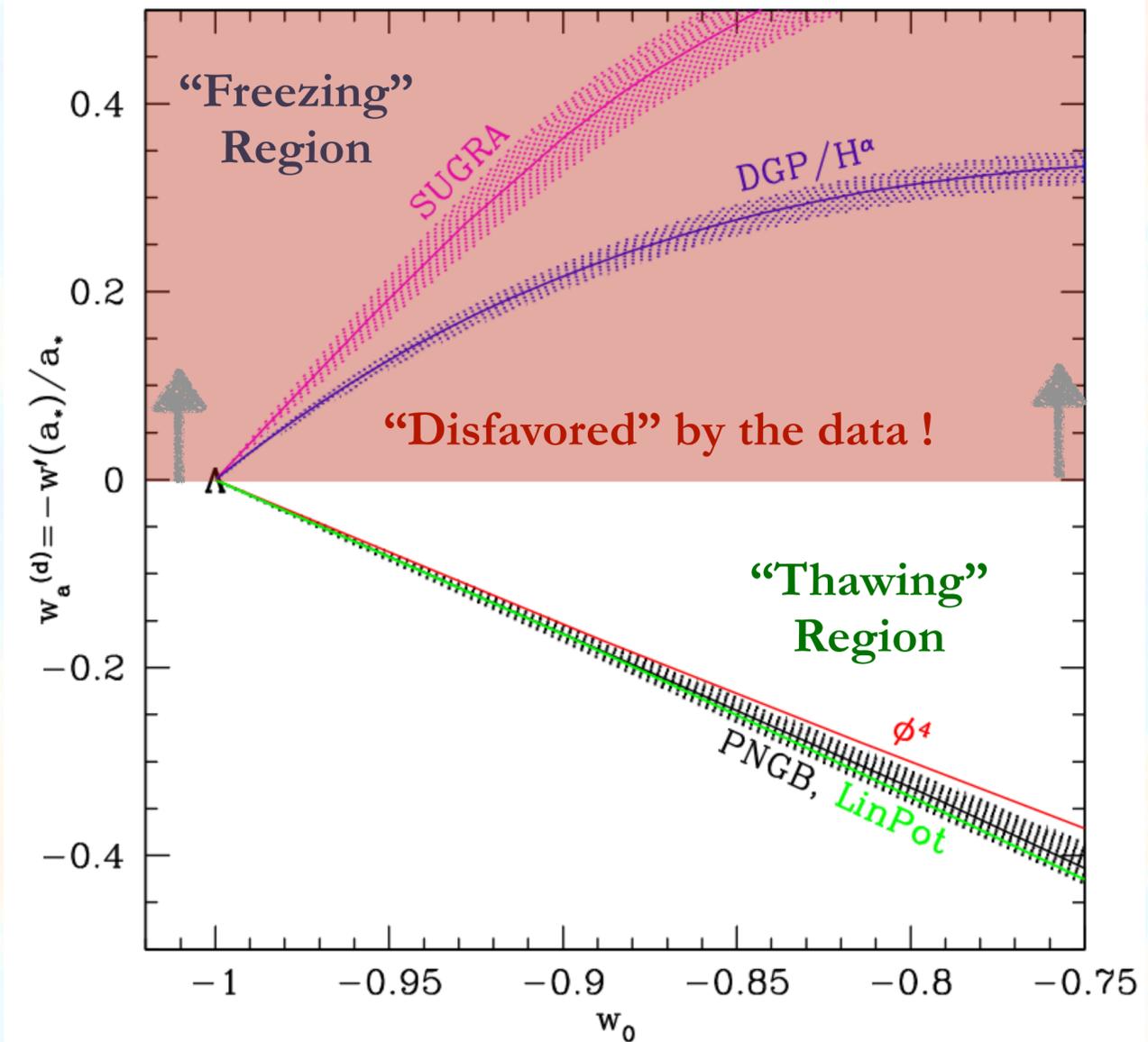
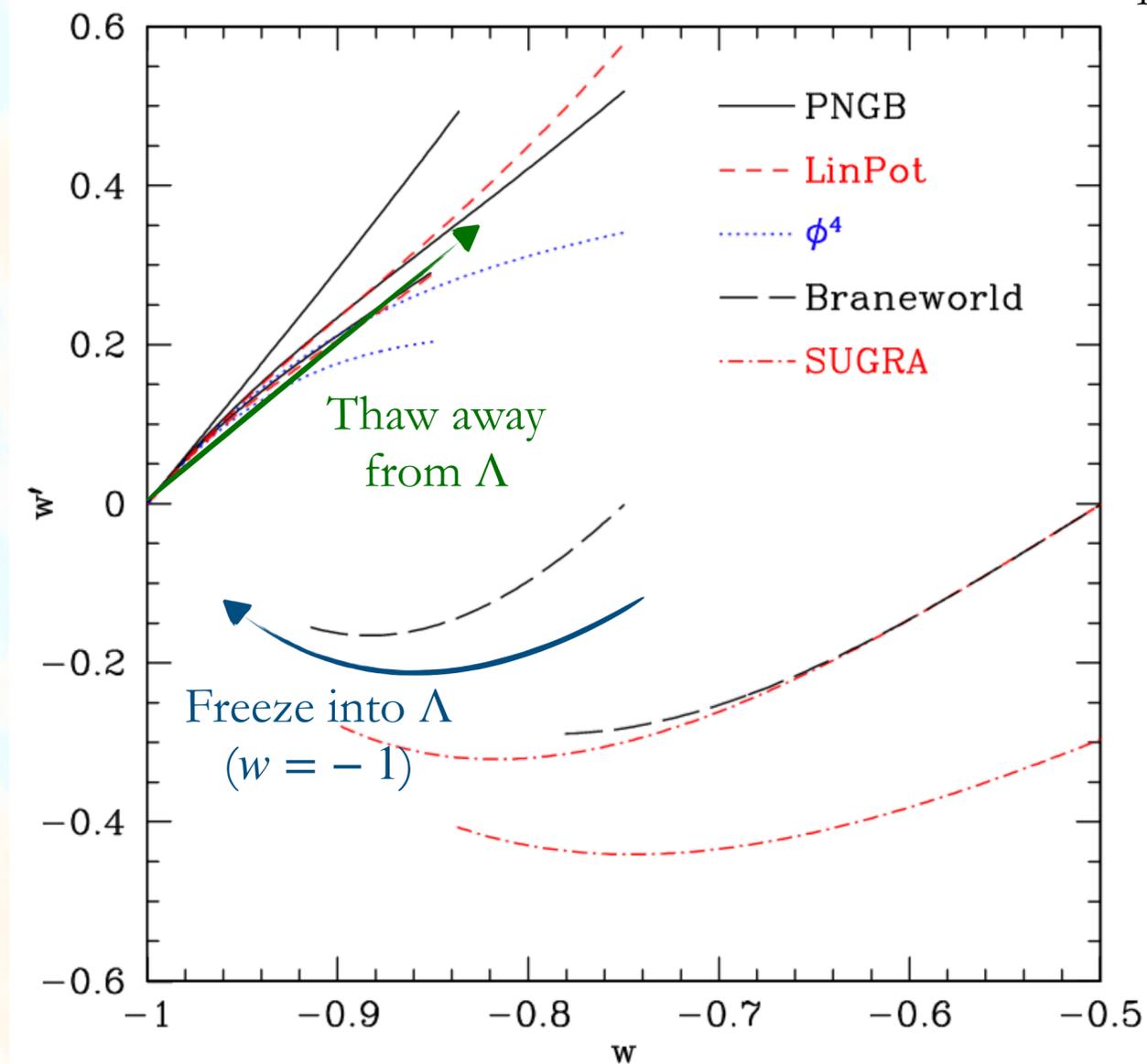
R. de Putter & E. Linder - JCAP 10 (2008) 042

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$$(\phi, \dot{\phi}) \longrightarrow (w, w')$$

2 “distinct” regions
in phase-space

$$w(a) = w_0 + w_a(1 - a)$$



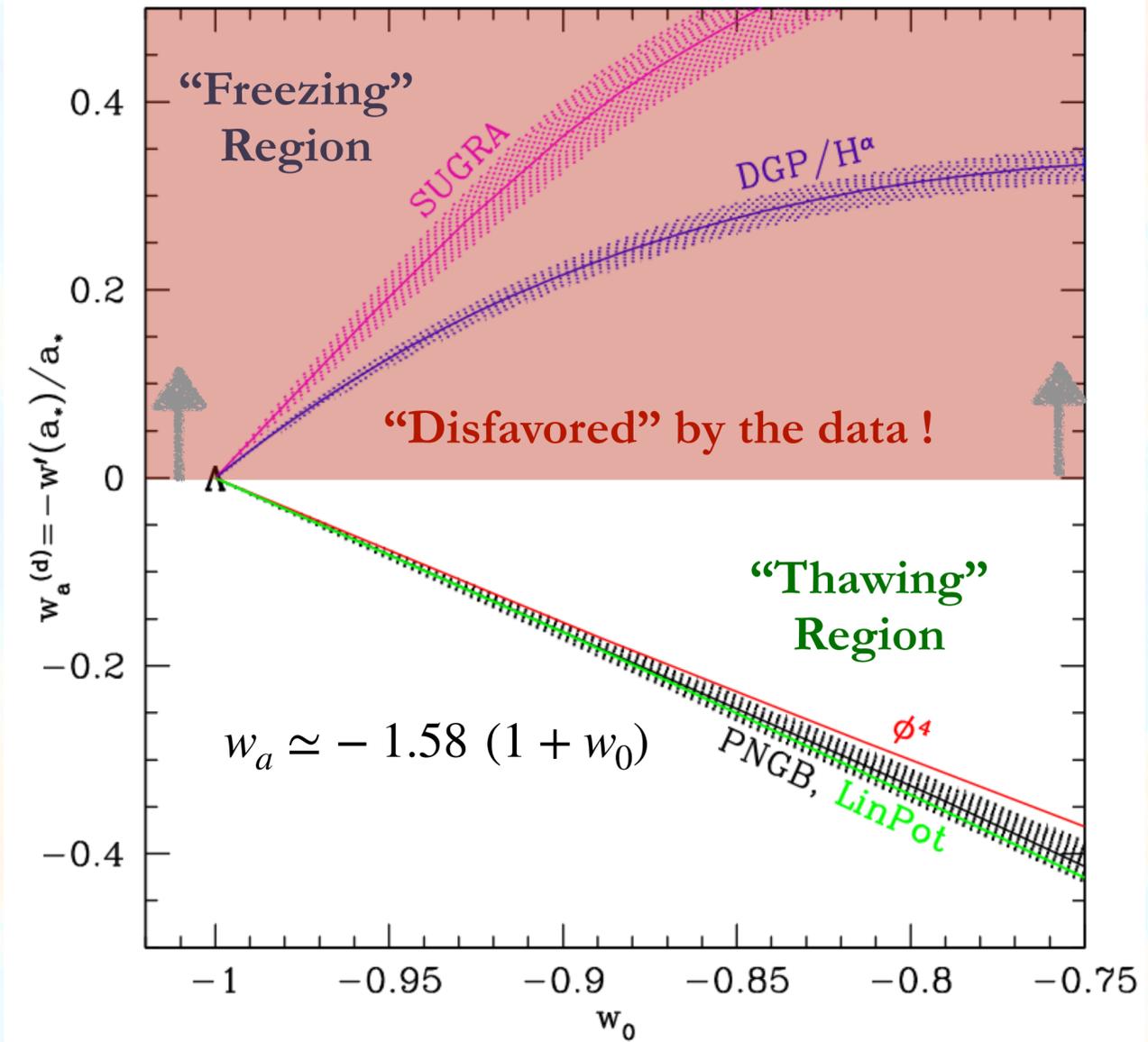
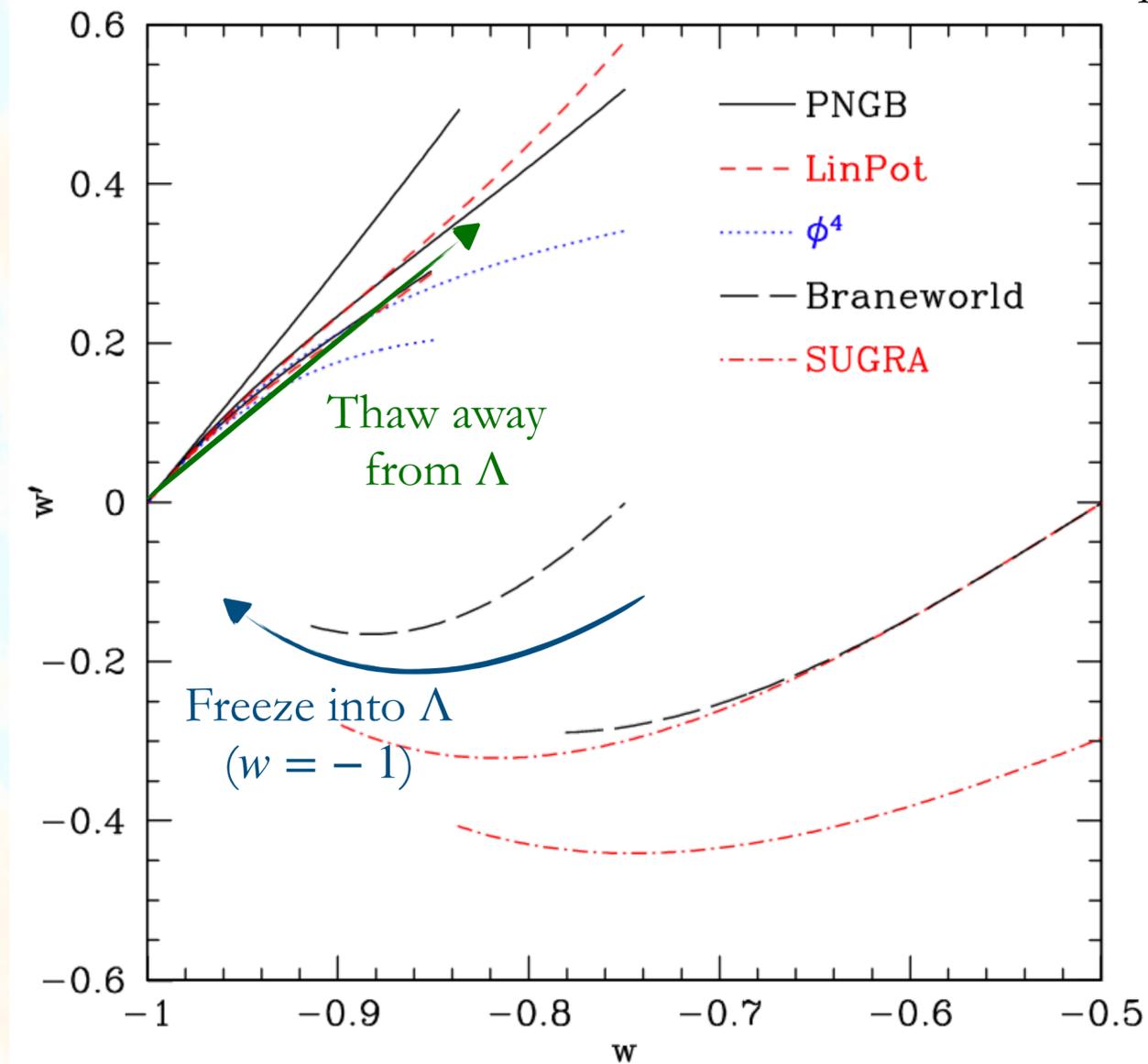
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R. de Putter & E. Linder - JCAP 10 (2008) 042

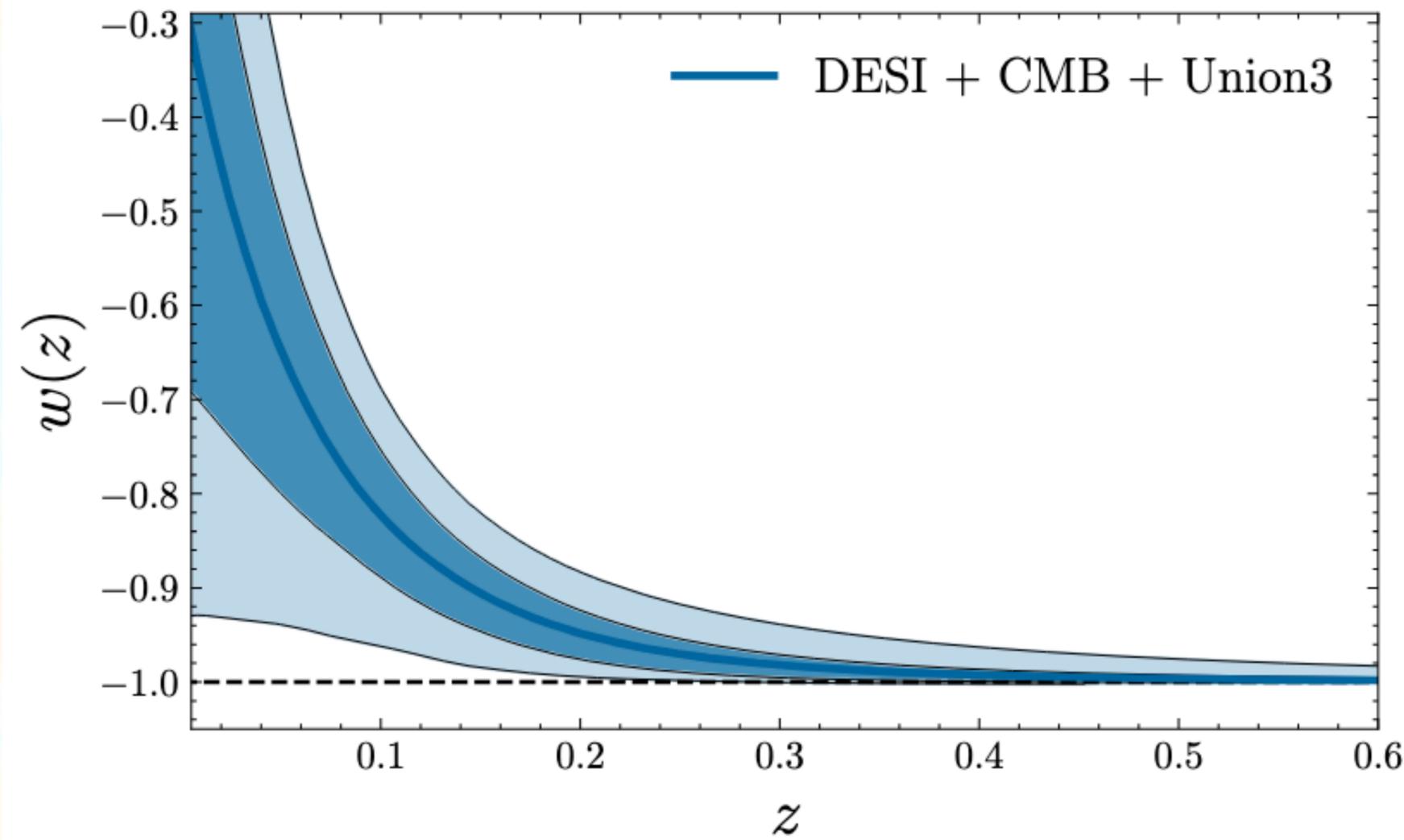
Quintessence-like models

DESI Collaboration, K. Lodha, R. Calderon, W. Matthewson, A. Shafieloo et al.
arXiv: [2503.14743](https://arxiv.org/abs/2503.14743)

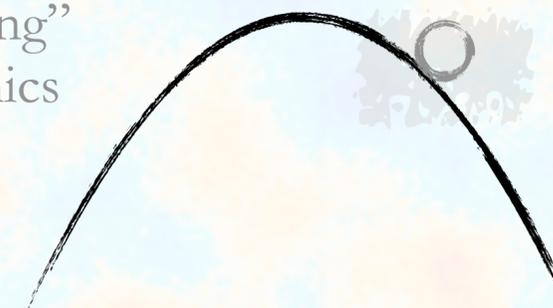
$$w \geq -1$$

E. Linder - *Gen.Rel.Grav.* 40 (2008) 329-356

$$1 + w(a) = (1 + w_0) a^p \left(\frac{1 + b}{1 + b a^{-3}} \right)^{1-p/3}$$



“Thawing”
Dynamics



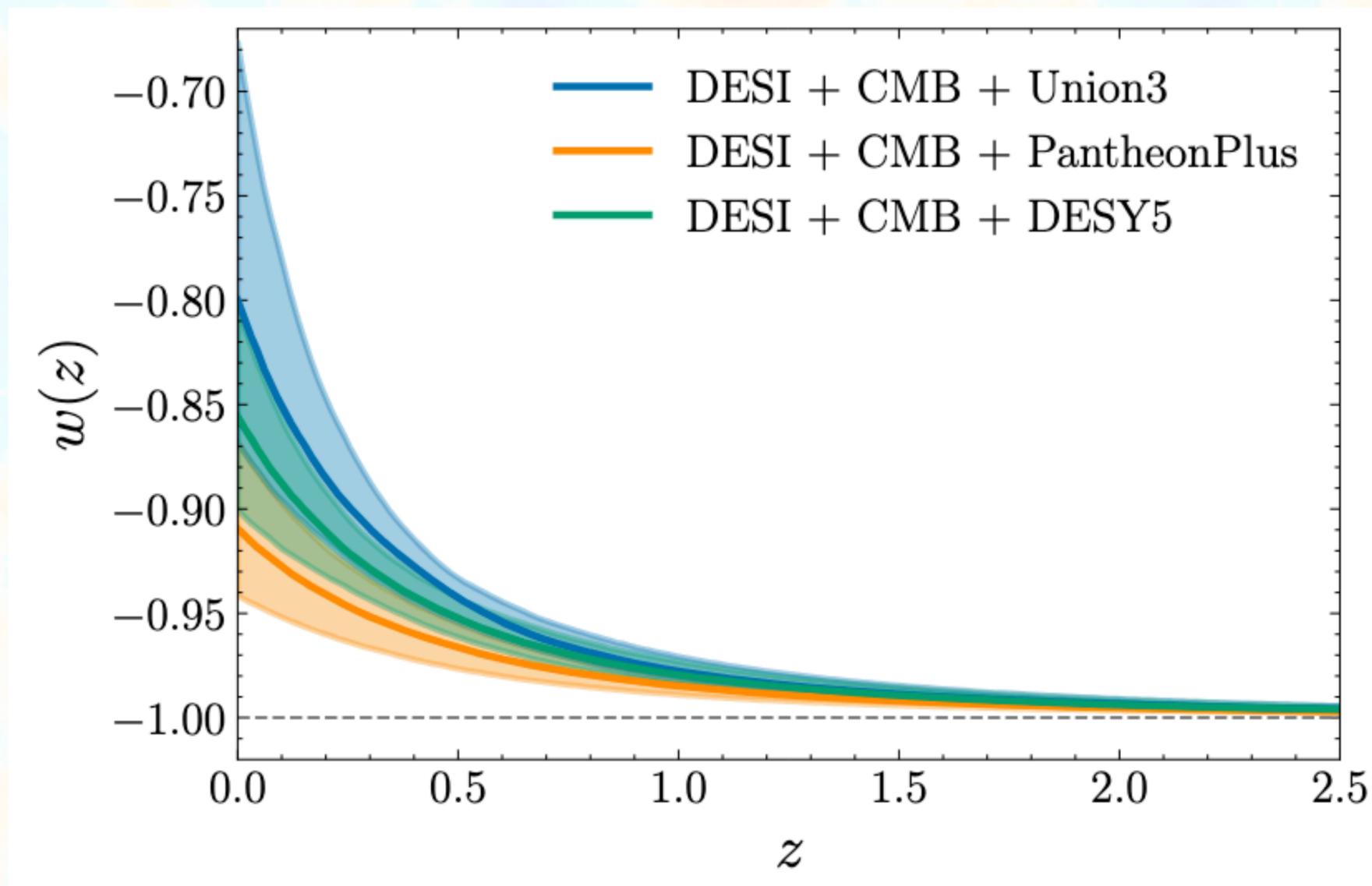
Frozen by
Hubble friction
 $w \simeq -1$

- PANGB/Axion-like
- $V \propto \phi^2$
- $V \propto \phi^4$

A concrete axion-like $V(\varphi)$

DESI Collaboration, K. Lodha, R. Calderon, W. Matthewson, A. Shafieloo et al.
arXiv: [2503.14743](https://arxiv.org/abs/2503.14743)

$$w \geq -1$$



$$V(\varphi) = m_a^2 f_a^2 [1 + \cos(\varphi/f_a)]$$

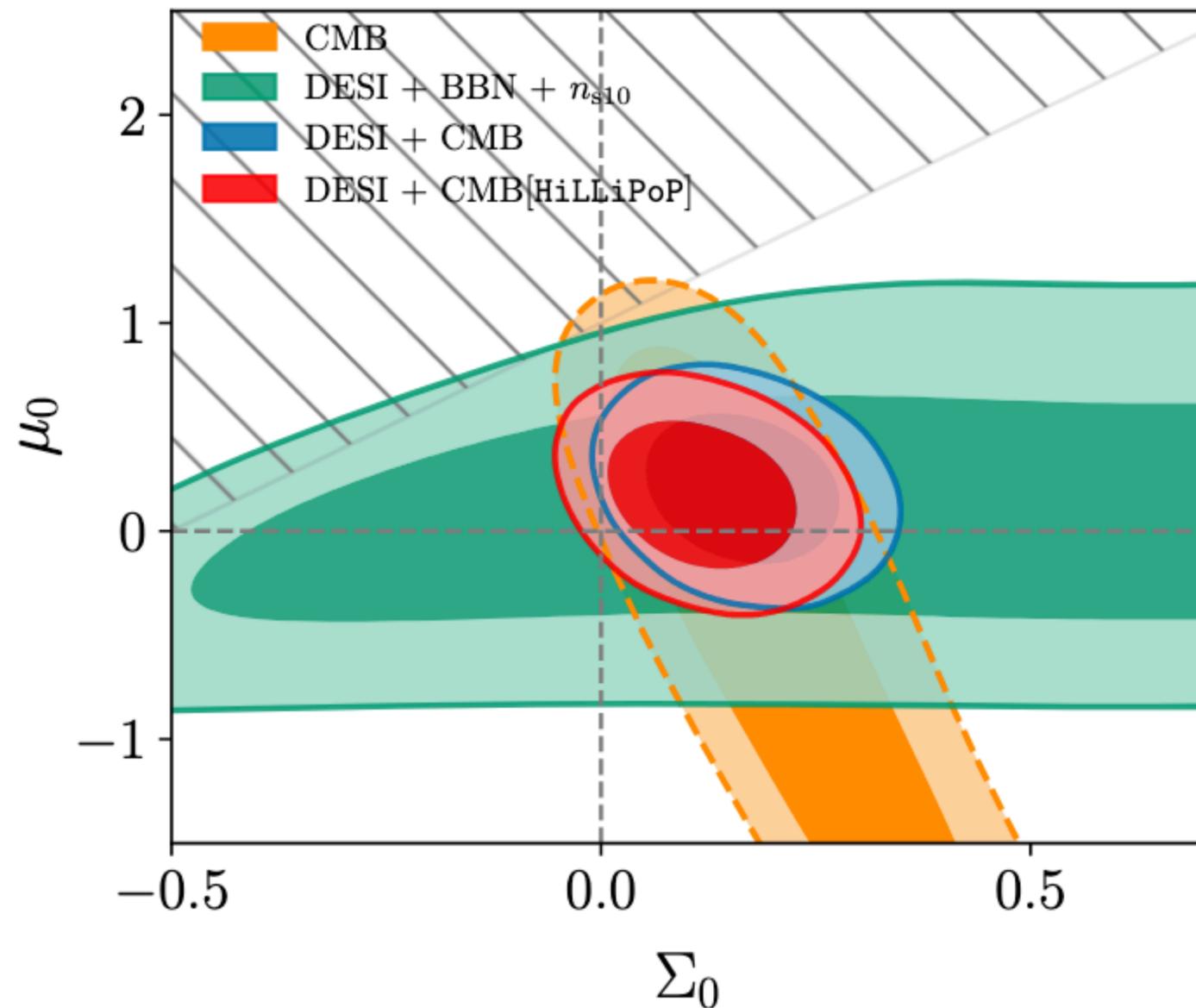
$$\Delta\chi_\varphi^2 = -6.9$$

vs.

$$\Delta\chi_{w_0 w_a}^2 = -17.4$$

Phantom crossing seems to be **needed to significantly improve** the fit over Λ CDM

Testing gravity at cosmological scales



DESI Collaboration, A.G. Adame et al - arXiv: [2411.12022](https://arxiv.org/abs/2411.12022)

Massive Particles (Growth)

$$-\frac{k^2}{a^2}\Psi = 4\pi G\mu(a, k)\rho\delta$$

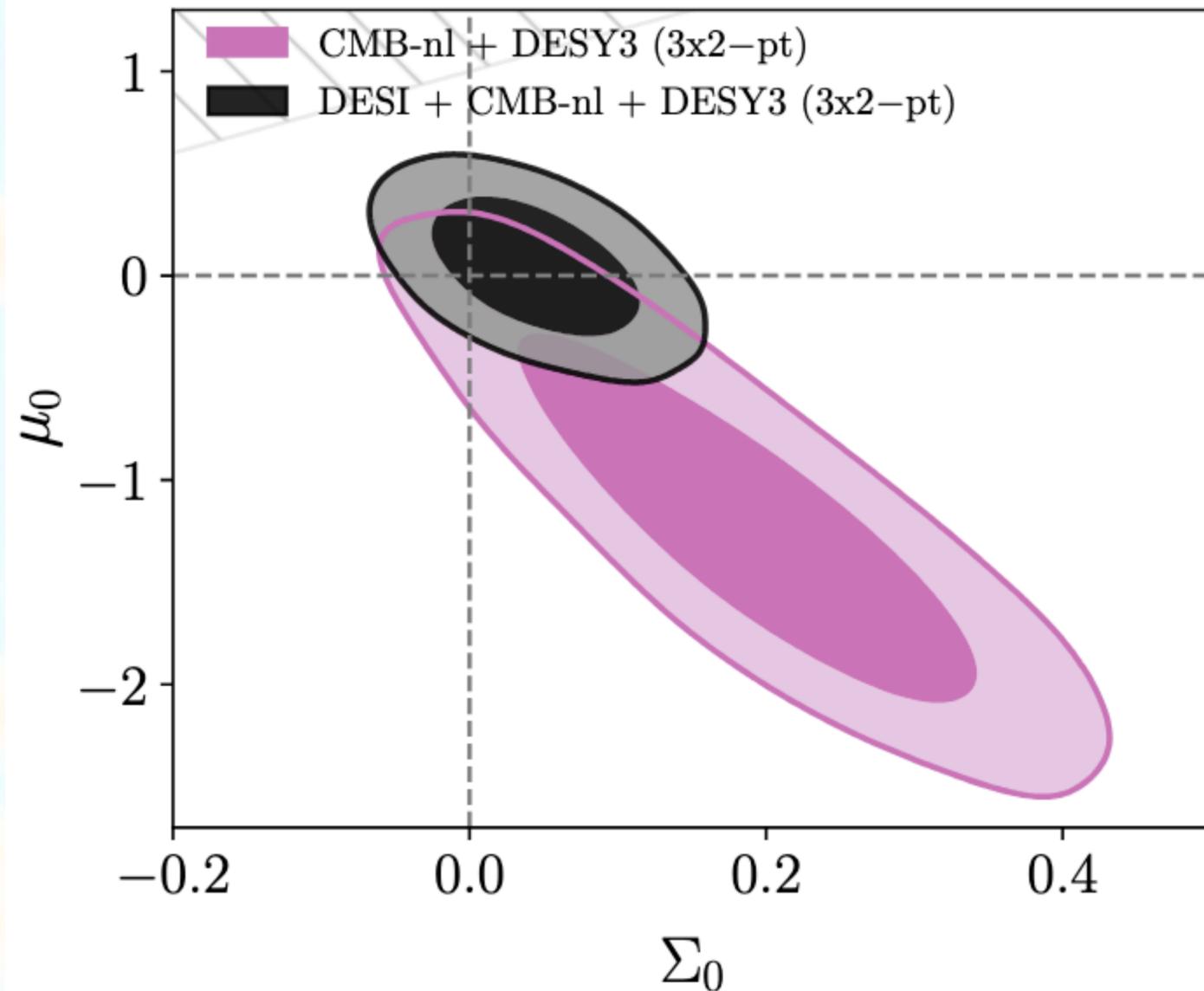
$$\mu(a) = 1 + \mu_0 \frac{\Omega_{\text{DE}}(a)}{\Omega_{\text{DE},0}}$$

Massless Particles (Lensing)

$$-\frac{k^2}{a^2}(\Phi + \Psi) = 8\pi G\Sigma(a, k)\rho\delta$$

$$\Sigma(a) = 1 + \Sigma_0 \frac{\Omega_{\text{DE}}(a)}{\Omega_{\text{DE},0}}$$

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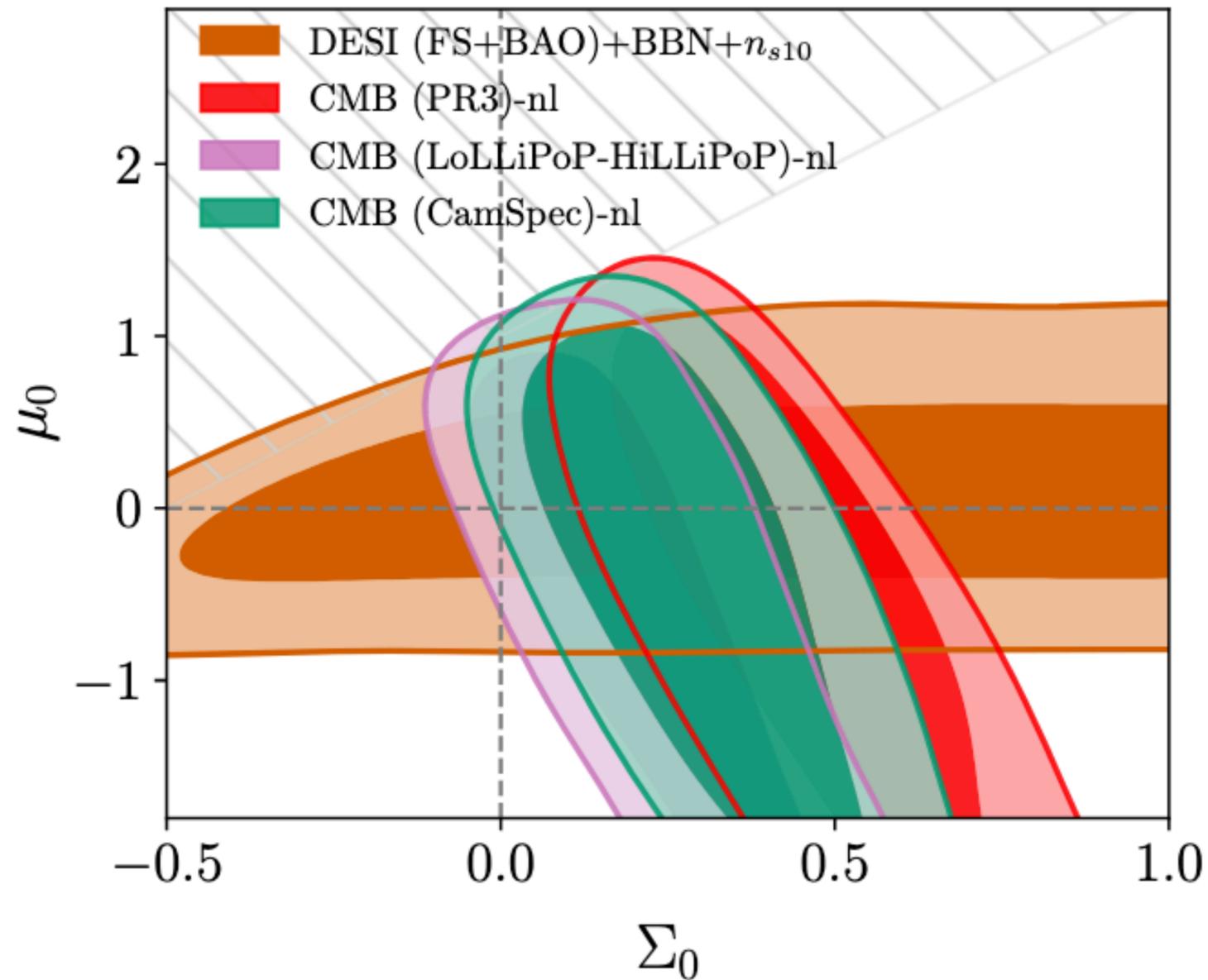
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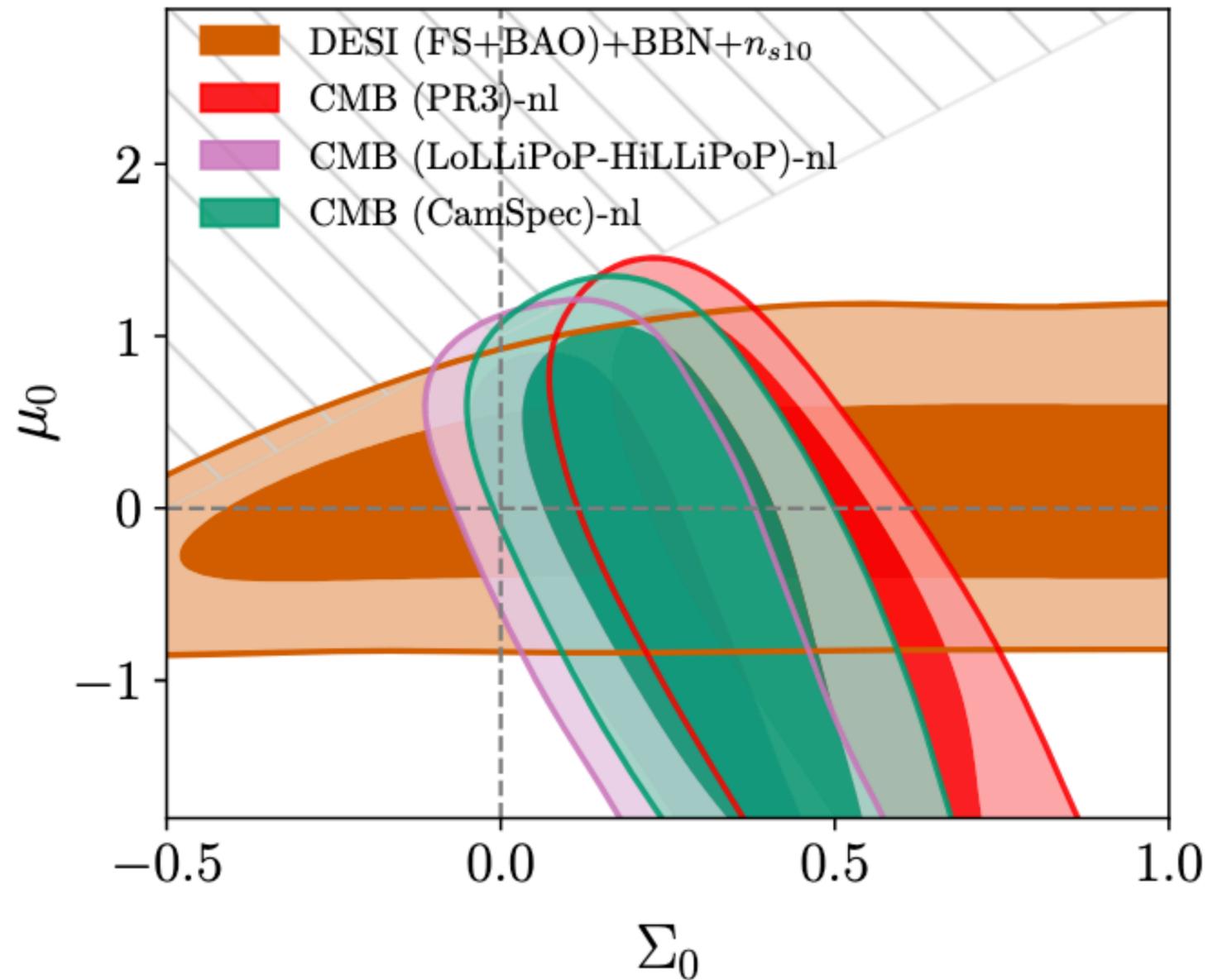
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Hints of modified gravity ?



DESI Collaboration - M. Ishak, J. Pan, R. Calderon et al - arXiv: [2411.12022](https://arxiv.org/abs/2411.12022)

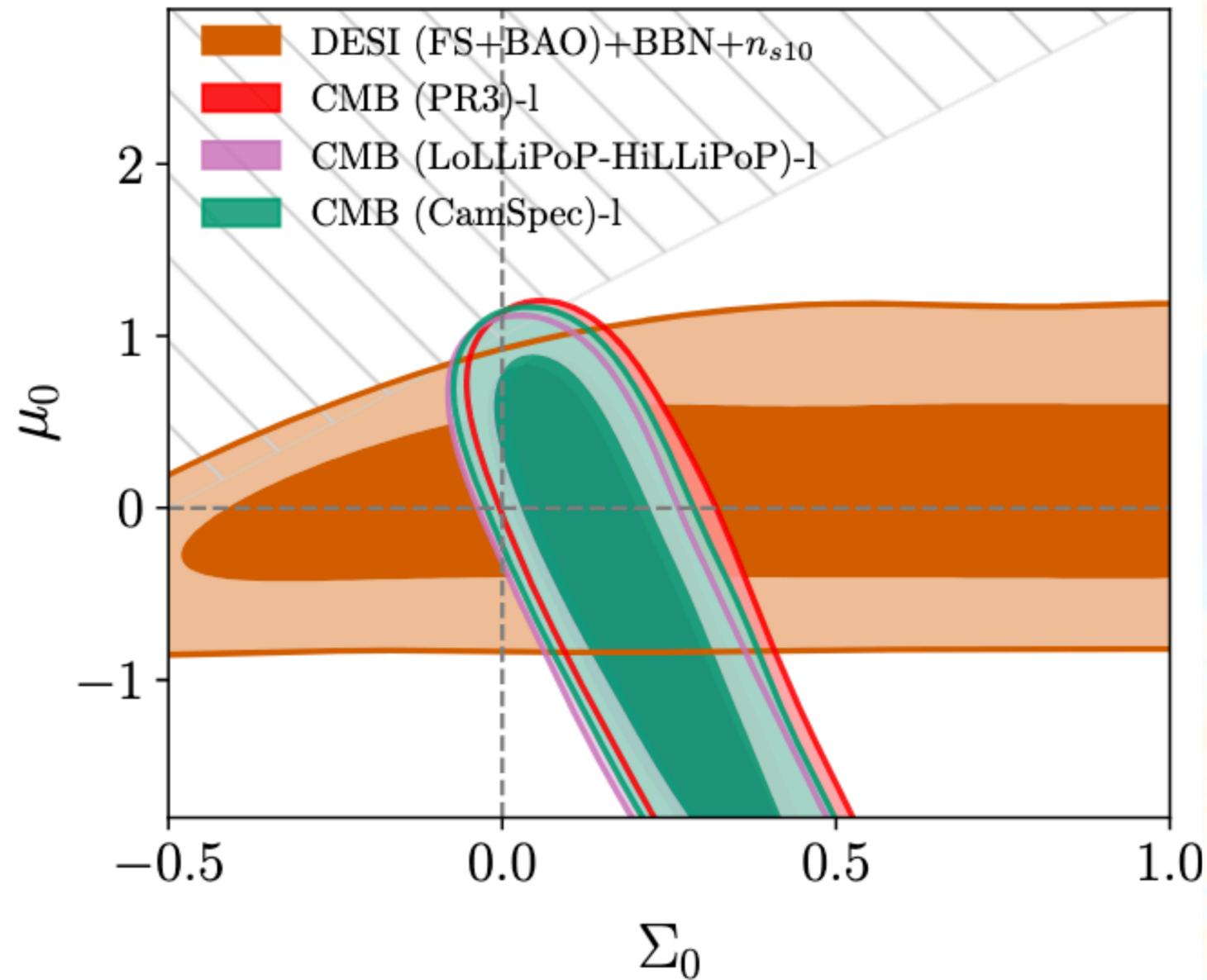
Hints of modified gravity ?



- ▶ **DESI (on its own) can only constrain the growth of structures $\mu(z)$**

DESI Collaboration - M. Ishak, J. Pan, R. Calderon et al - arXiv: [2411.12022](https://arxiv.org/abs/2411.12022)

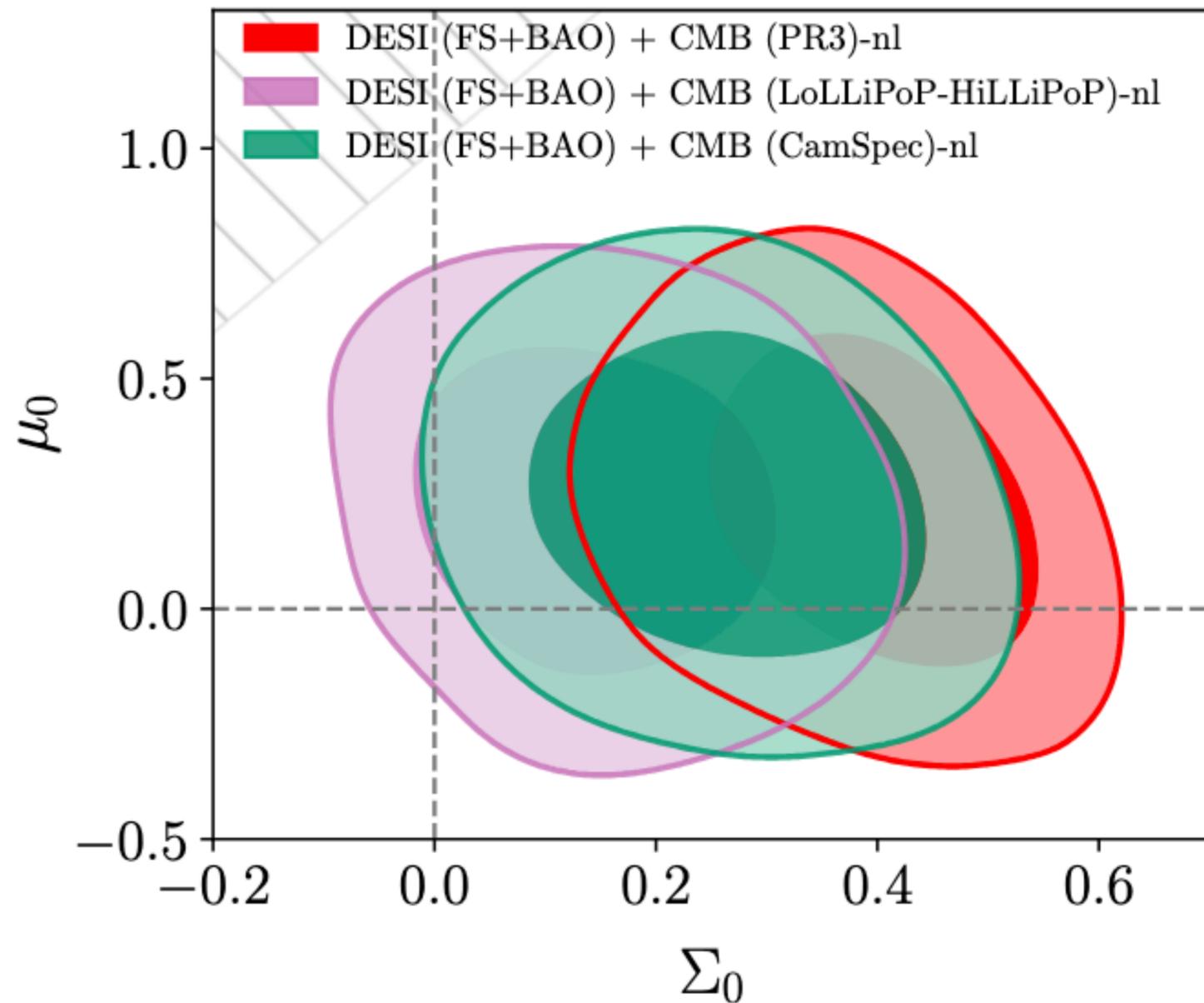
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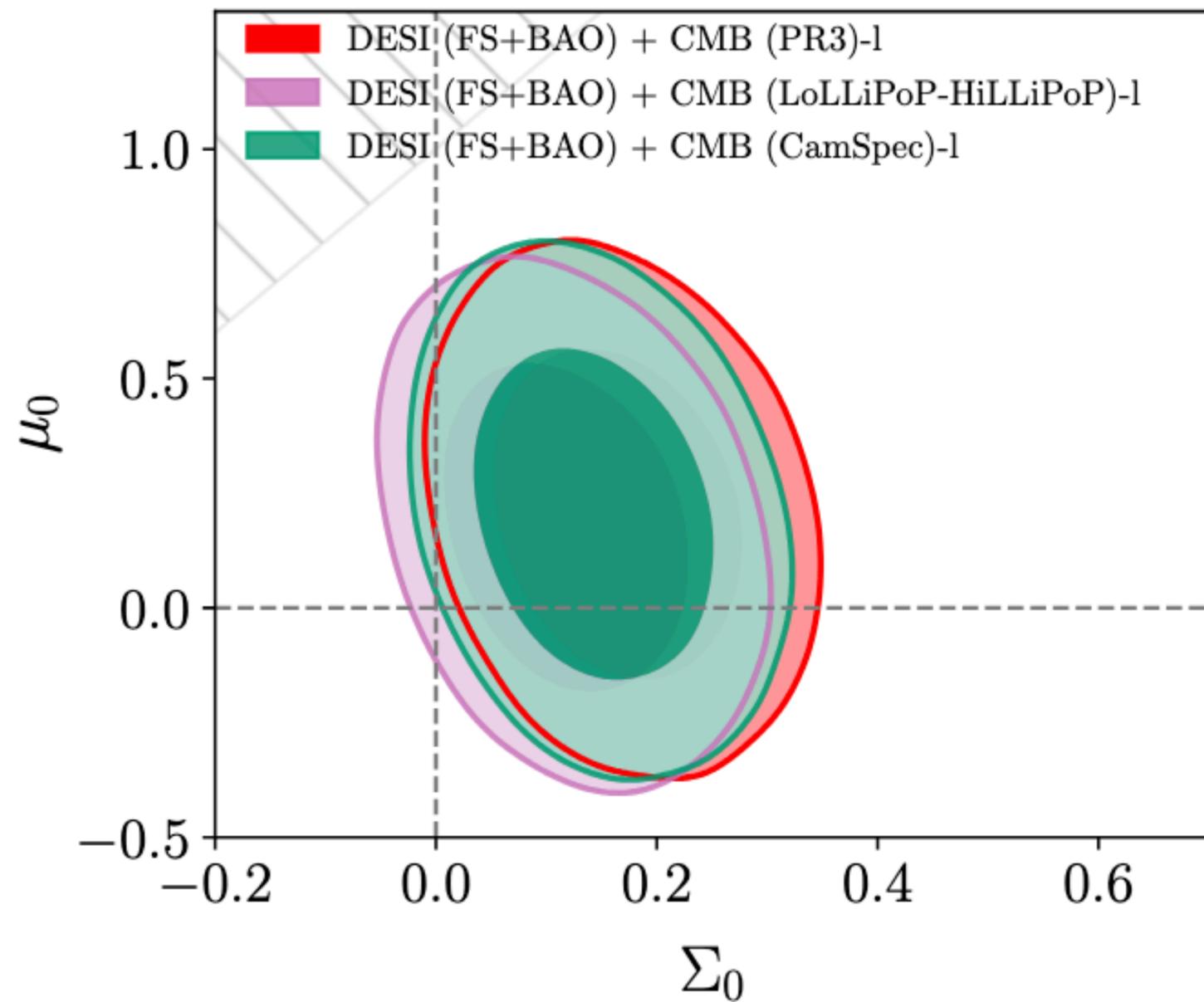
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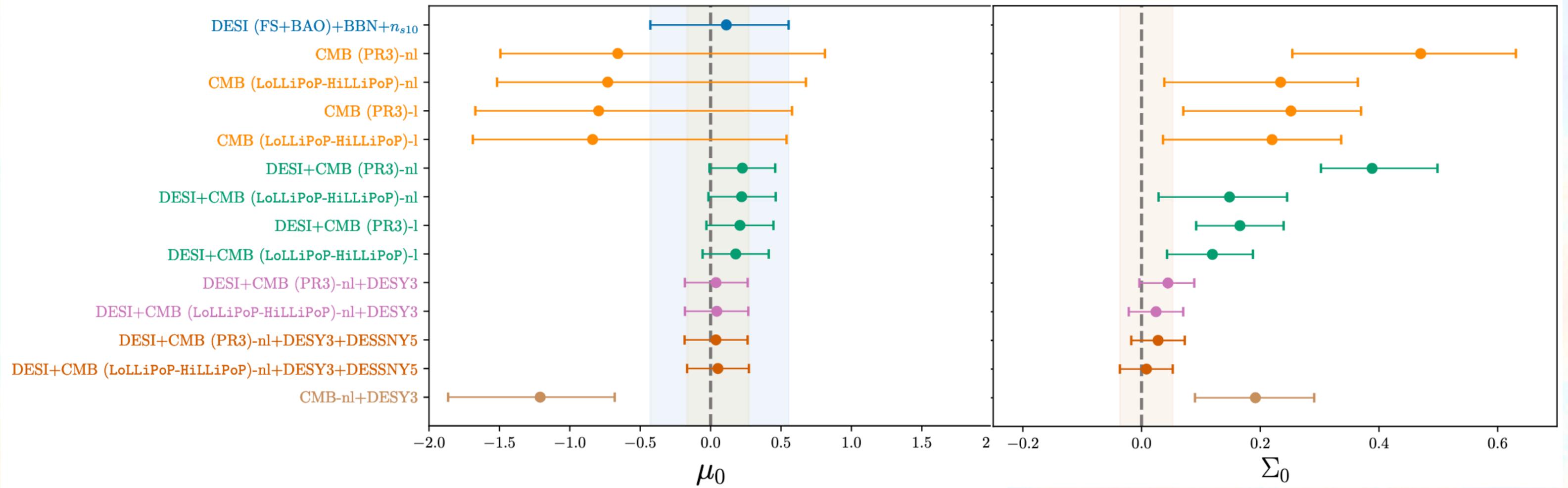
Hints of modified gravity ?



- ▶ **DESI (on its own) can only constrain the growth of structures $\mu(z)$**
- ▶ **Without CMB lensing, constraints on $\Sigma(z)$ are highly sensitive to the choice of CMB likelihood**
- ▶ **Including CMB lensing helps stabilising the constraints on $\Sigma(z)$**

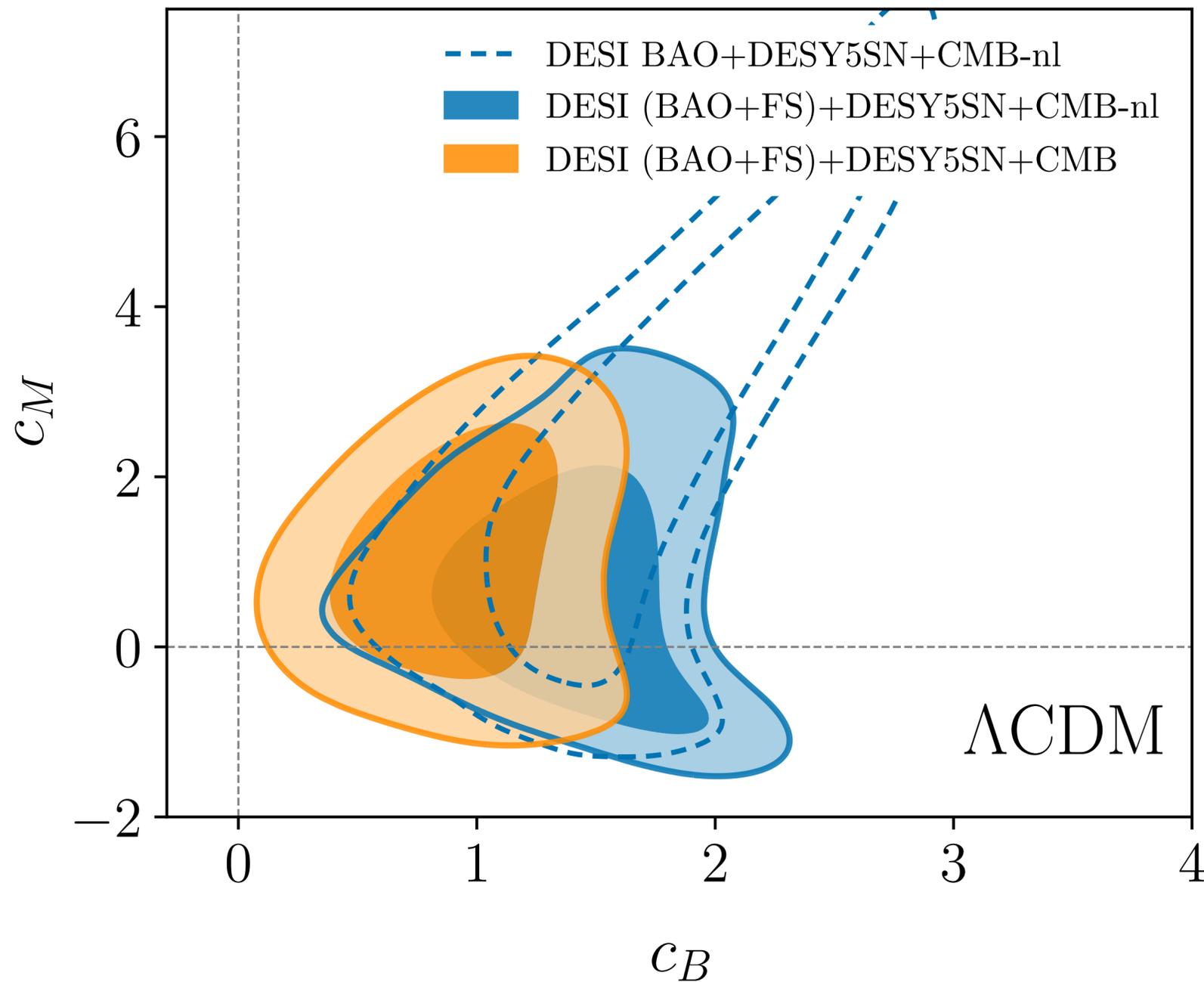
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Implications of $w(z) < -1$



In the EFT of DE, linear perturbations **entirely characterised** by 4 functions of time

- “Running”:

$$\alpha_M = \frac{d \ln M_{\text{eff}}^2}{d \ln a}$$
- “Braiding”:

$$\alpha_B(t)$$
- “Kineticity”:

$$\alpha_K(t)$$
- “Tensor speed excess”:

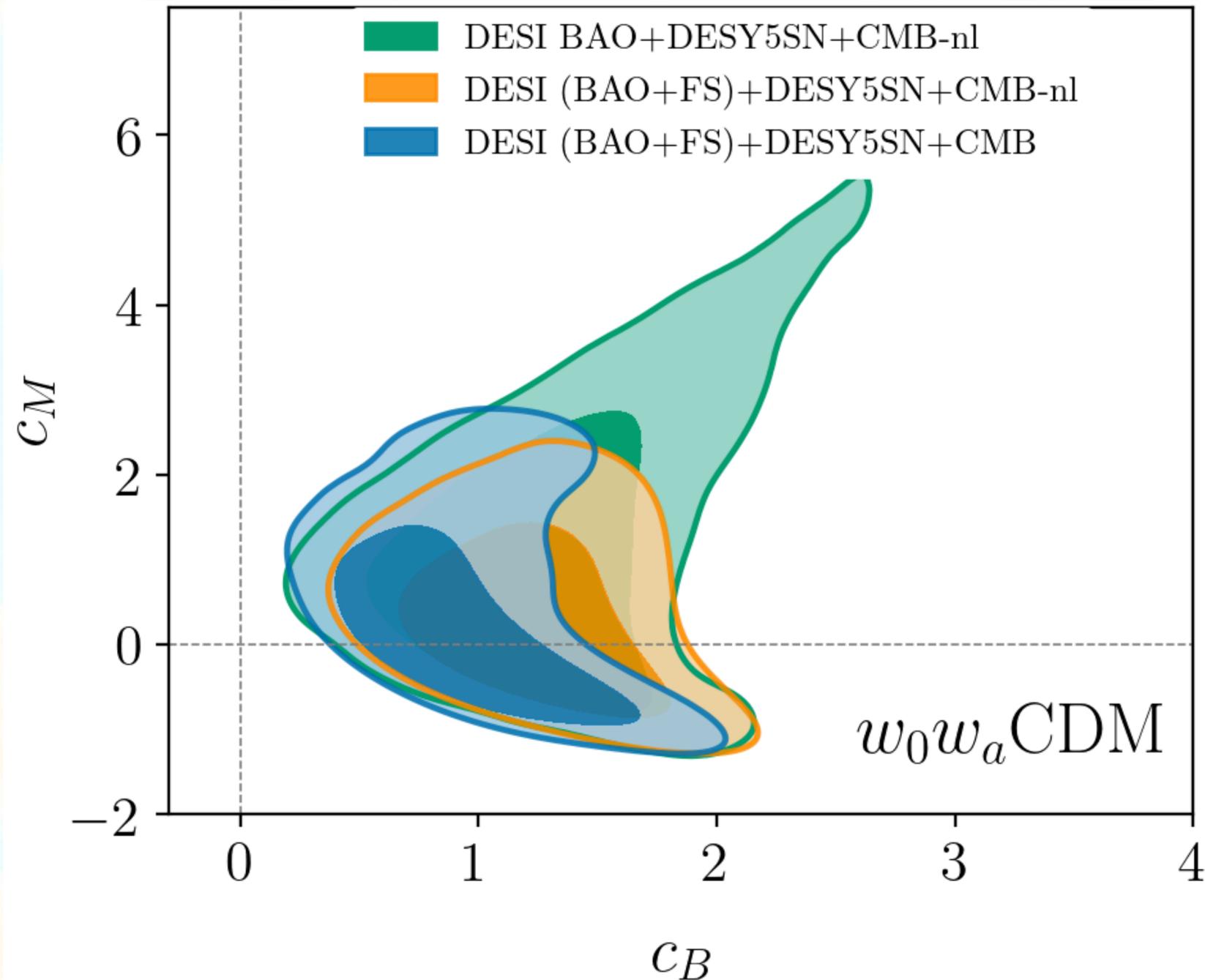
$$\alpha_T = c_T^2 - c^2 \lesssim 10^{-15}$$

At least one of the $\alpha_i(t) \neq 0$!

$$\alpha_i(t) = c_i \Omega_{DE}(a)$$

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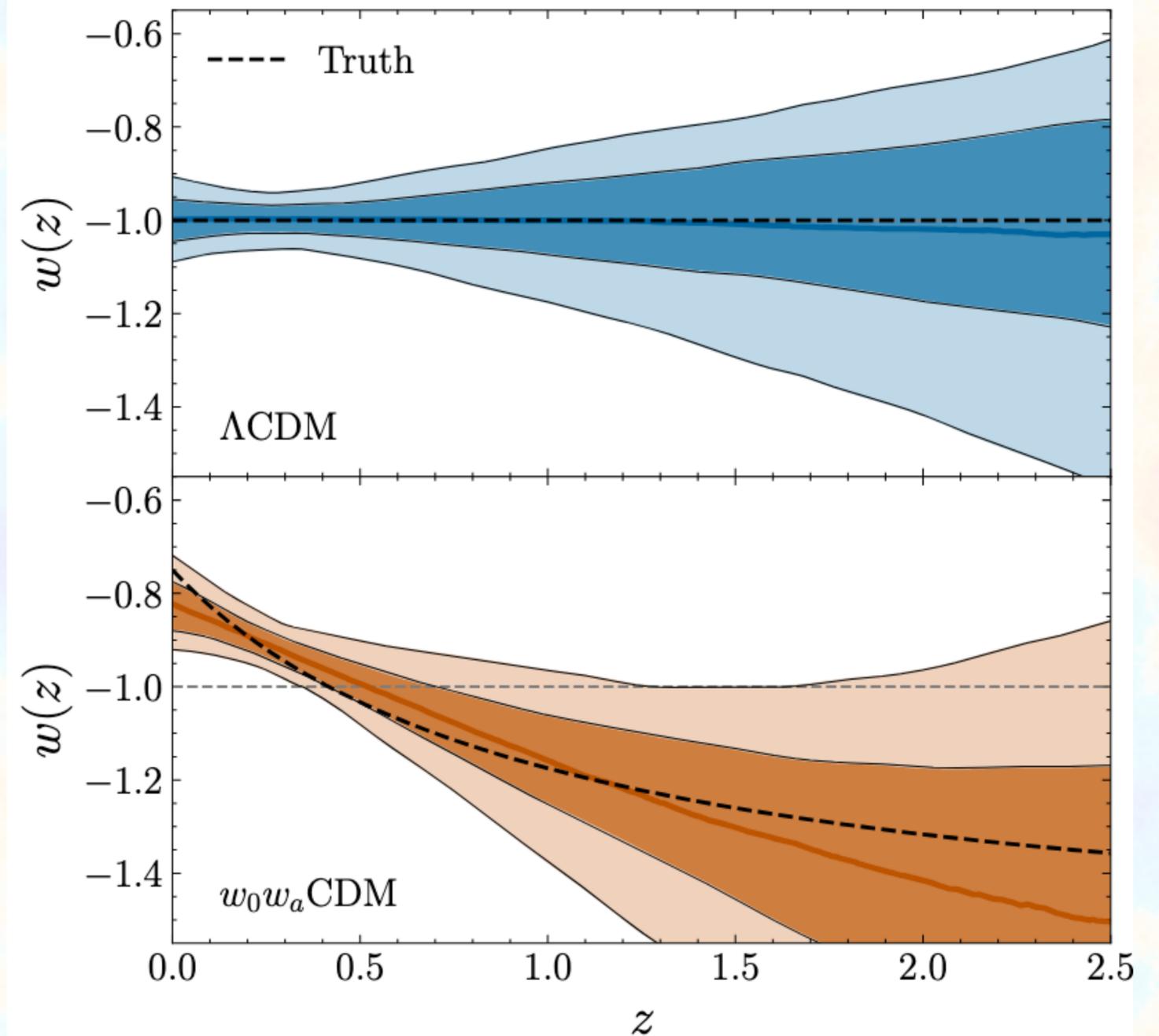
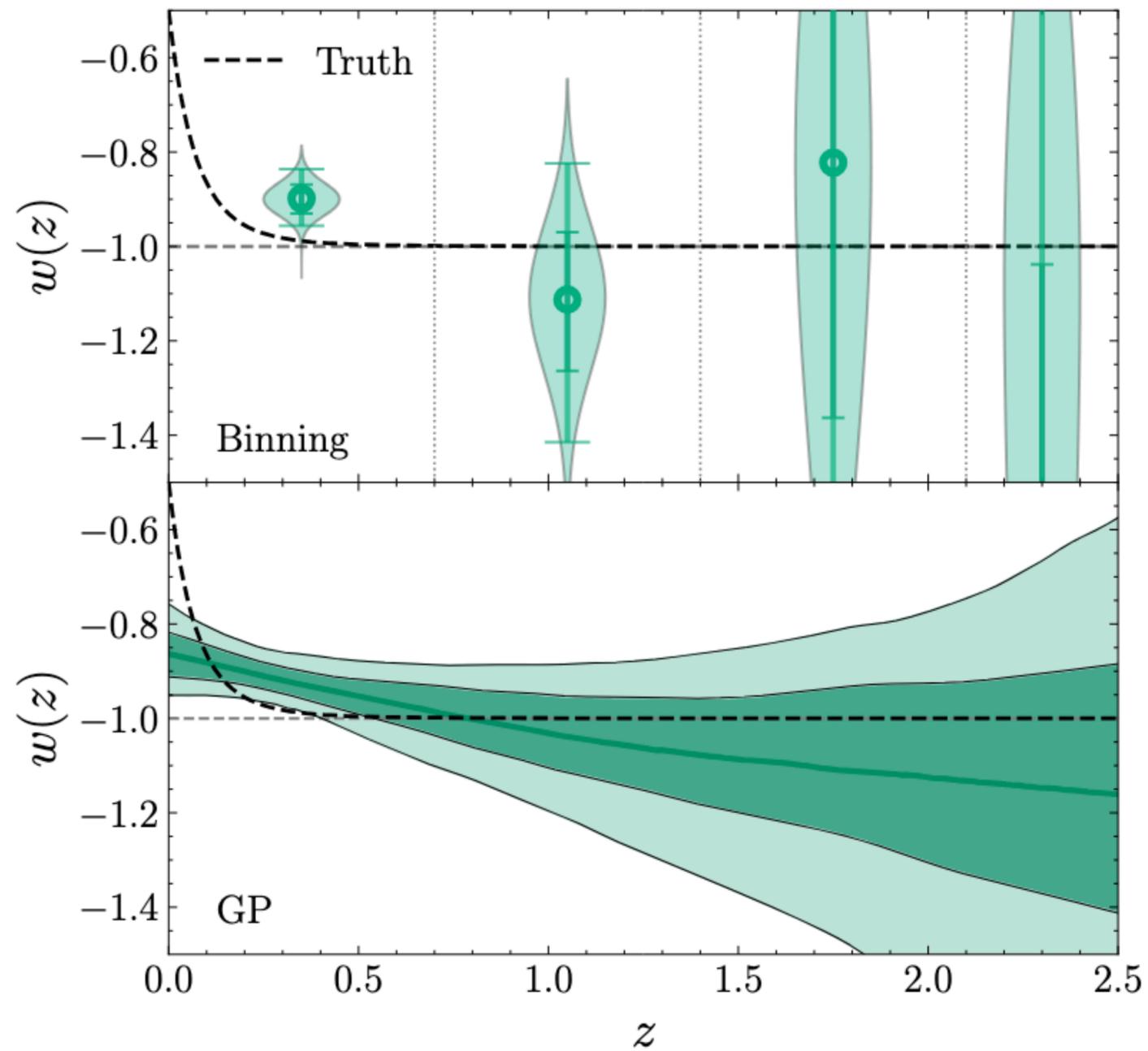
DESI Collaboration - M. Ishak, J. Pan, R. Calderon et al - arXiv: [2411.12022](https://arxiv.org/abs/2411.12022)

Summary

- Tantalising hints of an **evolving dark energy** component:
 $\sim 3 - 4\sigma$ deviation from Λ ($w_0 = -1, w_a = 0$)
Results are **stable** under different **data combinations**
& **NOT** driven by the parametrisation of $w(a)$
- Models that cross $w = -1$ consistently fit the data better than those that do not
(GP suggests $w(z) < -1$ at $\sim 3\sigma$)
- If confirmed, these results could have profound theoretical implications for DE
DE/DM interactions, Non-minimal couplings/Modified gravity
- Careful investigation of the CMB lensing excess ($A_{\text{lens}} > 1$)
 $\rightarrow \Sigma(z) > 1$
- $\rightarrow \Sigma m_\nu < 0$
- DESI (DR2) constraints from 2-pt & 3-pt functions are on the way (+Euclid results!)
Extremely exciting times for Cosmology

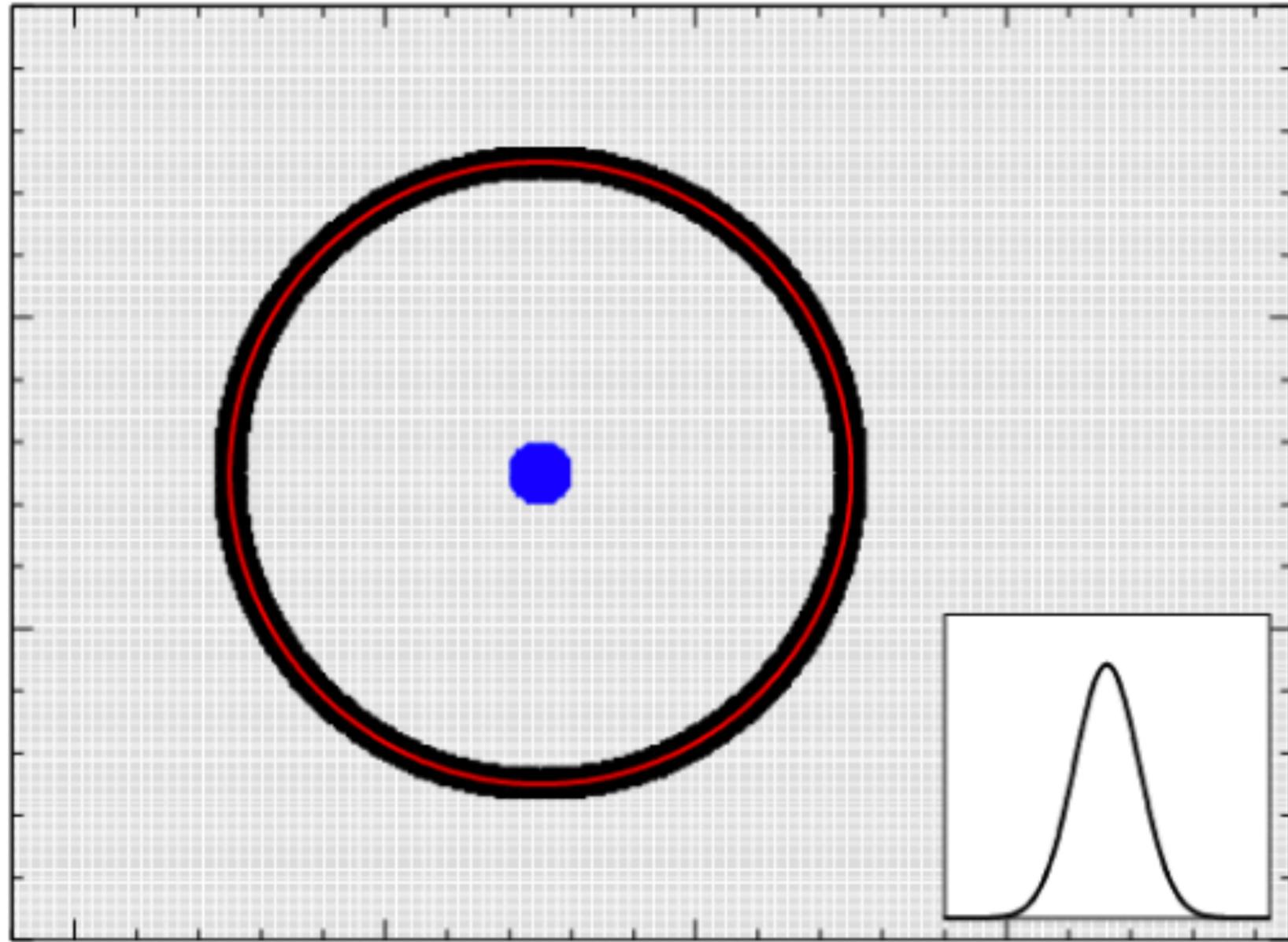
calderon@fzu.cz

Validation with Mocks



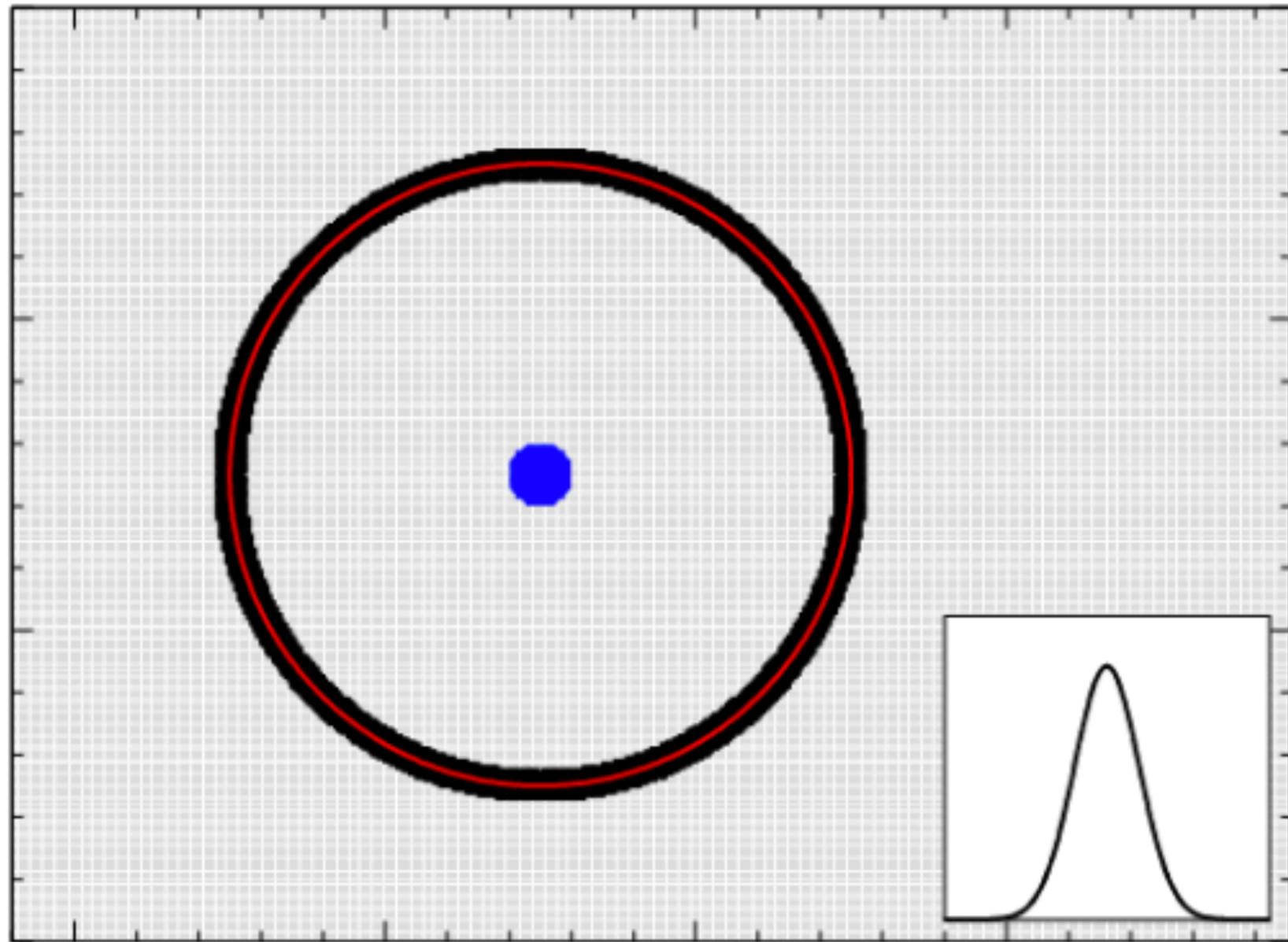
DESI Collaboration, K. Lodha, R. Calderon, W. Matthewson, A. Shafieloo et al.
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Baryon Acoustic Oscillations



Padmanabhan et al. (2012) MNRAS

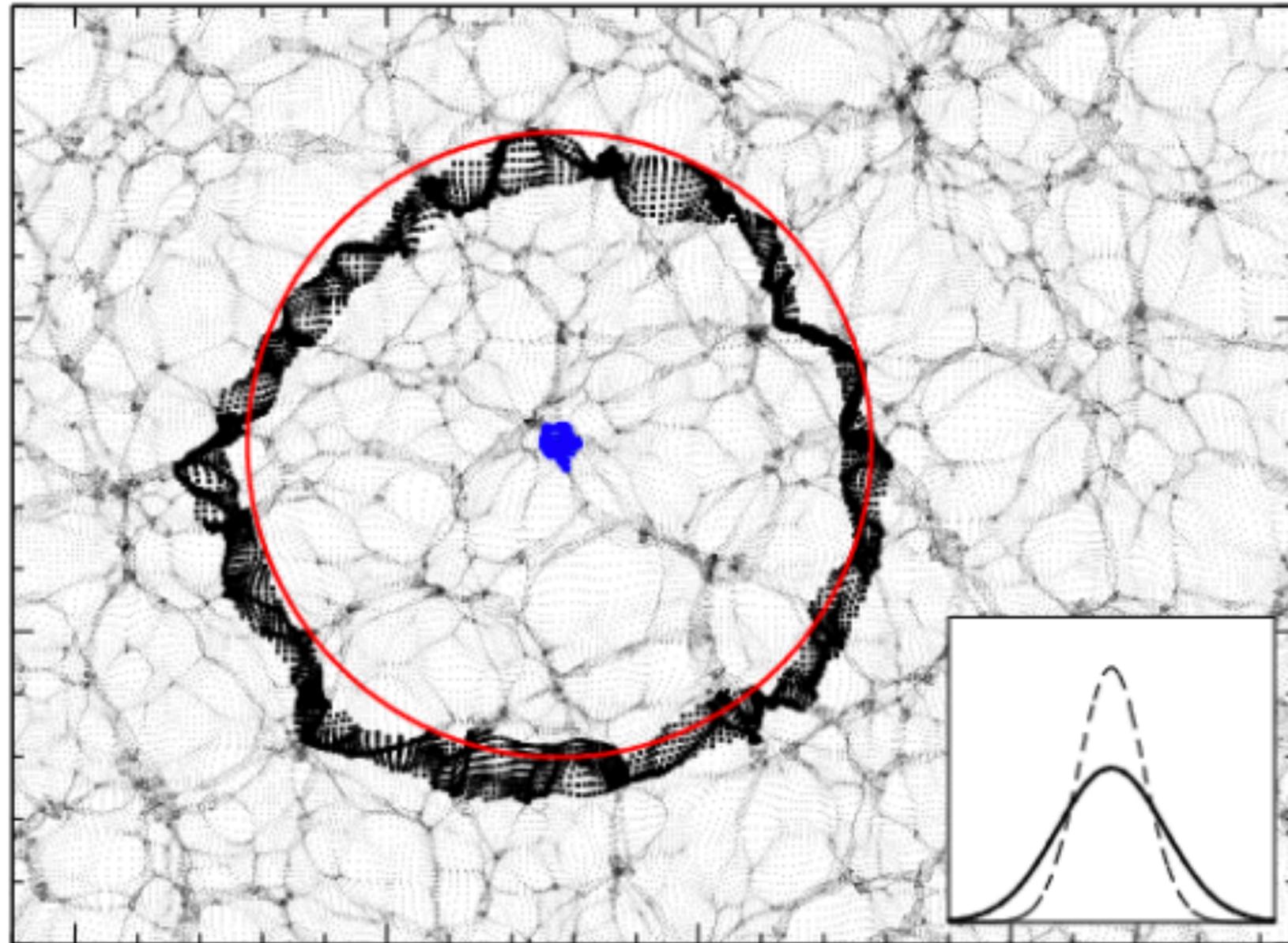
Baryon Acoustic Oscillations



- The BAO feature is expected to be **isotropic** !

Padmanabhan et al. (2012) MNRAS

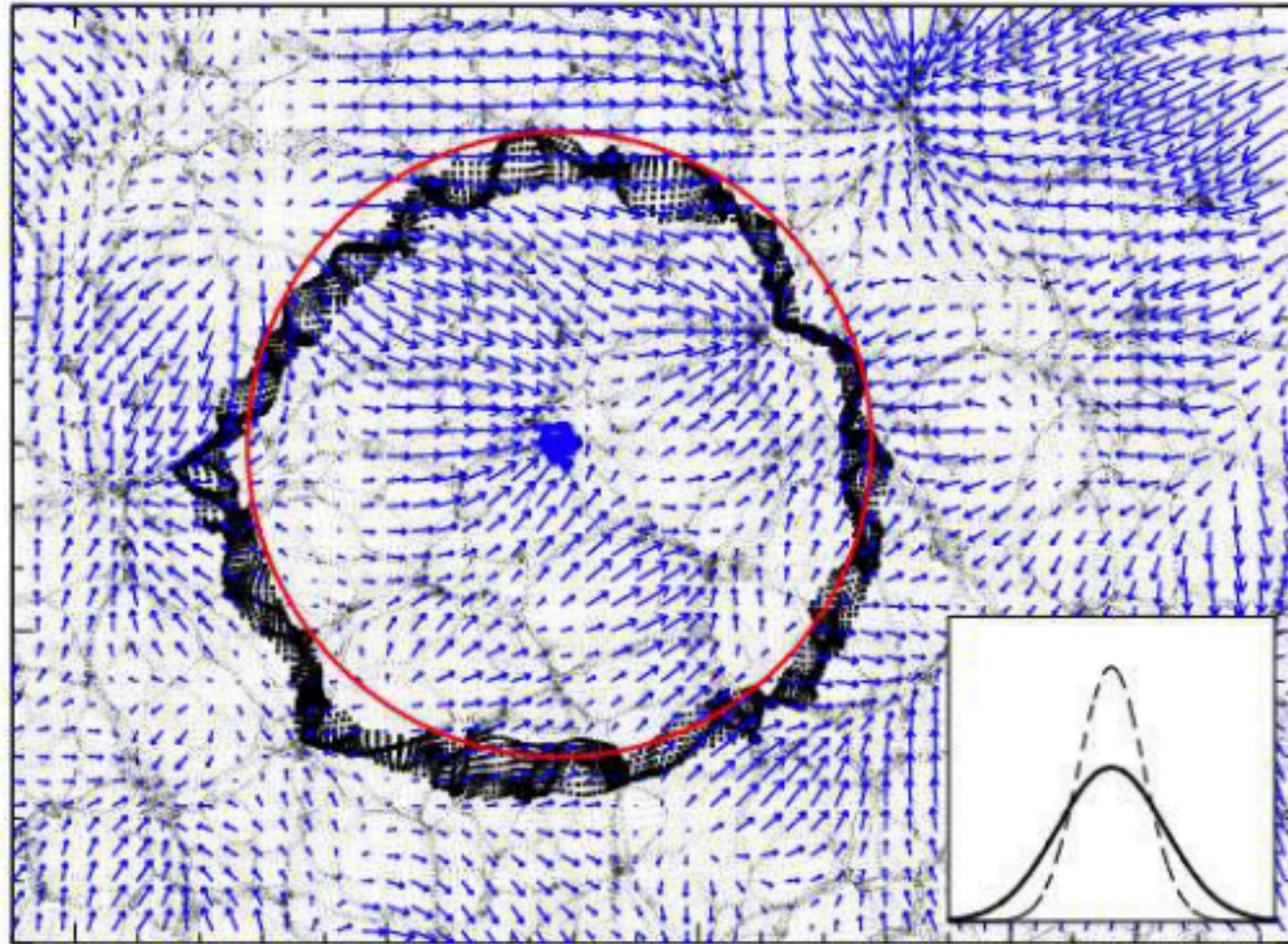
Baryon Acoustic Oscillations



- The BAO feature is expected to be **isotropic** !
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 - Broadening of the BAO peak in 2pt correlation function

Padmanabhan et al. (2012) MNRAS

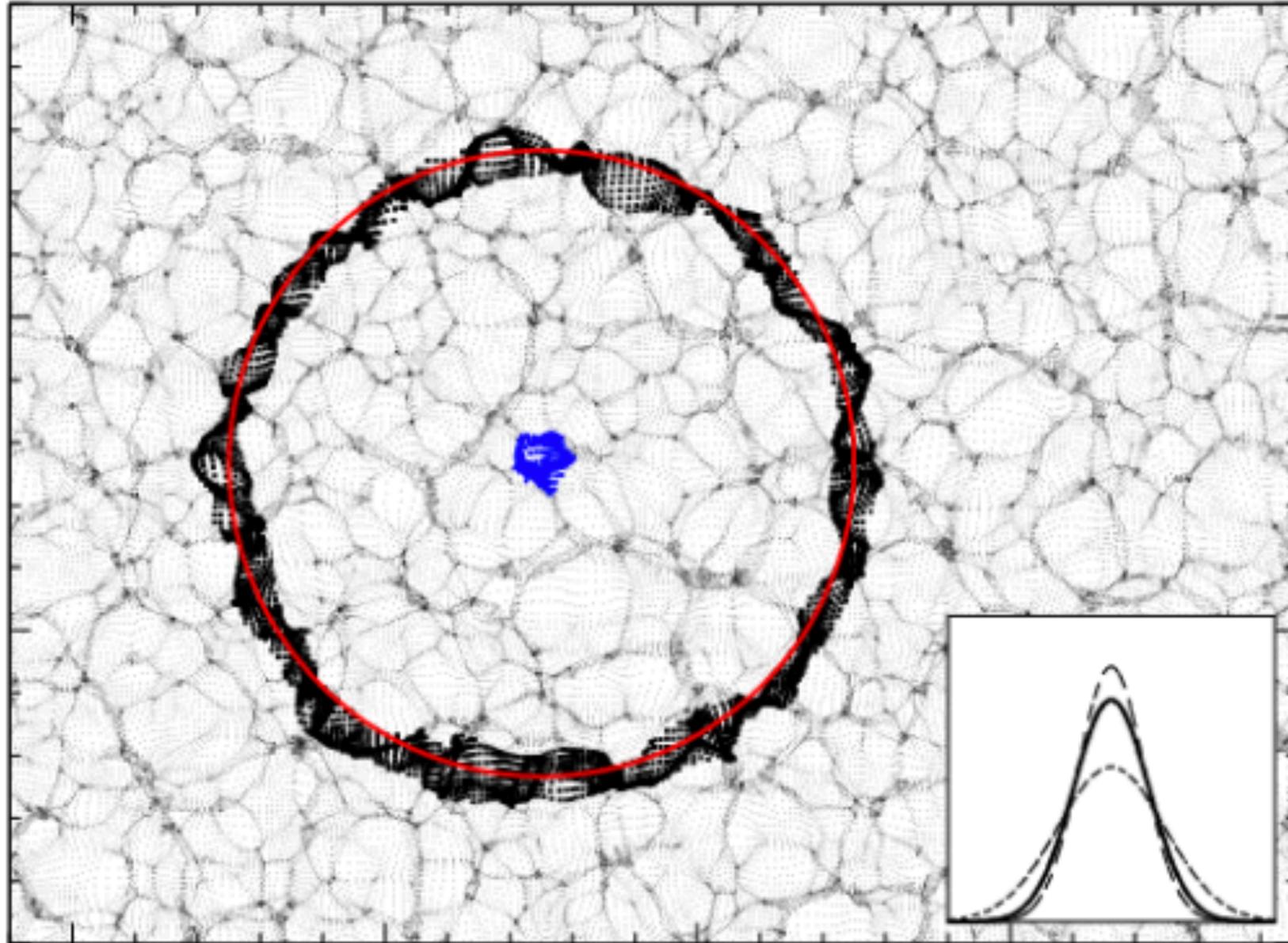
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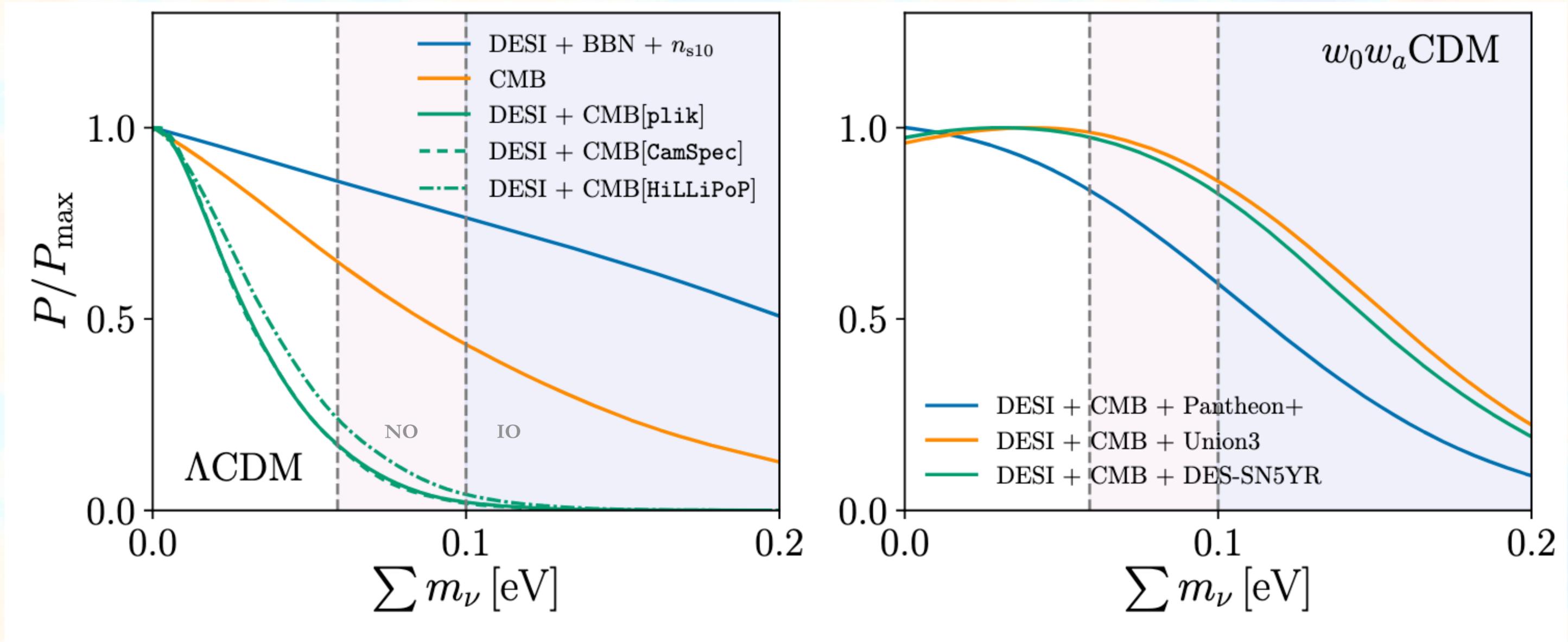
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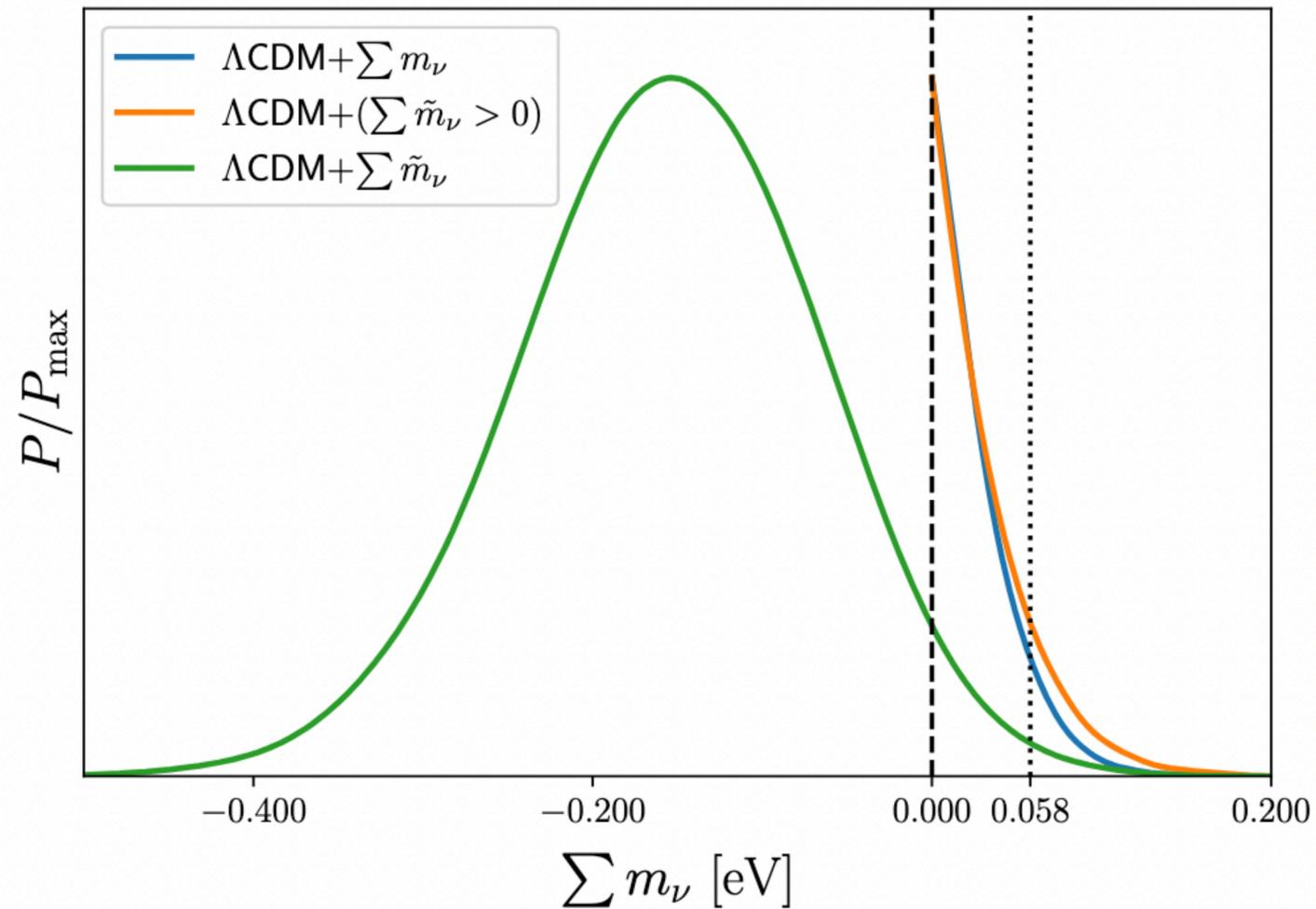
Ruling out inverted ordering for ν 's?



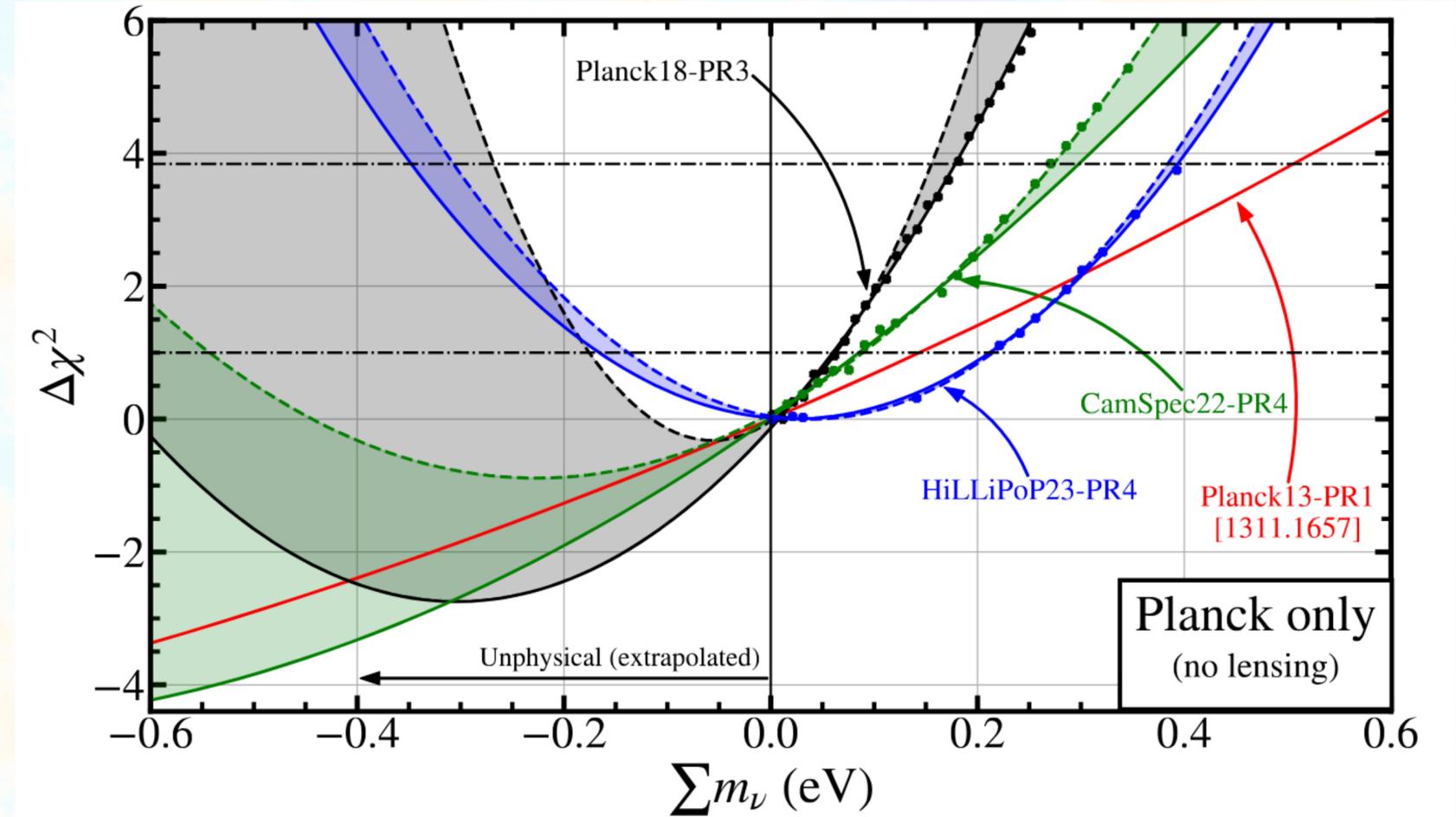
DESI Collaboration, A.G. Adame et al - arXiv: [2411.12022](https://arxiv.org/abs/2411.12022)

$$\Delta P(k)/P(k) \propto -\Omega_\nu/\Omega_m$$

Negative neutrino masses ?



Craig et al. [[2405.00836](#)]

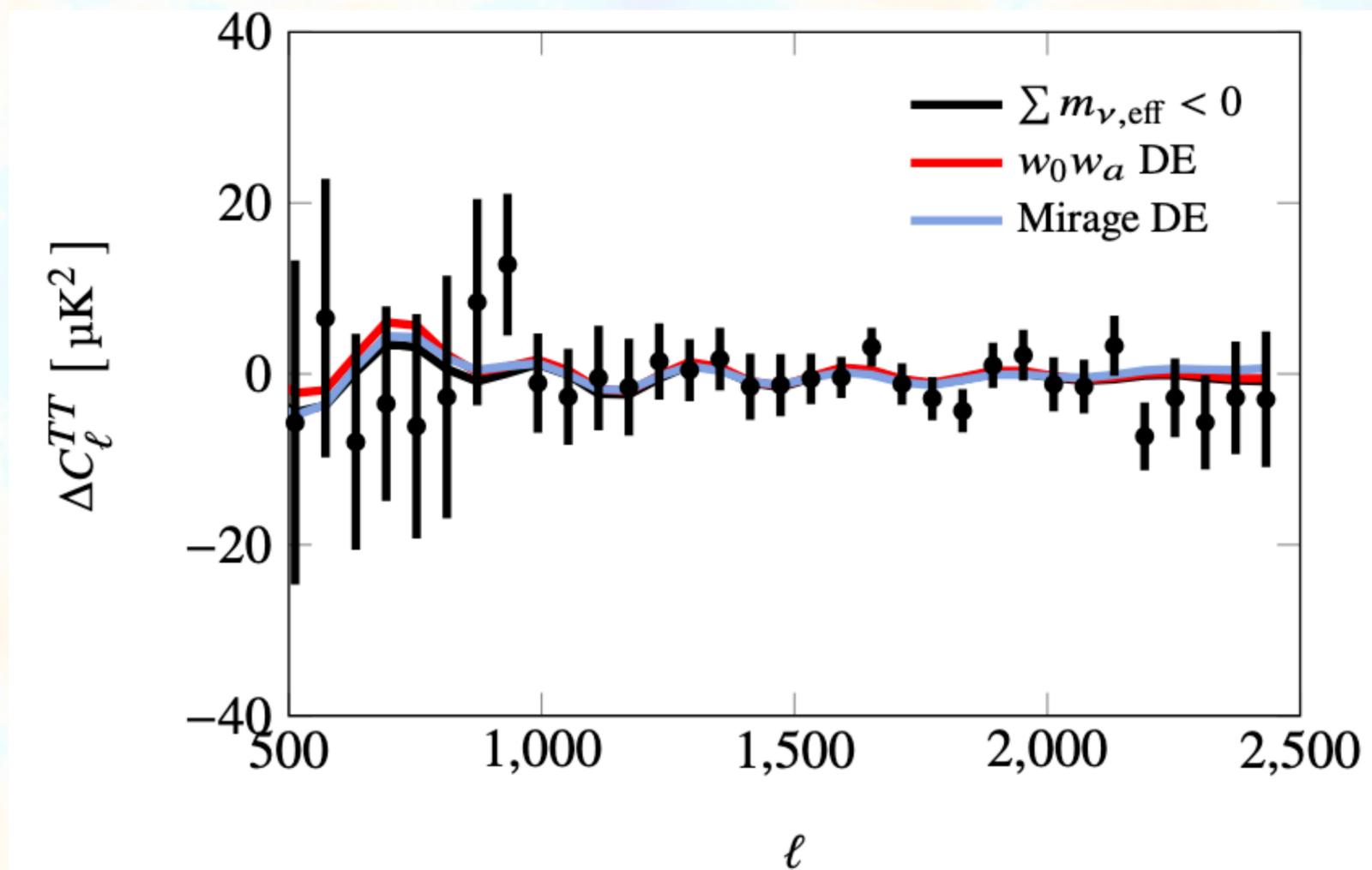


D. Naredo-Tuero et al. [[2407.13831](#)]

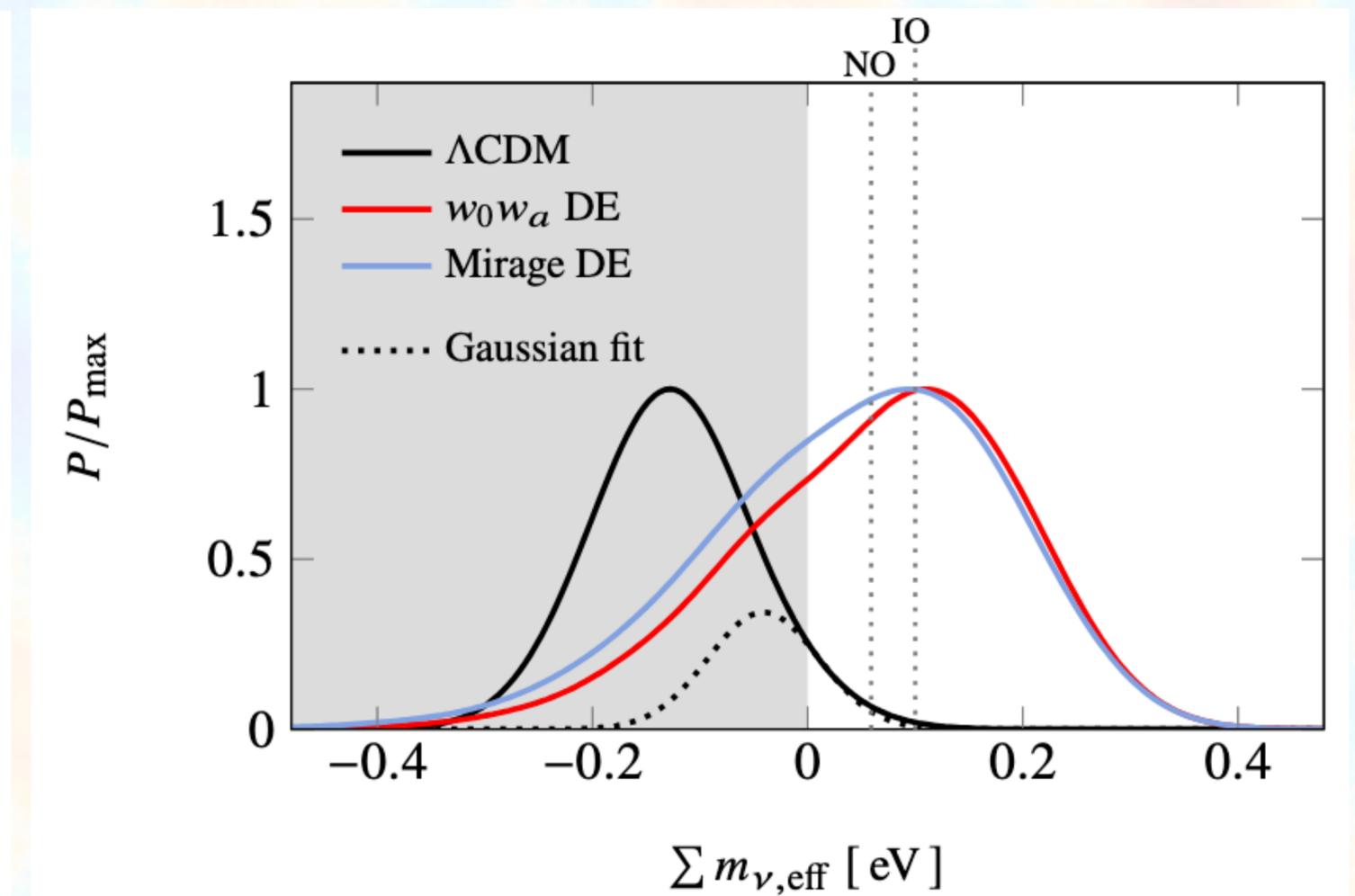
Tightly connected to the CMB lensing excess/anomaly ($A_{\text{lens}} > 1$)

Negative neutrino masses ?

$$X_{\theta}^{\sum m_{\nu, \text{eff}}} \equiv X_{\theta}^{\sum m_{\nu} = 0} + \text{sgn}(\sum m_{\nu, \text{eff}}) \left[X_{\theta}^{|\sum m_{\nu, \text{eff}}|} - X_{\theta}^{\sum m_{\nu} = 0} \right]$$



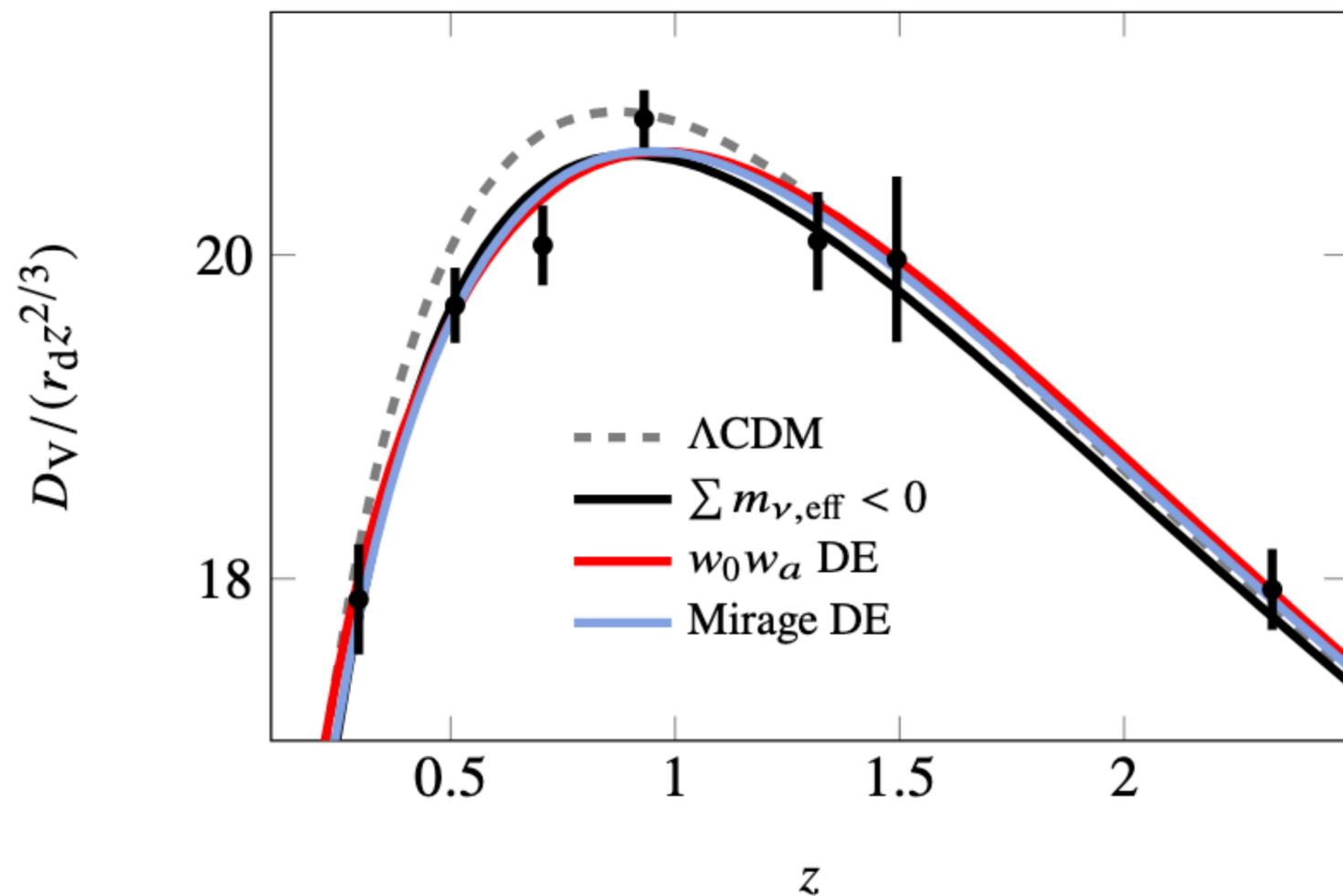
W. Elbers et al. [[2407.10965](#)]



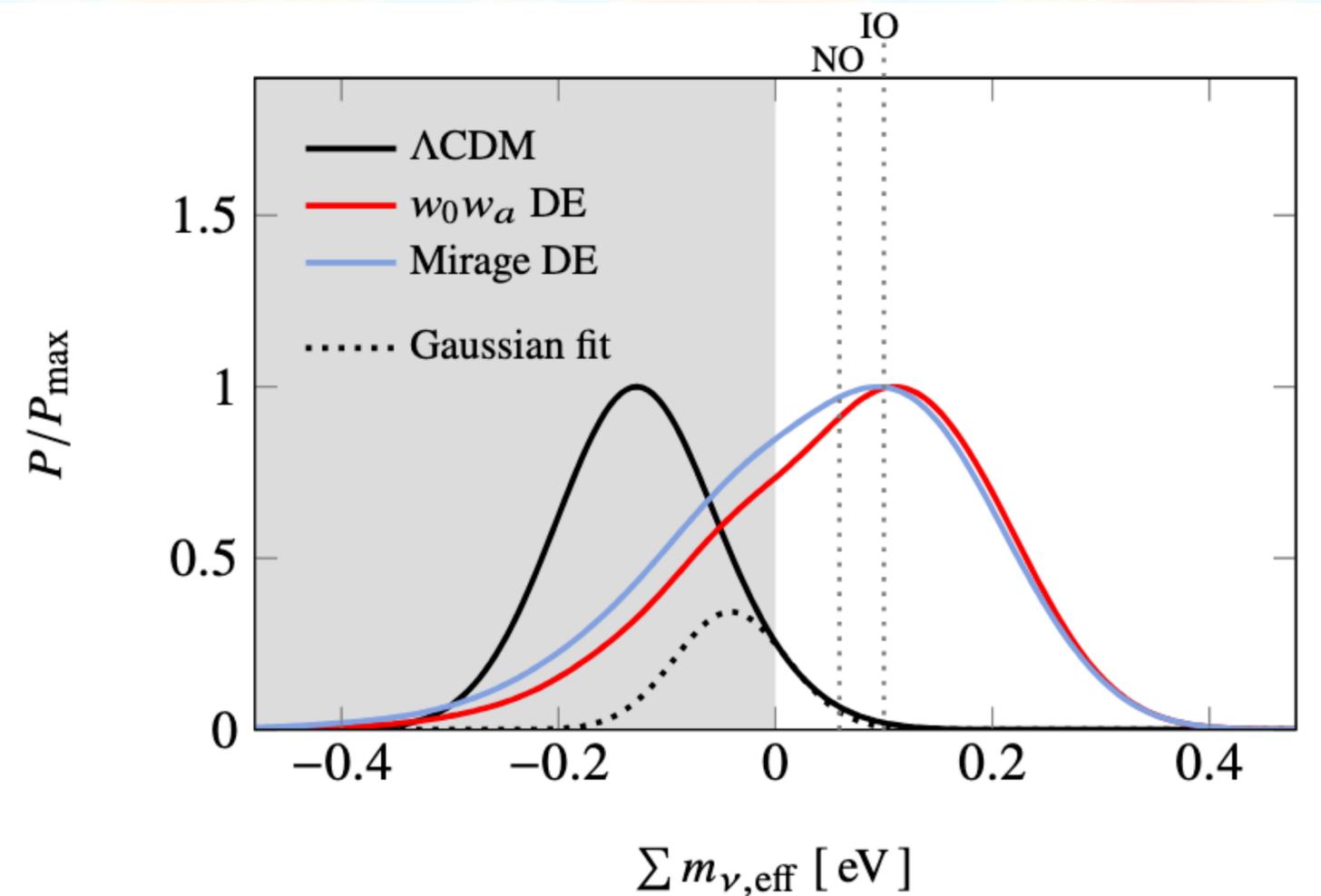
2.8 – 3.3 σ with tension neutrino oscillations

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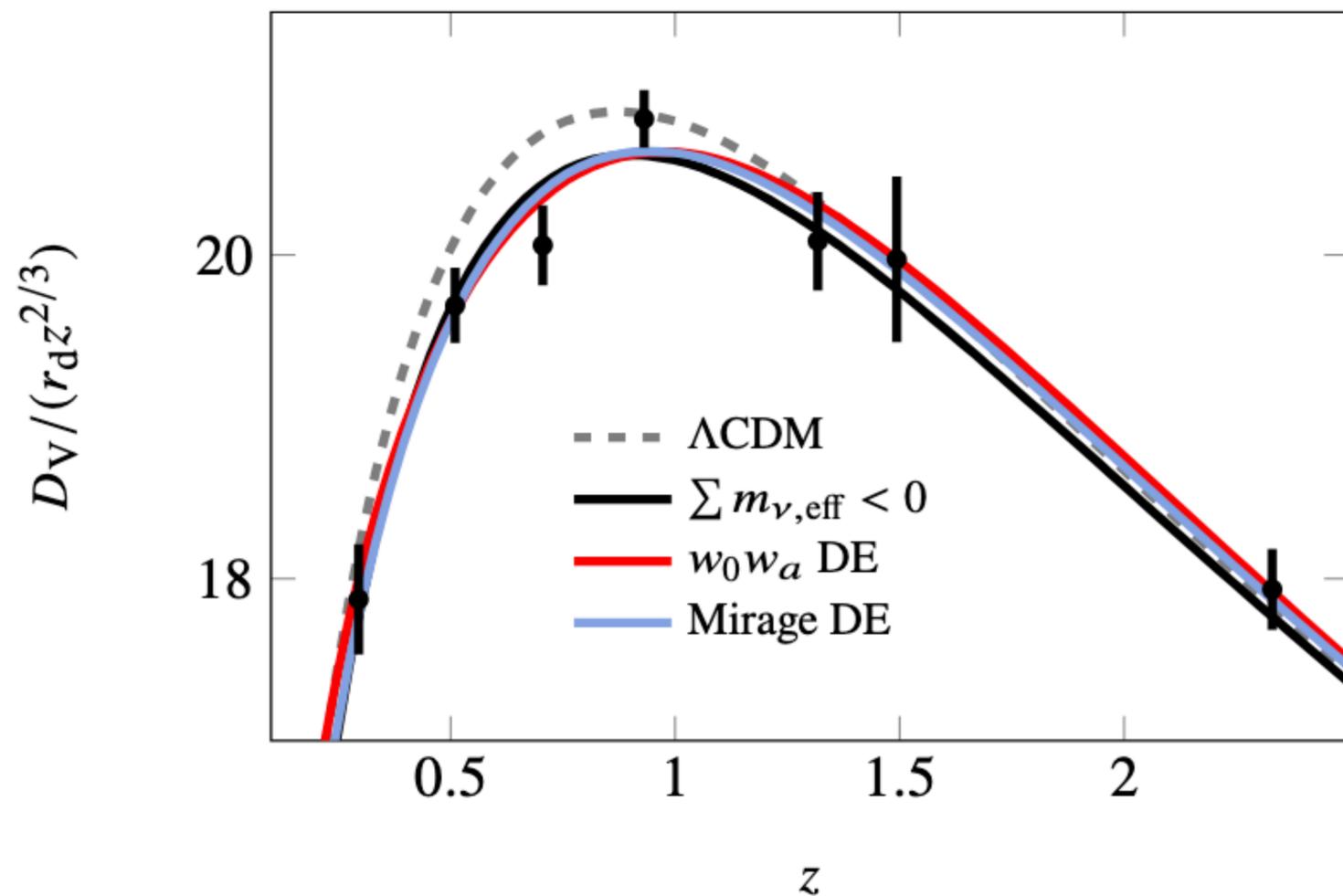
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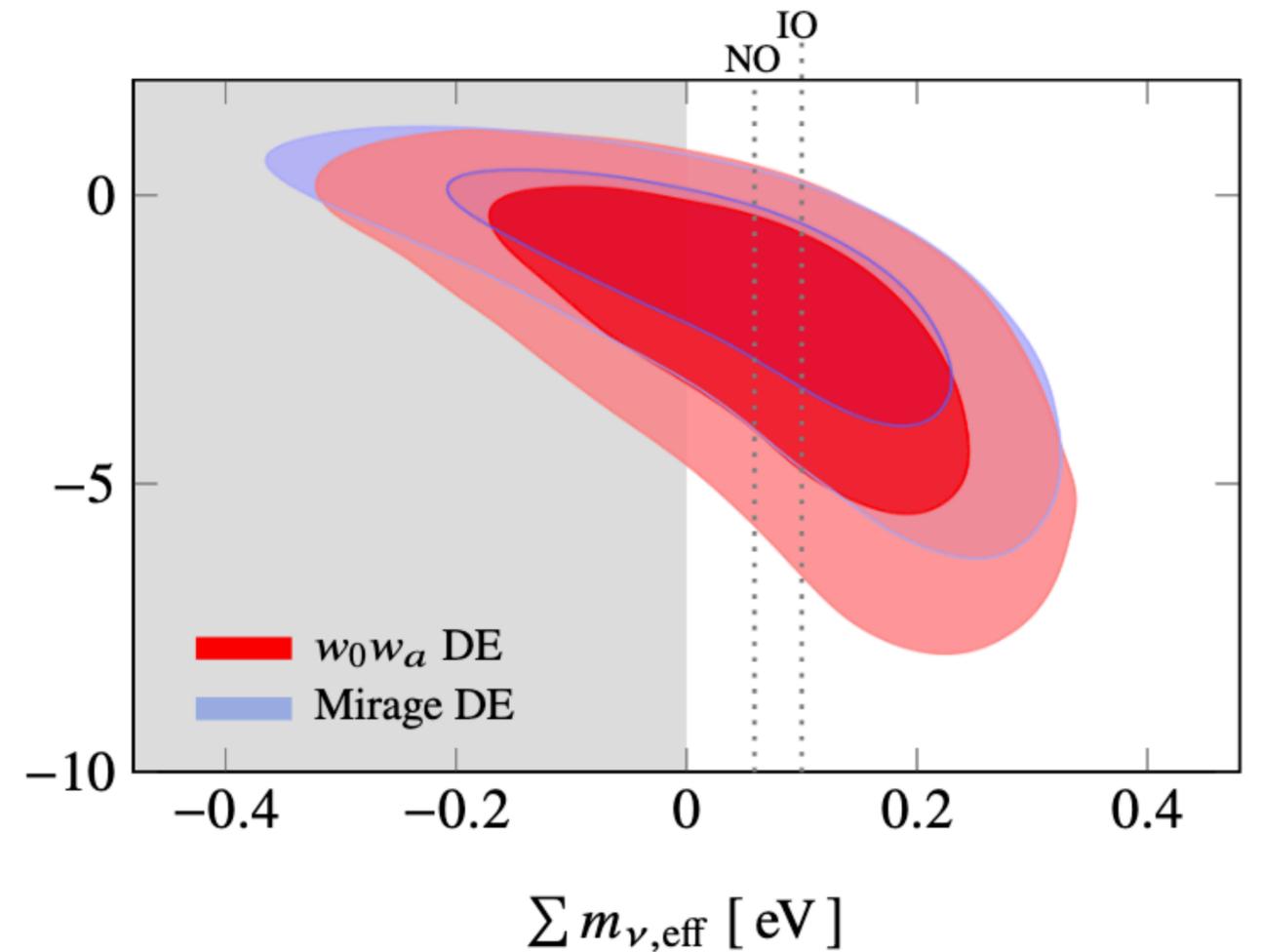
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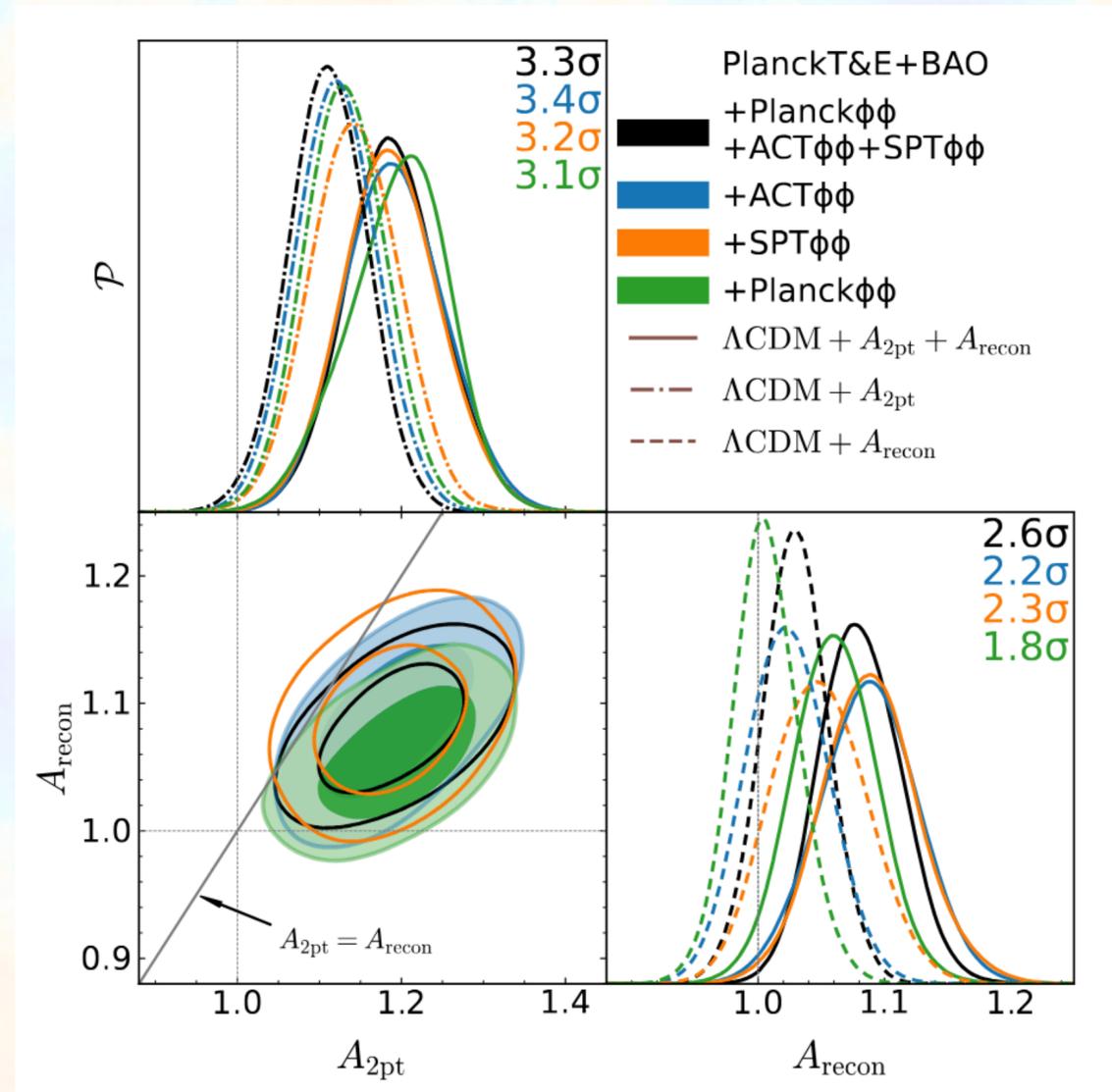
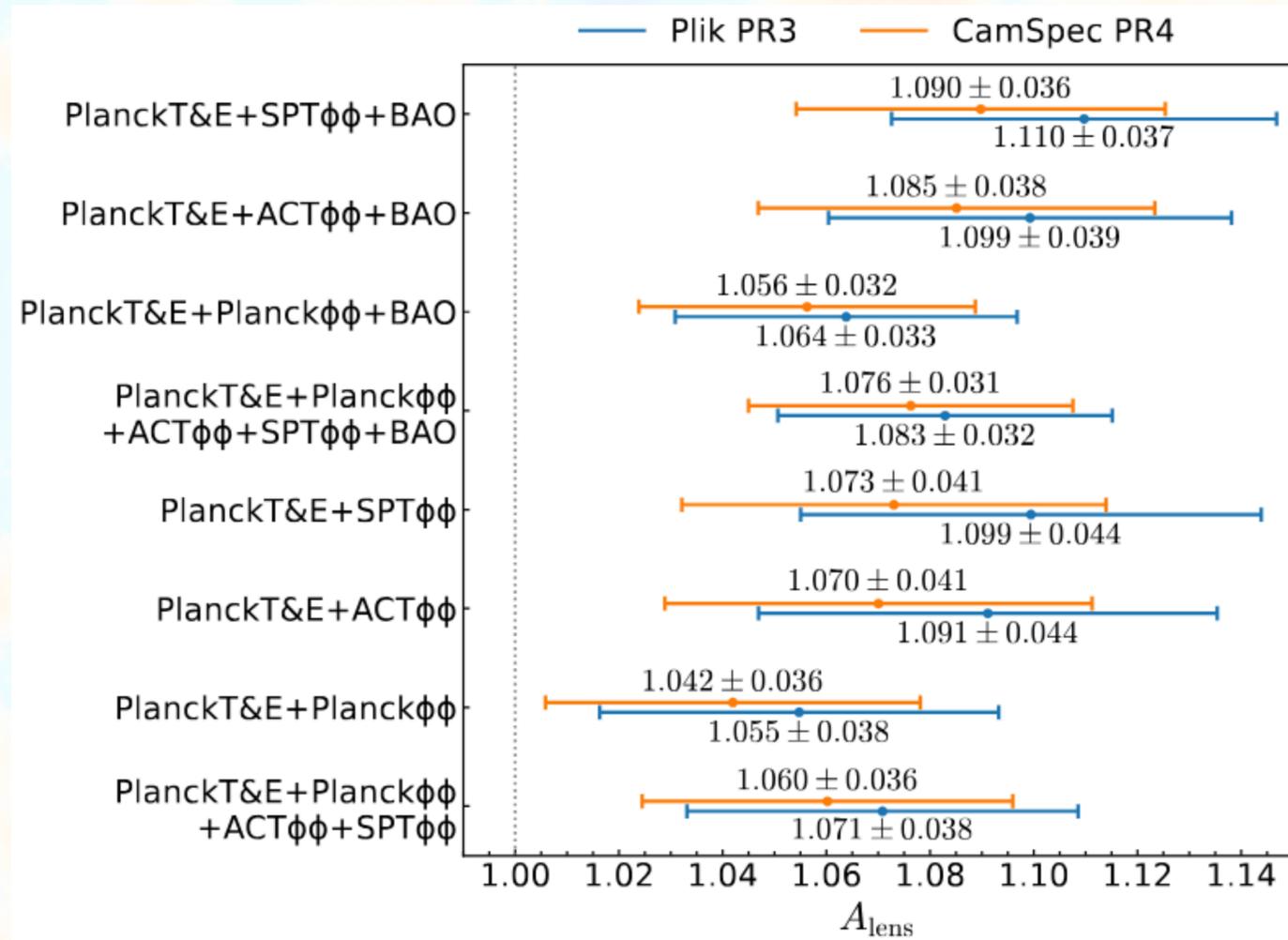
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2.8 – 3.3 σ with tension neutrino oscillations

Is there an excess of lensing?

Cosmology from CMB lensing and delensed EE power spectra using SPT-3G polarization data

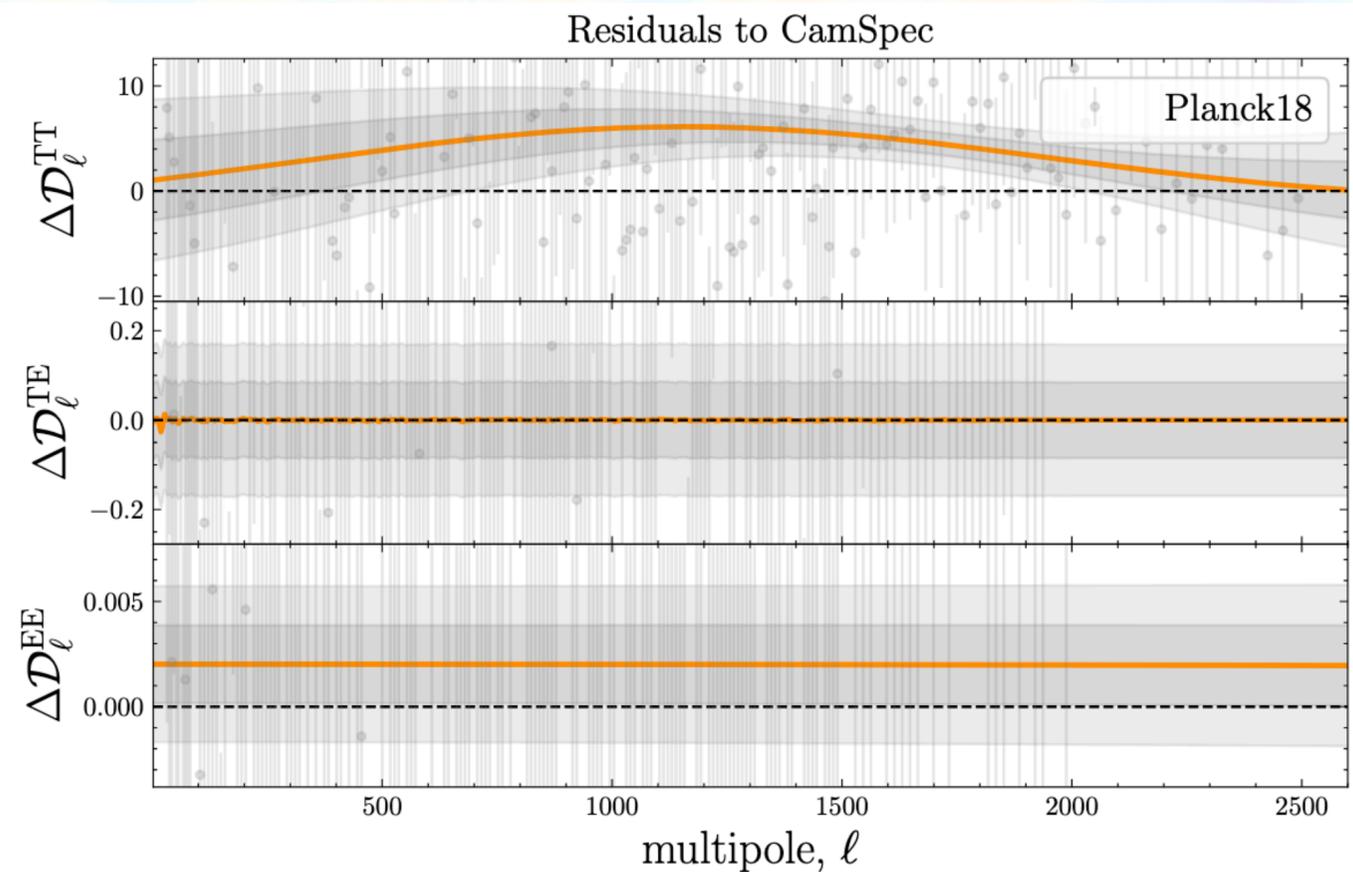
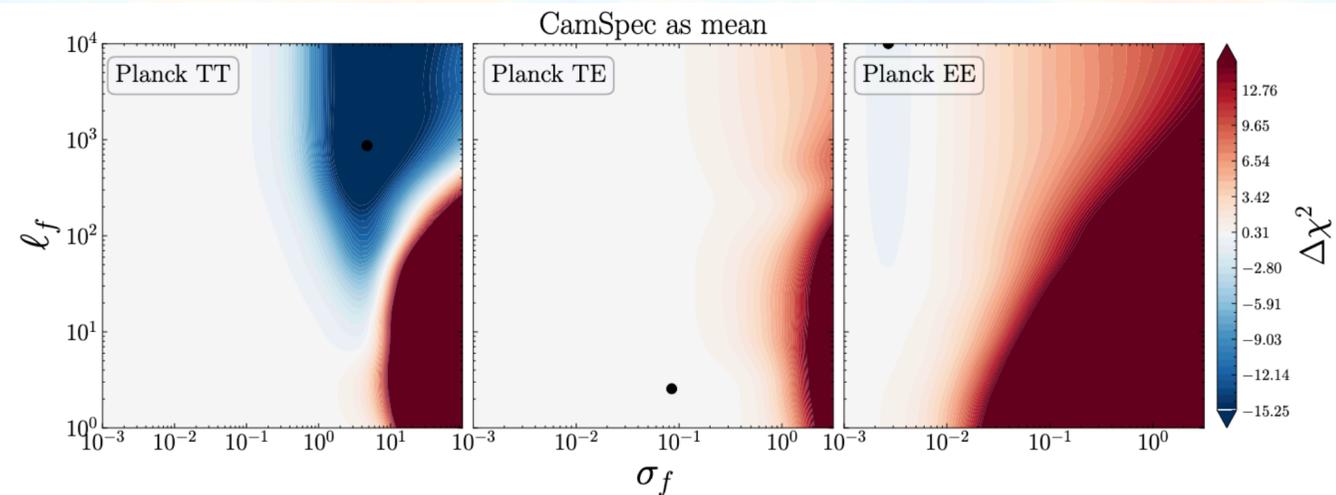
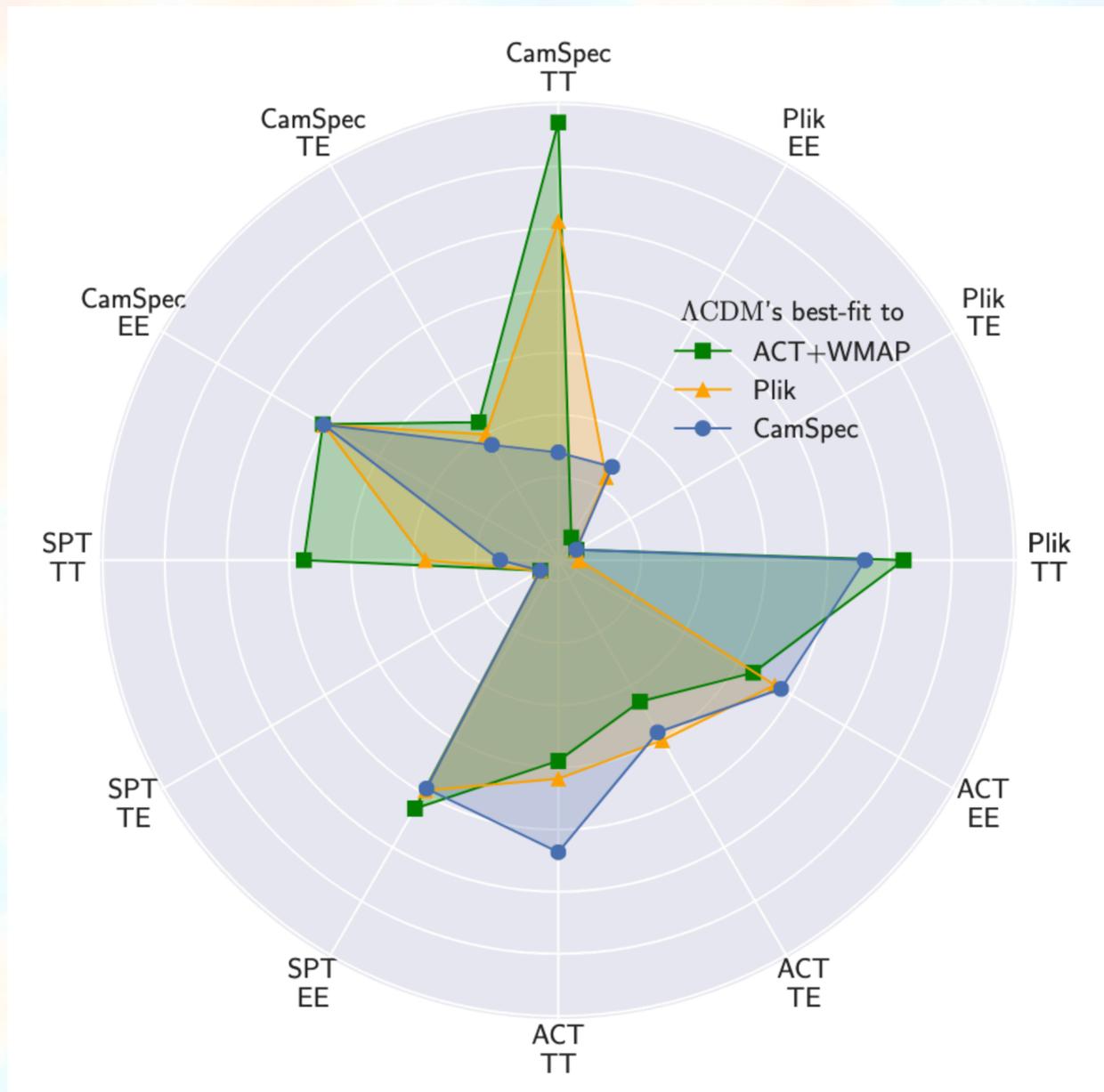


$$\Sigma \tilde{m}_\nu = -0.122 \pm 0.072 \text{ eV}$$

Neutrino-like lensing template

SPT Collaboration - Ge et al. [2411.06000]

Systematics in the data ?



R. Calderon, A. Shafieloo, D. Hazra, W. Sohn - *JCAP* 08 (2023) 059

The “cosmic calibration” tension

Standard “Candle”

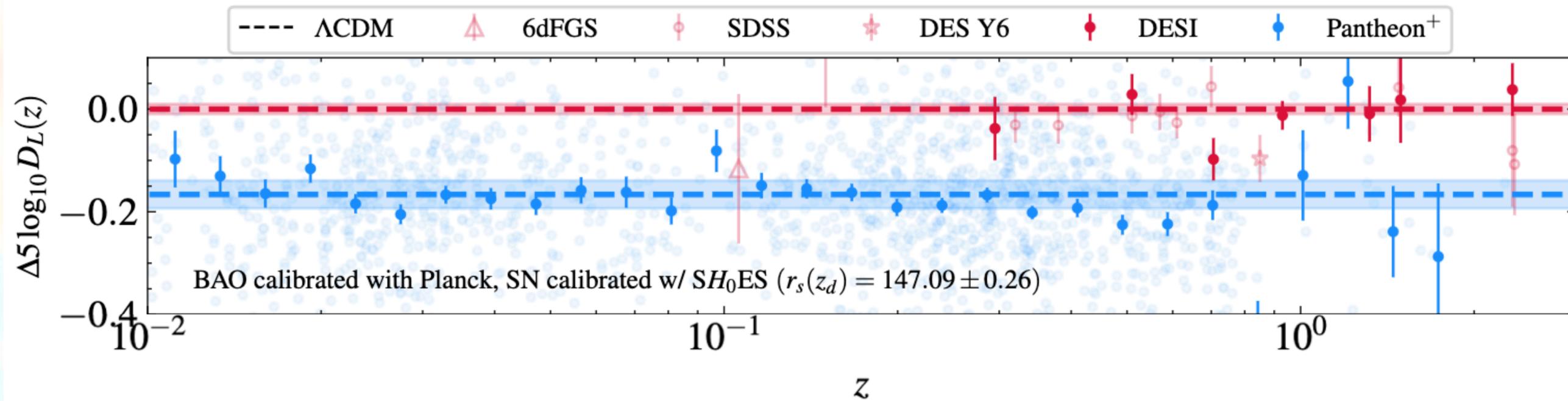
$$m_B(z) = 5 \log_{10} D_L(z) + 25 + M_B$$

Distance-Duality Relation
(DDR)

$$D_L(z) = (1 + z)^2 D_A(z)$$

Standard “Ruler”

$$\alpha_{\perp}(z_{\text{eff}}) \propto \frac{D_M(z_{\text{eff}})}{r_d} = \frac{D_A(z_{\text{eff}})}{r_d(1 + z_{\text{eff}})}$$



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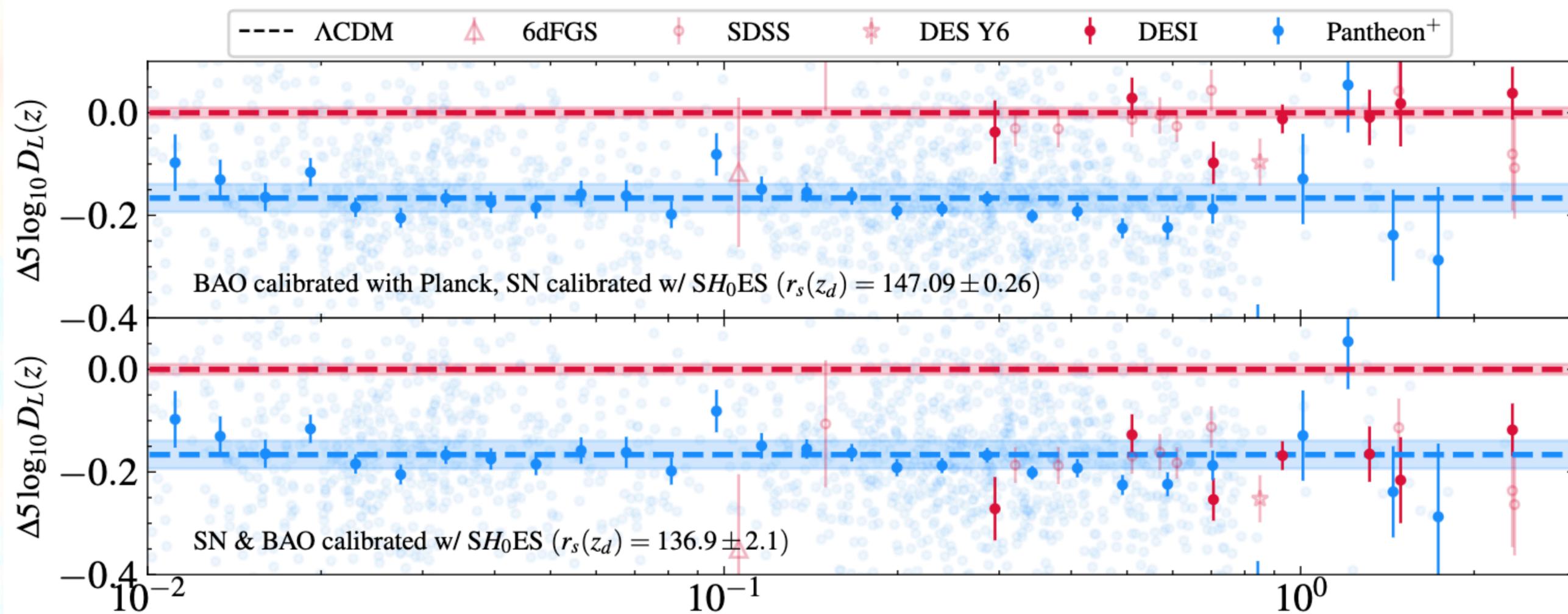
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V. Poulin, T. L. Smith, R. Calderon, T. Simon - arXiv: [2407.18292](https://arxiv.org/abs/2407.18292) z